On the variability of the Charnock constant and the functional dependence of the drag coefficient on wind speed

Part II Observations

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Abstract An analytical expression for the 10m-drag law in terms of the 10m wind speed at the maximum in the 10m drag coefficient, and the Charnock constant is presented, which is based on the results obtained from a model of the air-sea interface derived in Bye et al. (2010). This drag law is almost independent of wave age and over the mid-range of wind speeds ($5 - 17 \text{ ms}^{-1}$) is very similar to the drag law based on observed data presented in Foreman and Emeis (2010). The linear fit of the observed data, which incorporates a constant into the traditional definition of the drag coefficient is shown to arise to first-order as a consequence of the momentum exchange across the air-sea boundary layer brought about by wave generation and spray production which are explicitly represented in the theoretical model.

Keywords Air-sea momentum exchange · Charnock constant · inertial coupling

1 Introduction

The purpose of this paper is to bring together the results of several studies of the drag coefficient in the air-

sea boundary layer presented in a recent observational paper (Foreman and Emeis 2010), and the theoretical predictions for the drag coefficient presented in Bye et al. (2010). At the time of writing of the latter paper the analysis of the observational results was not available. Here we show the basic agreement of the theoretical model with the observations, and also discuss the conclusions of the theoretical model as a description of the various sea states that are encountered.

This paper is essentially Part 2 of Bye et al. (2010), which for brevity we call Part 1. A full historical summary of the programmes on which the observed drag law is based can be found in Foreman and Emeis (2010), and equally the background analysis for the theoretical drag law can be found in Bye et al. (2010). An explicit representation of the theoretical results for the 10m drag law and the Charnock constant in Part 1, however is given for the first time in this paper.

In Section 2 the physical processes on which the theoretical model is based are discussed, and in Section 3 the analytical expression for the 10m-drag coefficient based on the results in Part 1, which are presented in the Appendix, is given. An important subsection (Section 3.1) introduces the use of the Charnock constant as a constraint on the prediction for the drag coefficient, derived from the observed wind and wave properties at the maximum of the 10m-drag coefficient. Section 3.2 demonstrates the key result that the drag law is almost independent of wave age.

In Section 4 the observations presented in Foreman and Emeis (2010) and also in a later paper by Andreas et al. (2012) are critically discussed, and it is shown that the theoretical model for the drag coefficient is a good representation of the observations in which the simple linear regression relation for the drag used in the observational study arises as a fundamental prop-

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erty. The complementary nature of the physical models presented in Foreman and Emeis (2010) and in this paper is discussed in the Conclusion (Section 5).

2 The physical processes

There are three processes which govern the construction of the model for the 10m drag law, $u_* = \sqrt{K_{10}} \cdot u_{10}$ where u_* is the friction velocity in air, u_{10} is the 10m wind speed and K_{10} is the 10m drag coefficient, proposed in Bye et al. (2010). The first process is wave generation, which is represented by the relation,

$$c_0 = Bu_1 \quad (1)$$

where $c_0 = gT/2\pi$ is the peak wave speed in which g is the acceleration of gravity and T is the peak wave period, and u_1 is the surface wind speed which occurs at the height, $z_B = 1/(2k_0)$ where $k_0 = g/c_0^2$ is the peak wave number, and B is a wave generation parameter, which is determined by the nature of the wind field which generates the wave field as discussed in Section 3.2. The second process is frictional drag in the air-sea boundary layer, which is represented by the relation,

$$u_* = \frac{\sqrt{K_I}}{R} u_1 \quad (2)$$

where K_I is the inertial drag coefficient¹ and R is a frictional parameter which quantifies the relative contributions of the velocity shear in the wave boundary layer due to wave motion and turbulence. The wave induced shear, which is due to the Lagrangian Stokes drift of the wave spectrum, is the difference between the Stokes drift at the sea surface and that at the bottom of the wave boundary layer which is zero, and the turbulent shear, which is due to the Eulerian velocity shear, is the difference between the frictional current at the sea surface and the surface current (u_2) at the bottom of the wave boundary layer. For $R < 1$ the turbulent shear has the same sign as the wave shear, for $R = 1$, the ratio of turbulent/wave shear is zero, and for $R > 1$ the turbulent shear is of opposite sign to the wave shear indicating a return of momentum from the ocean to the atmosphere by frictional drag, see Part 1. The consideration of near surface shear in both fluids is a central feature of the model. The third process is

¹ The inertial drag coefficient is defined by the drag relation, $u_* = \sqrt{K_I}(u_1 - u_2/\epsilon)$ in terms of u_1 and the surface current speed, u_2 , which occurs at the depth $1/(2k_0)$, where $\epsilon = \sqrt{(\rho_1/\rho_2)}$ in which ρ_1 and ρ_2 are respectively the density of air and water. K_I is a property of the irrotational wave spectrum without recourse to frictional processes and field observations from the fully developed growing wind-wave sea indicate that $K_I = 0.0015$ (Bye and Wolff 2008).

the generation of spray which is represented through the relation,

$$R = \frac{R_0}{1 - au_*} \quad a > 0 \quad (3)$$

in which a is the spray parameter and R_0 is the friction parameter at very low friction velocities. This relation enables R to be evaluated in terms of u_* , and the increase in R as u_* increases shows that the spray (and the associated processes of whitecapping and slip) essentially return momentum to the atmosphere. The use of (3) leads to drag laws in which there is a maximum in the 10m drag coefficient.

The three parameters (B , R_0 and a) were expressed in Part 1 in terms of three properties of the wavefield at the maximum in drag coefficient, namely the 10m wind speed (u_{10m}), the drag coefficient maximum (K_{10m}) and the peak wave period (T_m). Hence in the model on assuming these quantities to be known, there are no disposable constants. Note that the maximum friction velocity, $u_{*m} = \sqrt{K_{10m}} \cdot u_{10m}$ and the maximum wave speed, $c_{0m} = gT_m/2\pi$ follow from these three quantities.

3 The 10m drag law

The model has a universal character on the assumption that (3) realistically represents the spray/surface slip mechanism, and its application yields a 10m drag law which was shown to be almost independent of the wave generation parameter (B). This was illustrated for two values ($B = 0.66$ and $B = 1.30$) in Fig. 3 of Part 1, from which it was concluded that the 10m drag law was almost independent of wave age ($W = c_0/u_*$).

Here we build on the results of Part 1 by deriving an explicit relation for the 10m drag law which illustrates this conclusion.

This procedure essentially requires a transformation of the physical results for which the natural vertical scale is the thickness of the wave boundary layer (z_B) to the reference height of 10m upon which the 10m drag coefficient is defined. For a logarithmic velocity profile, this transformation yields,

$$u_{10} = u_1 + \frac{u_*}{\kappa} \ln \frac{z_{10}}{z_B} \quad (4)$$

where $z_{10} = 10\text{m}$ and $\kappa = 0.4$ is von Kármán's constant, and in which from (1) and (2) $u_1 = Ru_*/\sqrt{K_I}$ and $z_B = 1/2(BRu_*)^2/(gK_I)$. Hence,

$$\frac{1}{\sqrt{K_{10}}} = \frac{R}{\sqrt{K_I}} - \frac{1}{\kappa} \ln \frac{(BRu_*)^2}{2gz_{10}K_I} \quad (5)$$

On invoking (3) and differentiating (5) with respect to u_* assuming that B is a constant, and then evaluating

at the maximum in the 10m drag coefficient (K_{10m}),
after some algebra, we obtain,

$$R_m = R_0 + 2 \frac{\sqrt{K_I}}{\kappa} \quad (6)$$

in which R_m is the friction parameter at K_{10m} (Bye et al. 2010). Note that $R_m > R_0$ indicating the return of momentum to the air which is occurring due to the production of spray. This innocent looking relation enables the 10m drag law to be explicitly evaluated in terms of the sea state occurring at the drag coefficient maximum, namely the 10m wind velocity (u_{10m}), the 10m drag coefficient (K_{10m}) and the peak wave speed (c_{0m}), as is shown in the Appendix. The resulting universal relation (A5) for u_{10} in terms of u_* is,

$$u_{10} = A(s)u_* + su_{10m} \quad (7)$$

where

$$A(s) = \frac{2}{\kappa} \left\{ \frac{X(s-1)}{(X-s)} - \ln \left[\frac{(X-1)s}{(X-s)} \right] \right\}$$

in which κ is von Kármán's constant, $s = u_*/u_{*m}$ and $X = 1/(au_{*m})$, which may be inverted to yield the 10m drag law,

$$u_* = \sqrt{K_{10m}} \cdot u_{10} - \sqrt{K_{10m}} \cdot A(s)u_* \quad (8)$$

In (8), $(-\sqrt{K_{10m}} \cdot A(s)u_*)$ may be regarded as an offset to a simple drag law in which at all wind speeds the drag coefficient is equal to its maximum value. For $A(s) > 0$, this term reduces the drag coefficient as the wind speed decreases.

3.1 The use of the Charnock constant in the specification of the drag law

The additional requirement that the value of the Charnock constant,

$$\alpha_0 = \frac{gz_0}{u_*^2} \quad (9)$$

where z_0 is the sea surface roughness length, agrees with observations, leads to a preferred choice for the value of K_{10m} , which is not well defined by observation, and the restriction of the model to "aerodynamically" rough conditions which occur at the onset of wave growth at $u_{10} > 3 \text{ ms}^{-1}$ (Bye and Babanin 2009) implies that in the comparison with observations the Charnock constant should be evaluated from the theoretical model at this threshold wind speed, see Appendix.

The results in the Appendix assuming that $K_{10m} = 0.002$, $u_{10m} = 40 \text{ ms}^{-1}$ and $T_m = 17.6 \text{ s}$ ($c_{0m} = 27.6 \text{ ms}^{-1}$) lead to the following properties for the drag law: $X = 5.15$ (A2), $a = 0.11$ (A14) and $B = 0.60$ (A4). For these parameters, on assuming that the onset of wave

growth occurs at $s = 0.05$, we find in agreement with observations for the fully developed sea, that from (A5) $u_{10} = 3.0 \text{ ms}^{-1}$ and from (A13) $\alpha = 0.018$. On using this calibration, we also find that the friction parameter, R (A1) increases from 0.81 at the onset of wave growth ($s = 0.05$) to 1.00 at the maximum in drag coefficient ($s = 1$), and that the wave age, W (A10) increases from 12.5 to 15.4 over the same range.

This set of conditions is a model for the interactions described in Section 2, and the peak wave period at the maximum in drag coefficient (T_m) shows that the full range of sea state conditions which give rise to a maximum in the 10m drag coefficient is achievable in the open ocean, and also that at this maximum, the near surface shear is mainly due to the wave motion ($R \approx 1$). The prediction for the wave generation parameter, B , indicates that there is a slip of about 0.6 between the surface wind speed and the peak wave speed which arises from the large scale properties of the storm systems which generate the wave field.

3.2 Sensitivity of the drag law to the peak wave period at the maximum drag coefficient

The relation (A2) shows that X increases as T_m increases and X decreases as T_m decreases. The 10m drag coefficient $K_{10}(u_{10})$ derived by interpolation from the inverse drag law (A5) for two widely different maximal peak wave periods, $T_m = 5 \text{ s}$ ($X = 3.89$) and $T_m = 50 \text{ s}$ ($X = 6.19$) is shown in Fig. 1 in comparison with that for $T_m = 17.6 \text{ s}$ discussed in Section 3.1. It is clear that the 10m drag coefficient is hardly influenced by these large changes in peak wave conditions over which the Charnock constant, α , only varies from 0.016 for $T_m = 5 \text{ s}$ to 0.019 for $T_m = 50 \text{ s}$. Hence the theoretical drag law may be said to be almost independent of wave age. From (A4) however, the wave generation parameter has a large variability, ranging from $B = 1.41$ at $T_m = 50 \text{ s}$ to $B = 0.22$ at $T_m = 5 \text{ s}$.

This conclusion indicates that the observed drag law may conceal many possible sea state regimes. A well known regime is the fully developed sea (Toba 1973) in which the wave age,

$$W = A \quad (10)$$

where $A = 1/0.029(34.5)$. On the assumption that (10) is applicable at a moderate wind speed, for example $s = 0.2$ ($u_* = 0.36 \text{ ms}^{-1}$), on applying (A10) using (A2), we find that $X = 6.1$ and hence $a = 0.09 \text{ m}^{-1}\text{s}$, $B = 1.31$ and $R = 1.02$. This regime differs from the open ocean regime in so far as the special conditions of a steady constant wind give rise to a regime of reduced spray production (smaller a) and more efficient wave

Fig. 1 The theoretical 10m drag coefficient, K_{10} , as a function of u_{10} derived by interpolation from (A5) for three maximal peak wave periods: (a) $T_m = 5$ s, (b) $T_m = 17.6$ s and (c) $T_m = 50$ s.

Fig. 3 The friction velocity (u_*) as a function of the 10m wind speed (u_{10}): (a) from the linear fit (11) to the observational data, (b) from the linear fit (12) to the theoretical relation (A5), (c) from the theoretical relation (A5) for $T_m = 17.6$ s.

production (larger B) in which the wave shear dominates the turbulent shear ($R \approx 1$). This regime however never extends to the maximum in drag coefficient which from (A10) would occur at a wave period, $T_m = 46$ s, which is not achievable in the ocean. Similar conclusions are found for other moderate values of friction velocity. This constant wave age regime was originally discussed on the assumption that $R = 1$ in Bye and Wolff (2004) where it was shown that this model was in excellent agreement with observational data (Garratt 1992). An important property of this theoretical model for the fully developed sea is that from (A9), $\alpha = 0.019$ which is in good agreement with observations (Wu 1980).

Fig. 2 The offset $(-\sqrt{K_{10m}}A(s)u_*)^{1/2}$ of the square root of the 10m drag coefficient (8) as a function of u_{10} for (a) $T_m = 5$ s, (b) $T_m = 17.6$ s and (c) $T_m = 50$ s.

4 Comparison with observations

In a recent analysis of several sets of observations in various locations Foreman and Emeis (2010) proposed that the most appropriate definition of the drag law for the air-sea interface is of the form,

$$u_* = C_m u_{10} + b \quad (11)$$

where C_m and $b < 0$ are constants. In their analysis of the various data sets the linear relation (11) was obtained by restricting the data to $u_{10} \geq 8 \text{ ms}^{-1}$ which yielded $C_m = 0.051$ and $b = -0.14 \text{ ms}^{-1}$. On evaluating (11) at $u_{10} = 8 \text{ ms}^{-1}$, $u_* = 0.27 \text{ ms}^{-1}$, which the authors claimed to be equal to the onset of aerodynamically rough flow. It is clear from Fig. 2 of Foreman and Emeis (2010) however that the linear relationship extends to a lower friction velocity of about 0.10 ms^{-1} ($u_{10} = 5 \text{ ms}^{-1}$) and it also only extends to an upper friction velocity of about 0.85 ms^{-1} ($u_{10} = 17 \text{ ms}^{-1}$). At a higher friction velocity u_* tends to become proportional to u_{10} with no offset. In a later more extensive observational study (Andreas et al. 2012) the coefficients of similar linear regressions for $u_{10} \geq 9 \text{ ms}^{-1}$ from aircraft and tower data (778 values) and from a much larger low flying aircraft data set (4878 values) for stable and weakly unstable conditions were respectively ($C_m = 0.0581, b = -0.214 \text{ ms}^{-1}$) and ($C_m = 0.0585, b = -0.243 \text{ ms}^{-1}$).

The evaluation of (8) yields a theoretical value for C_m of 0.045 ($K_{10m} = 0.002$), and Fig. 2 shows the offset $(-\sqrt{K_{10m}}A(s)u_*)^{1/2}$ as a function of u_{10} . Over the range,

$5 \leq u_{10} \leq 17 \text{ ms}^{-1}$, the offset is almost constant for each T_m with a mean value of about -0.07 ms^{-1} , which is almost independent of T_m . This range corresponds approximately with that in Foreman and Emeis (2010) over which (11) is applicable. Hence over this range, the linear relation for the friction velocity derived from (8) is,

$$u_* = 0.045 \cdot u_{10} - 0.07 \quad (12)$$

which is of the same form as the observed data (11) although the coefficients in the regression are slightly different. The theoretical model (Fig. 2) indicates that the offset decreases at higher $u_{10} < u_{10m}$ as is indicated in the observational data, becoming zero at u_{10m} , and also decreases at lower u_{10} as is evidenced by (12) which yields $u_* = 0.065 \text{ ms}^{-1}$ at $u_{10} = 3.0 \text{ ms}^{-1}$ instead of $u_* = 0.090 \text{ ms}^{-1}$ from (A5).

Over the mid range of wind speed ($5 \leq u_{10} \leq 17 \text{ ms}^{-1}$), Fig. 3 indicates that the linear relation (12) is very similar to the observational linear relation (11) of Foreman and Emeis (2010).

Observational estimates of K_{10m} however are inconclusive, see for example Bye et al. (2010), and it is clear from (8) that a higher value of K_{10m} would increase the slope of the theoretical linear regression, e.g. for $K_{10m} = 0.0025$ the slope would be 0.050 rather than 0.045, which is in better agreement with the observations. However, the choice of $K_{10m} = 0.002$ yields Charnock constant at the onset of wave generation, $\alpha = 0.018$ in good agreement with observations. A higher value of K_{10m} would yield a much larger Charnock constant, and for $u_{10} = 40 \text{ ms}^{-1}$, $T_m = 17.5 \text{ s}$ and $K_{10m} = 0.0025$, $\alpha = 0.035$, see (A13). For this reason we have chosen $K_{10m} = 0.002$ in the evaluation of the theoretical model, however there is an uncertainty here that is not yet resolved.

Fig. 3 also shows that the linear relation (12) is in close agreement with the theoretical relation derived from (A5) for $T_m = 17.6 \text{ s}$ over the complete range of wind speed from the onset of waves at 3 ms^{-1} up to at least 60 ms^{-1} . There is however an important difference between (12) and (A5). The small scale structure of (A5) shows the occurrence of the maximum in drag coefficient at 40 ms^{-1} (Fig. 3), whereas there is no evidence of this maximum in the fitted linear relation (9).

This is a major problem in the use of linear regressions in defining the drag coefficient at very high wind speeds. The high wind speed asymptotic drag coefficient (C_m^2) may be much greater than that occurring at say 40 ms^{-1} , and the difference depends critically on the intercept (b) which cannot be determined with a high precision due to the extrapolation to a zero 10m wind speed from the wind data set which is truncated

at 8 or 9 ms^{-1} . For the Foreman and Emeis (2010) data set and the two data sets of Andreas et al. (2012), the 40m and asymptotic drag coefficients ($\times 10^3$) are the respective pairs: 2.20 and 2.60, 2.78 and 3.38, and 2.73 and 3.40.

5 Conclusion

Foreman and Emeis (2010) and Andreas et al. (2012) propose that the linear regression (11) can be applied to the observational data, which is interpreted as a modified drag law in which b/C_m is a reference velocity for aerodynamically rough flow governed by a constant drag coefficient (C_m^2). The theoretical model shows how the complex interactions which occur in the wave boundary layer give rise to a drag law which can be approximately represented over the range of wind speeds from $3 - 60 \text{ ms}^{-1}$ by a linear regression of similar form to (11). This result lends strong support to the physical interactions used in the theoretical model as being realistic, however as pointed out in Section 4 the fitting of the linear regression to the observations over a restrictive intermediate range of u_{10} gives rise to uncertainty in the intercept (b) at zero u_{10} , and also importantly may miss a maximum in K_{10} at high u_{10} , which is important with regard to a main aim of the air-sea boundary layer studies which is to specify the momentum transfer which affects the generation of tropical cyclones and also the mixing below the wave boundary layer which occurs in these extreme events. In summary, the theoretical model, which takes account of the interaction of the three physical processes governing the momentum exchange at the sea surface (Section 2), gives rise to a 10m drag law which is almost independent of wave age and is also in agreement with a wide variety of observational data sets.

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Appendix

The derivation of the 10m drag law

A convenient analytical procedure is to express the various relations in terms of the non-dimensional parameter $X = 1/(au_{*m})$. On substituting X in (3) using (6) we obtain the frictional parameter,

$$R = \frac{2\sqrt{K_I}}{\kappa} \cdot \frac{X(X-1)}{X-s} \quad (A1)$$

in which K_I is the inertial drag coefficient, κ is von Kármán's constant and $s = u_*/u_{*m}$, and where from (5) evaluated at K_{10m} using (6),

$$X = \frac{1}{2} \left[\ln \frac{c_{0m}^2}{2gz_{10}} + \frac{\kappa}{\sqrt{K_{10m}}} \right] \quad (A2)$$

in which g is the acceleration of gravity and $z_{10} = 10m$. Similarly, using (2) and (A1), we obtain,

$$c_0 = \frac{(X-1)s}{(X-s)} c_{0m} \quad (A3)$$

and the wave generation parameter,

$$B = \frac{1}{2} \frac{\kappa c_{0m}}{Xu_{*m}} \quad (A4)$$

On substituting for R and B in (5) and using (A2) to eliminate c_{0m} , we obtain the following relation for the inverse drag law, $u_{10}(u_*)$, in terms of X ,

$$u_{10} = \frac{2u_*}{\kappa} \left\{ \frac{X(s-1)}{(X-s)} - \ln \left[\frac{(X-1)s}{(X-s)} \right] \right\} + su_{10m} \quad (A5)$$

from which the 10m drag law (5) is determined. X can be evaluated from (A2) provided that K_{10m} , and c_{0m} which depends on sea state, are known. Direct observations of c_{0m} (or T_m) however are not generally available. It is therefore necessary to use field data at $u_{10} < u_{10m}$ to infer X , as is shown below.

On substituting (A3) in (A2) we obtain,

$$X = X' + \ln \left[\frac{X-s}{X-1} \right] \quad (A6)$$

where $X' = 1/2 [\ln c_0^2/2gs^2z_{10} + \kappa/\sqrt{K_{10m}}]$, and since $X \gg 1$, on using the binomial expansion (A6) yields approximately,

$$X = X' + \frac{1-s}{X'} \quad (A7)$$

Hence X may be evaluated in terms of s , c_0 and K_{10m} by substituting c_0 in X' .

The Charnock constant can also be evaluated in terms of X and compared with observations. From the defining relation for the sea surface roughness (z_0) we have $\ln z_{10}/z_0 = \kappa/\sqrt{K_{10}}$ and hence from (9),

$$\alpha = \frac{g}{u_*^2} z_{10} \exp \left[\frac{-\kappa}{\sqrt{K_{10}}} \right] \quad (A8)$$

which on eliminating K_{10} using (5) yields,

$$\alpha = \frac{1}{2} W^2 \exp \left[\frac{-R\kappa}{\sqrt{K_I}} \right] \quad (A9)$$

where $W = c_0/u_*$ is the wave age (Bye et al. 2010). On substituting for R from (A1), and for W from (A3) which yields,

$$W = W_m \frac{(X-1)}{(X-s)} \quad (A10)$$

where $W_m = c_{0m}/u_{*m}$ is the wave age at the drag coefficient maximum, we obtain,

$$\alpha = \frac{1}{2} W_m^2 \left[\frac{X-1}{X-s} \right]^2 \exp \left[-2X \frac{(X-1)}{(X-s)} \right] \quad (A11)$$

in which, from (A2),

$$W_m^2 = \frac{2gz_0}{u_*^2} \exp \left[2X - \frac{\kappa}{\sqrt{K_{10m}}} \right]. \quad (A12)$$

Finally, on substituting (A12) in (A11) we have the expression for the Charnock constant,

$$\alpha = \left[\frac{X-1}{X-s} \right]^2 \frac{gz_{10}}{u_{*m}^2} \exp \left[2 \frac{X(1-s)}{(X-s)} \right] \exp \left[\frac{-\kappa}{\sqrt{K_{10m}}} \right] \quad (A13)$$

We note that (A13), which is independent of c_{0m} , indicates that the choice of K_{10m} , rather than u_{*m} or c_{0m} , is highly significant in the evaluation of α . In terms of X , the spray parameter,

$$a = \frac{1}{Xu_{*m}} \quad (A14)$$

These expressions will be evaluated using the observed estimates at the maximum drag coefficient of $K_{10m} = 0.002$ and $u_{10m} = 40 \text{ ms}^{-1}$ ($u_{*m} = 1.79 \text{ ms}^{-1}$), and also $\kappa = 0.4$, $g = 9.8 \text{ ms}^{-2}$ and $K_I = 0.0015$, and at the onset of wave growth ($s = 0.05$) yield from (A5) $u_{10} = 3.0 \text{ ms}^{-1}$, and, $\alpha = 0.018$ in agreement with observations for the fully developed sea (Section 3.2). Note that all these expressions, except for (A1) and (A9) which involve R , are independent of K_I .

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