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Measurement of the $\bar{B} \rightarrow X_s \gamma$ Branching Fraction with a Sum of Exclusive Decays

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We use 772×10^6 $B\bar{B}$ meson pairs collected at the $\Upsilon(4S)$ resonance with the Belle detector to measure the branching fraction for $\bar{B} \rightarrow X_s \gamma$. Our measurement uses a sum-of-exclusives approach in which 38 of the hadronic final states with strangeness equal to +1, denoted by X_s , are reconstructed. The inclusive branching fraction for $M_{X_s} < 2.8 \text{ GeV}/c^2$, which corresponds to a minimum photon energy of 1.9 GeV, is measured to be $\mathcal{B}(\bar{B} \rightarrow X_s \gamma) = (3.51 \pm 0.17 \pm 0.33) \times 10^{-4}$, where the first uncertainty is statistical and the second is systematic.

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INTRODUCTION

The $b \rightarrow s\gamma$ transition is a flavor-changing neutral current process forbidden at tree level in the Standard Model

(SM). It proceeds at low rate through radiative penguin loop diagrams. Since the loop diagram is the only contribution, effects of new particles within the loop predicted by many new physics models (NP) can be investigated

by a precise measurement of the branching fraction [1–3]. The inclusive branching fraction of the $b \rightarrow s\gamma$ transition is sensitive to NP as it is theoretically well described in the SM. The SM calculation for the branching fraction has been performed at next-to-next-to-leading order in the perturbative expansion; for a photon energy above 1.6 GeV in the B meson rest frame, the calculations predict a branching fraction of $\mathcal{B}(\overline{B} \rightarrow X_s\gamma) = (3.15 \pm 0.23) \times 10^{-4}$ [1] or $(2.98 \pm 0.26) \times 10^{-4}$ [4], where \overline{B} is either \overline{B}^0 or B^- and X_s denotes all the hadron combinations that carry strangeness of +1. Charge conjugation is implied throughout this article. The dominant uncertainty of the expectation comes from the non-perturbative corrections. The increase in background with decreasing photon energy limits the ability to make measurements below a minimum photon energy. The measured branching fraction is extrapolated to a photon energy threshold of 1.6 GeV to compare with the theoretical expectation. The current measured world average is $\mathcal{B}(\overline{B} \rightarrow X_s\gamma) = (3.40 \pm 0.21) \times 10^{-4}$ [5]. This value is consistent with the SM prediction within the uncertainties.

We report a measurement of the branching fraction of $\overline{B} \rightarrow X_s\gamma$ with a 711 fb^{-1} data set collected at the $\Upsilon(4S)$ resonance containing 772×10^6 $B\overline{B}$ meson pairs recorded by the Belle detector [6] at the KEKB asymmetric-energy e^+e^- collider (3.5 GeV e^+ and 8.0 GeV e^-) [7]. Our measurement uses a sum-of-exclusives approach whereby we measure as many exclusive final states of the s -quark hadronic system, X_s , as possible and then calculate the combined branching fraction. Exclusive branching fractions measured to date do not saturate the inclusive process, but one can still infer the total branching fraction by estimating the proportion of unmeasured modes using simulated fragmentation processes.

In this article, we present a measurement that supersedes an earlier Belle analysis [8], which was limited to only 5.8 fb^{-1} . We also use an improved analysis procedure here.

DETECTOR

The Belle detector is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector (SVD), a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter comprised of CsI(Tl) crystals (ECL) located inside a super-conducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside of the coil is instrumented to detect K_L^0 mesons and to identify muons (KLM). The detector is described in detail elsewhere [6]. The origin of the coordinate system is defined as the position of the nominal interaction point (IP). The z axis is aligned with

the direction opposite the e^+ beam and is parallel to the direction of the magnetic field within the solenoid. The x axis is horizontal and points towards the outside of the storage ring; the y axis is vertical upward. The polar angle θ and azimuthal angle ϕ are measured relative to the positive z and x axes, respectively.

SIMULATION SAMPLE

We use Monte Carlo (MC) simulations to model signal and background events and to optimize the selection criteria prior to examining the signal region in the data.

We generate two types of signal MC samples, according to the X_s mass region: one in the $K^*(892)$ region ($M_{X_s} < 1.15 \text{ GeV}/c^2$), where the hadronic part corresponds to a K^* , and the other in the inclusive hadronic region ($M_{X_s} > 1.15 \text{ GeV}/c^2$). In the inclusive signal MC, various resonances and final states are simulated. The photon energy spectrum is produced following the Kagan-Neubert model [9] in the inclusive signal MC. This model has two parameters: the b quark mass (m_b) and the Fermi-motion parameter of the b quark inside the B meson (μ_π^2). The nominal values of these parameters are determined from a best fit to the Belle inclusive photon energy spectrum [10]: $m_b = 4.440 \text{ GeV}/c^2$ and $\mu_\pi^2 = 0.750 \text{ GeV}^2$. In the inclusive X_s mass region, the generated light quark pair is fragmented into final state hadrons in PYTHIA [11]. The signal reconstruction efficiency depends on the particle content in the final state; thus, it is important to determine the breakdown of the final state using data. We assume the branching fraction to be the current measured world average in order to optimize the background rejection.

We simulate the background using $q\overline{q}$ and $B\overline{B}$ MC samples where we generate $e^+e^- \rightarrow q\overline{q}$ ($q = u, d, s, c$) (“continuum”) and $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\overline{B}$, respectively. In the latter case, we assume equal production of charged and neutral B meson pairs.

B MESON RECONSTRUCTION AND BACKGROUND SUPPRESSION

We reconstruct the B candidate from a high energy photon and one of the 38 X_s final states listed in Table I.

A high-energy photon generates an electromagnetic shower in the ECL and is detected as an isolated energy cluster not associated with charged particles. We take the photon candidate with an energy in the center-of-mass (CM) frame between 1.8 and 3.4 GeV. The photon candidate is required to be within the acceptance of the barrel ECL, $33^\circ < \theta < 132^\circ$. It must satisfy $E_9/E_{25} \geq 0.95$, which is the ratio of energy deposition within the 3×3 cells to that in the 5×5 cells cen-

tered on the maximum-energy ECL cell of the cluster. To reject candidates that arise from π^0 and η decays, the photon candidate is paired with all other photons in the event with energy above 40 MeV. We reject the candidate based on a likelihood formed as a function of the invariant mass of the two-photon system and the laboratory energy of the partner photon (π^0/η -veto). Furthermore, photon candidates with a two-photon invariant mass between 117 and 153 MeV/ c^2 are rejected irrespective of the likelihood.

Charged particles must have a distance of closest approach to the IP within ± 5 cm along the z axis and 0.5 cm in the transverse plane, and a laboratory momentum above 0.1 GeV/ c . Flavor identification of K^\pm and π^\pm [12] is based on a likelihood formed with information from the specific ionization in the CDC, the flight time measured by the TOF, and the response of the ACC.

Candidate K_S^0 mesons are formed from $\pi^+\pi^-$ pairs by a multivariate analysis with a neural network technique [13]. The neural network uses the distance between two helices in the z direction, the flight length in the x - y plane, the angle between the K_S^0 momentum and the vector joining the K_S^0 decay vertex to the IP, the shorter distance in the x - y plane between the IP and two child helices, the angle between the pion momentum and the laboratory-frame direction in the K_S^0 rest frame, and the pion hit information in the SVD and CDC. The selection efficiency and purity, evaluated with the MC sample, are 87% and 94%, respectively, over the entire momentum

TABLE I. Reconstructed X_s final states, where charge conjugated modes are implicitly included. A $K_S(\eta)$ is reconstructed via $\pi^+\pi^-$ ($\gamma\gamma$) final state. Final states with $\pi^+\pi^-\pi^0$ implicitly include intermediate $\eta \rightarrow \pi^+\pi^-\pi^0$ decays (i.e., here the η is not reconstructed).

Mode ID	Final State	Mode ID	Final State
1	$K^+\pi^-$	20	$K_S^0\pi^+\pi^0\pi^0$
2	$K_S^0\pi^+$	21	$K^+\pi^+\pi^-\pi^0\pi^0$
3	$K^+\pi^0$	22	$K_S^0\pi^+\pi^-\pi^0\pi^0$
4	$K_S^0\pi^0$	23	$K^+\eta$
5	$K^+\pi^+\pi^-$	24	$K_S^0\eta$
6	$K_S^0\pi^+\pi^-$	25	$K^+\eta\pi^-$
7	$K^+\pi^-\pi^0$	26	$K_S^0\eta\pi^+$
8	$K_S^0\pi^+\pi^0$	27	$K^+\eta\pi^0$
9	$K^+\pi^+\pi^-\pi^-$	28	$K_S^0\eta\pi^0$
10	$K_S^0\pi^+\pi^+\pi^-$	29	$K^+\eta\pi^+\pi^-$
11	$K^+\pi^+\pi^-\pi^0$	30	$K_S^0\eta\pi^+\pi^-$
12	$K_S^0\pi^+\pi^-\pi^0$	31	$K^+\eta\pi^-\pi^0$
13	$K^+\pi^+\pi^+\pi^-\pi^-$	32	$K_S^0\eta\pi^+\pi^0$
14	$K_S^0\pi^+\pi^+\pi^-\pi^-$	33	$K^+K^+K^-$
15	$K^+\pi^+\pi^-\pi^-\pi^0$	34	$K^+K^-K_S^0$
16	$K_S^0\pi^+\pi^+\pi^-\pi^0$	35	$K^+K^+K^-\pi^-$
17	$K^+\pi^0\pi^0$	36	$K^+K^-K_S^0\pi^+$
18	$K_S^0\pi^0\pi^0$	37	$K^+K^+K^-\pi^0$
19	$K^+\pi^-\pi^0\pi^0$	38	$K^+K^-K_S^0\pi^0$

region. We also require that the di-pion invariant mass fall within 10 MeV/ c^2 of the nominal K_S^0 mass [5]. We do not include K_L^0 mesons nor $K_S^0 \rightarrow \pi^0\pi^0$ decays.

Candidate π^0 mesons are reconstructed from pairs of photons with energy greater than 50 MeV in the laboratory frame. We require a minimum π^0 momentum of 100 MeV/ c . The candidates must have an invariant mass between 125 and 145 MeV/ c^2 , corresponding to $\pm 1.5\sigma$ around the nominal π^0 mass, and the cosine of the angle in the laboratory frame between the two photons must be below 0.4.

Candidate η mesons are reconstructed from pairs of photons with energy greater than 100 MeV and an invariant mass between 515 and 570 MeV/ c^2 , corresponding to $\pm 2.0\sigma$ around the nominal η mass. We require the η momentum to be above 200 MeV/ c . The photons from η candidates must have a helicity angle (θ_{hel}) satisfying $\cos\theta_{\text{hel}} < 0.8$; θ_{hel} is defined as the angle between the photon momentum and laboratory-frame direction in the η rest frame. Although $\eta \rightarrow \pi^+\pi^-\pi^0$ decays are not explicitly reconstructed, they are included implicitly in the final states if the final state is included in Table I.

The “ $K4\pi$ ” modes ($K^+\pi^+\pi^+\pi^-\pi^-$, $K_S^0\pi^+\pi^+\pi^-\pi^-$, $K^+\pi^+\pi^-\pi^-\pi^0$ and $K_S^0\pi^+\pi^+\pi^-\pi^0$), corresponding to identification numbers (mode IDs) 13-16 in Table I, and “ $K2\pi^0$ ” modes ($K^+\pi^0\pi^0$, $K_S^0\pi^0\pi^0$, $K^+\pi^-\pi^0\pi^0$, $K_S^0\pi^+\pi^0\pi^0$, $K^+\pi^+\pi^-\pi^0\pi^0$, and $K_S^0\pi^+\pi^-\pi^0\pi^0$), corresponding to mode IDs 17-22, have substantial background. Therefore, the momentum of the leading π in the $K4\pi$ mode and the leading π^0 in the $K2\pi^0$ mode is required to be above 400 MeV/ c , and the momentum of the subleading π is required to be above 250 MeV/ c .

We do not include $\omega \rightarrow \pi^0\gamma$ modes ($K\omega$, $K\omega\pi$, $K\omega 2\pi$) nor $\eta' \rightarrow \rho^0\gamma$ modes ($K\eta'$, $K\eta'\pi$, $K\eta'2\pi$) as the yields are too small to make useful measurements. The 38 measured final states cover 56% of the total X_s rate, according to the MC simulation. Assuming the K^0 meson decays equally into K_L^0 and K_S^0 , the proportion of our measured final states is 74%.

We combine the photon candidate and the X_s candidate to form the B candidate. The latter is selected using two kinematic variables defined in the $\Upsilon(4S)$ rest frame: the beam-energy-constrained mass, $M_{\text{bc}} = \sqrt{(E_{\text{beam}}/c^2)^2 - |\vec{p}_B/c|^2}$, and the energy difference, $\Delta E = E_B - E_{\text{beam}}$, where E_{beam} is the beam energy and (E_B, \vec{p}_B) is the reconstructed four-momentum of the B candidate. The B momentum vector \vec{p}_B is calculated without using the magnitude of the photon momentum according to $\vec{p}_B = \vec{p}_{X_s} + \vec{p}_\gamma/|\vec{p}_\gamma| \times (E_{\text{beam}} - E_{X_s})$, since the X_s momentum and the beam energy are determined with substantially better precision than that of the photon candidate. We require $M_{\text{bc}} > 5.24$ GeV/ c^2 and -0.15 GeV $< \Delta E < 0.08$ GeV; the ΔE selection is tightened to -0.10 GeV $< \Delta E < 0.05$ GeV for the final states with $2\pi^0$ and $\eta\pi^0$ (mode IDs of 17-22, 27-28 and 31-32) due to the larger background.

A large background still remains after signal reconstruction, dominated by three categories. The first is from events with D meson decay, especially $B \rightarrow D^{(*)}\rho^+$. These give rise to a peak in the signal region of M_{bc} . In order to suppress such background, a D veto is applied for candidates with $M_{X_s} > 2.0 \text{ GeV}/c^2$. D meson candidates of the major decay modes are reconstructed with combinations of particles used in the X_s reconstruction. The event is rejected if any of the D meson candidates falls in a veto window around the D mass. We set the central value and the width of the veto window depending on the charge of the D candidate and whether or not the D candidate is reconstructed in a mode with a π^0 or η meson. Consequently, 90 % (23%) of the signal (background) is kept.

The second and dominant category is continuum. We reduce this background by applying a selection criterion based on the event shape. We perform a multivariate analysis with a neural network [13] that uses the following input variables: (1) the likelihood ratio of modified Fox-Wolfram moments [14, 15], (2) the cosine of the angle between the B candidate and the z axis, (3) the angle between the thrust axis of the B candidate's decay particles and that of the remaining particles in the event, (4) the thrust calculated with the remaining particles in the event, (5) the sphericity, (6) the aplanarity, (7) the flavor dilution factor of the accompanying B meson that ranges from zero for no flavor information to unity for unambiguous flavor assignment [16] and (8) the signal probability density for the ΔE value. Variables (1)-(6) are calculated in the $\Upsilon(4S)$ rest frame. The neural network is trained with signal and $q\bar{q}$ -background MC events with $2.2 \text{ GeV}/c^2 < M_{X_s} < 2.8 \text{ GeV}/c^2$. The neural network output classifier (NN classifier) is also optimized in this region since the measurement here is difficult and incurs a large systematic uncertainty, while the signal in the low M_{X_s} region is observed relatively easily. We obtain a NN classifier between -1 and $+1$, shown in Fig.1, which achieves good separation between the signal and the $q\bar{q}$ background. The acceptance criterion of the NN classifier is optimized at 0.78 by the significance in $2.2 \text{ GeV}/c^2 < M_{X_s} < 2.8 \text{ GeV}/c^2$. After requiring that the NN classifier exceed this value, 52 % (2 %) of the signal ($q\bar{q}$ background) is retained in the MC.

The third major category of background is ‘‘cross-feed’’ from $\bar{B} \rightarrow X_s\gamma$ events that have been incorrectly reconstructed. On average, there are approximately two B meson candidates in a given event after the $q\bar{q}$ background suppression, since 38 final states are reconstructed concurrently. To suppress cross-feed background, the B candidate with the largest NN classifier for the $q\bar{q}$ background suppression is selected (Best Candidate Selection or BCS); the efficiency is 85 % and the purity (defined as the ratio of number of signal to number of signal plus cross-feed after the BCS) is 68 %, evaluated with MC.

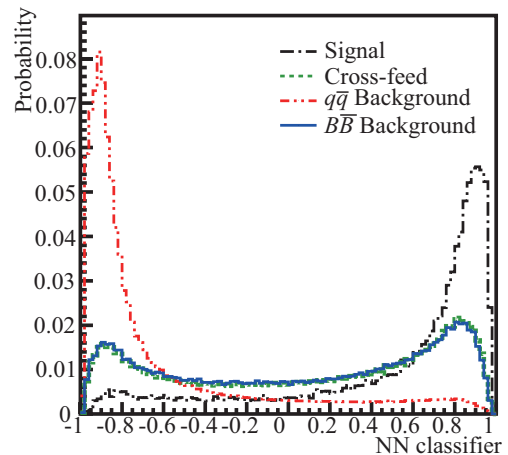


FIG. 1. Neural Network output classifier (NN classifier) that ranges from -1 for the $q\bar{q}$ background-like events to $+1$ for the signal-like events (MC). The signal (one dot-dashed line), the cross-feed (dashed line), the $q\bar{q}$ background (two dot-dashed line) and the $B\bar{B}$ background (solid line) are shown. We select events with the NN classifier above 0.78.

SIGNAL YIELD EXTRACTION

To extract the signal yield, a fit is performed in the M_{bc} distribution with an unbinned maximum likelihood method. The likelihood function consists of PDFs for signal, cross-feed, peaking and non-peaking background from $B\bar{B}$ events, and $q\bar{q}$ background. The signal is modeled by a Crystal Ball function (CB) [17]:

$$f_{\text{CB}}(x) = \begin{cases} \exp\left(-\frac{1}{2}\left(\frac{x-m}{\sigma}\right)^2\right) & \left(\frac{x-m}{\sigma} > -\alpha\right) \\ \left(\frac{n}{\alpha}\right)^n \exp\left(-\frac{1}{2}\alpha^2\right) & \left(\frac{x-m}{\sigma} < -\alpha\right), \end{cases} \quad (1)$$

where m and σ are the peak position and width, respectively, and the parameters α and n characterize the non-Gaussian tail. These parameters are fixed to the values obtained from the large-statistics $B \rightarrow D\pi$ data sample, but a small correction to the tail parameters is applied by using the signal MC. For the cross-feed background, we construct a histogram PDF from the signal MC. The fraction of the cross-feed to the signal is fixed to the value obtained from the MC. A Gaussian function is adopted to model the peaking background. The shape parameters and yield are fixed to the values obtained from data within the π^0/η -veto window. The non-peaking background from $B\bar{B}$ events is modeled by an ARGUS function [18]:

$$f_{\text{ARG}}(x) = x \left\{ 1 - \left(\frac{x}{E_{\text{beam}}^*} \right)^2 \right\}^p \cdot \exp \left[c \left\{ 1 - \left(\frac{x}{E_{\text{beam}}^*} \right)^2 \right\} \right], \quad (2)$$

where the endpoint is fixed to the beam energy E_{beam}^* in the CM frame and other shape parameters and yield are allowed to float. For the $q\bar{q}$ background PDF, we use a

modified ARGUS function:

$$f_{\text{ARG}}^{\text{mod}}(x) = x \left\{ 1 - \left(\frac{x}{E_{\text{beam}}^*} \right)^q \right\}^p \cdot \exp \left[c \left\{ 1 - \left(\frac{x}{E_{\text{beam}}^*} \right)^2 \right\} \right], \quad (3)$$

where a new power term, q , is introduced to account for the steep slope at low M_{bc} . The shape and yield are determined via a fit to 90 fb^{-1} of off-resonance data collected at about 60 MeV below the $\Upsilon(4S)$ resonance energy; the yield is scaled according to the luminosity. There are in total four free parameters in the fit for the signal extraction: the signal yield and the yield and shape parameters (p and c) of the non-peaking background from $B\bar{B}$ events. We perform an ensemble test on toy MC to ensure no bias in the fitting procedure and verify with a full MC sample. The signal yields are extracted in each M_{X_s} bin.

CALIBRATION OF X_s FRAGMENTATION MODEL

Since the signal efficiency depends on the specific decay modes, the fragmentation model in the inclusive MC is calibrated to that of the data to reduce associated modeling systematic uncertainties. The final states are divided into ten categories, defined in Table II [19], to calibrate the MC selection efficiencies to those of data. In Table III, we compare the expected relative proportion of each category in data and MC. We find that the MC overestimates the fraction of the low multiplicity final-state $K\pi$ by more than a factor of two (i.e., mode categories 1 and 2). In order to calibrate the proportions in the MC, we vary four relevant parameters in the nominal PYTHIA fragmentation model: the suppression factor of s -quark pair production compared with u - or d -quark pair production (PARJ(2)), the probabilities for forming a spin-1 meson (PARJ(11), PARJ(15)), and an extra suppression factor for η production in fragmentation (PARJ(25)). The proportions in the calibrated MC are given in the rightmost column of Table III. The total χ^2 is improved from 826 to 47 using this calibration technique over the 10 degrees of freedom corresponding to the 10 decay mode categories. There are several decay-mode categories whose proportions in the MC deviate significantly from those in data, especially in category 5 ($K3\pi$ without π^0). We investigated the fragmentation proportions in four M_{X_s} regions (1.15 - 1.5 , 1.5 - 2.0 , 2.0 - 2.4 and 2.4 - $2.8 \text{ GeV}/c^2$) in the data and the calibrated MC shown in Table IV. However, several mode categories in the calibrated MC have large deviations from those in the data. We find that the fine-tuning of the PYTHIA fragmentation is insufficient to accurately describe the data and, therefore, we calibrate directly using the ratio of the proportion for each mode category in data to that in the MC in the four mass regions shown in Table V. The uncertainty on the ratio

TABLE II. Mode category definitions for X_s fragmentation check.

Mode Category	Definition	Mode ID
1	$K\pi$ without π^0	1,2
2	$K\pi$ with π^0	3,4
3	$K2\pi$ without π^0	5,6
4	$K2\pi$ with π^0	7,8
5	$K3\pi$ without π^0	9,10
6	$K3\pi$ with π^0	11,12
7	$K4\pi$	13-16
8	$K2\pi^0$	17-22
9	$K\eta$	23-32
10	$3K$	33-38

TABLE III. The relative proportion (%) of each mode in the range of $1.15 \text{ GeV}/c^2 < M_{X_s} < 2.8 \text{ GeV}/c^2$ in the data, default MC and calibrated MC. Numbers in parentheses are deviation significances, defined as $([\text{Proportion in MC}] - [\text{Proportion in data}]) / \sigma_{\text{data}}$. The uncertainties in the MC proportions are much smaller than those for the data proportions and can be neglected.

Mode Category	Data	Default MC	Calibrated MC
1	4.2 ± 0.4	10.3 (+17)	4.6 (+1.2)
2	2.1 ± 0.2	5.4 (+19)	2.4 (+1.6)
3	14.5 ± 0.5	12.9 (-3.1)	15.7 (+2.4)
4	24.0 ± 0.7	15.2 (-12)	24.0 (-0.0)
5	8.3 ± 0.8	5.9 (-3.3)	4.6 (-5.0)
6	16.1 ± 1.8	15.7 (-0.2)	19.2 (+1.8)
7	11.1 ± 2.8	12.3 (+0.4)	10.2 (-0.3)
8	14.4 ± 3.5	14.4 (-0.0)	11.6 (-0.8)
9	3.2 ± 0.8	4.9 (+2.3)	5.4 (+2.8)
10	2.0 ± 0.3	3.0 (+3.3)	2.3 (+1.0)

is the statistical uncertainty in fitting each mode category in data. Measurements of the $K2\pi^0$ signals (mode category 8) with $2.0 \text{ GeV}/c^2 < M_{X_s} < 2.8 \text{ GeV}/c^2$ are difficult. Thus, the calibration by the factors in Table V is not applied to mode category 8 in the range $2.0 \text{ GeV}/c^2 < M_{X_s} < 2.8 \text{ GeV}/c^2$. The signal efficiencies in each M_{X_s} bin before and after the calibration are reported in Table VI.

SYSTEMATIC UNCERTAINTIES

The uncertainty on the total number of B mesons in our data sample is 1.4%.

The differences of the detector response between data and MC associated with photon detection, tracking of charged particles, K_S^0 , π^0 and η reconstruction, and K^\pm/π^\pm identification are evaluated; the efficiencies are corrected by these values and the errors are taken as the systematic uncertainties on a bin-by-bin basis, as shown

TABLE IV. Relative proportions (%) for each mode in each M_{X_s} region in the data and calibrated MC. Numbers in parentheses are deviation significances, defined as $([\text{Proportion in MC}] - [\text{Proportion in data}]) / \sigma_{\text{data}}$.

$1.15 < M_{X_s} < 1.5 \text{ (GeV}/c^2)$			$1.5 < M_{X_s} < 2.0 \text{ (GeV}/c^2)$		
Mode	Data	MC	Data	MC	
1	10.7±0.6	14.6 (+6.4)	2.4±0.4	2.9 (+1.5)	
2	5.3±0.3	7.5 (+7.1)	1.2±0.2	1.5 (+1.7)	
3	25.7±0.8	21.6 (-5.0)	13.6±0.8	15.0 (+1.9)	
4	44.8±1.5	36.5 (-5.5)	19.7±1.1	22.0 (+2.2)	
5	0.9±0.5	1.0 (+0.1)	11.3±0.9	6.6 (-5.0)	
6	8.1±2.2	14.9 (+3.1)	21.7±2.4	23.7 (+0.9)	
7	0.3±0.5	0.5 (+0.5)	8.8±2.7	8.4 (-0.2)	
8	2.5±2.5	2.5 (+0.0)	14.7±2.1	12.2 (-1.2)	
9	1.7±0.4	0.9 (-1.8)	5.0±1.3	5.8 (+0.6)	
10	0.0±0.0	0.1 (+0.0)	1.6±0.2	1.3 (-1.5)	
$2.0 < M_{X_s} < 2.4 \text{ (GeV}/c^2)$			$2.4 < M_{X_s} < 2.8 \text{ (GeV}/c^2)$		
Mode	Data	MC	Data	MC	
1	1.2±0.6	1.2 (-0.1)	0.5±0.7	0.9 (+0.7)	
2	0.6±0.3	0.6 (+0.0)	0.2±0.3	0.5 (+0.8)	
3	7.1±1.4	9.6 (+1.9)	3.8±2.2	8.2 (+2.0)	
4	8.9±2.6	13.9 (+1.9)	8.5±4.0	11.8 (+0.8)	
5	12.1±2.5	8.3 (-1.5)	12.7±5.2	8.2 (-0.9)	
6	16.1±5.7	22.6 (+1.1)	3.3±12.8	21.2 (+1.4)	
7	28.0±9.1	16.5 (-1.3)	3.1±26.7	20.4 (+0.7)	
8	15.5±15.5	18.5 (+0.2)	53.1±28.7	20.2 (-1.2)	
9	6.8±3.7	6.2 (-0.2)	10.6±8.2	5.9 (-0.6)	
10	3.6±1.1	1.4 (-2.0)	4.1±2.8	1.0 (-1.1)	

TABLE V. Calibration factors of each mode category in each M_{X_s} region, which are ratios of the proportion in data to that in MC.

Mode	M_{X_s} region (GeV/ c^2)				
	Category	1.15-1.5	1.5-2.0	2.0-2.4	2.4-2.8
1		0.66±0.10	0.82±0.12	1.05±0.56	0.51±0.72
2		0.71±0.04	0.80±0.12	1.00±0.53	0.47±0.65
3		1.19±0.04	0.91±0.05	0.73±0.14	0.47±0.26
4		1.23±0.04	0.90±0.05	0.64±0.19	0.72±0.34
5		0.96±0.55	1.72±0.14	1.45±0.30	1.55±0.64
6		0.54±0.15	0.92±0.10	0.71±0.25	0.15±0.60
7		0.58±0.96	0.72±0.22	1.70±0.55	0.15±1.30
8		1.00±1.00	1.79±0.25	0.84±0.84	2.63±1.42
9		1.84±0.46	0.87±0.22	1.11±0.60	1.80±1.39
10		0.00±0.00	1.27±0.19	2.54±0.77	3.97±2.73

in Table VII.

The D -veto uncertainty is evaluated by using a control sample of $B \rightarrow X_s J/\psi$ decays followed by $J/\psi \rightarrow \ell^+ \ell^-$ ($\ell = e, \mu$). To mimic the conditions of a $\bar{B} \rightarrow X_s \gamma$ decay, one of the leptons from the J/ψ is combined with the X_s candidate to ensure that the X_s mass lies within the D -veto region. This lepton is chosen such that the electric charge of X_s is $-1, 0$ or 1 after the

TABLE VI. The reconstruction efficiencies before and after the X_s fragmentation calibration.

M_{X_s} bin (GeV/ c^2)	Efficiency (%) before calibration	Efficiency (%) after calibration
0.6-0.7	7.0	7.0
0.7-0.8	7.2	7.2
0.8-0.9	6.7	6.7
0.9-1.0	7.0	7.0
1.0-1.1	6.7	6.7
1.1-1.2	4.3	4.2
1.2-1.3	4.0	3.5
1.3-1.4	3.7	3.3
1.4-1.5	3.6	3.3
1.5-1.6	2.7	2.4
1.6-1.7	2.3	2.1
1.7-1.8	2.0	1.7
1.8-1.9	1.7	1.6
1.9-2.0	1.4	1.3
2.0-2.1	1.2	1.1
2.1-2.2	0.9	0.9
2.2-2.4	0.8	0.7
2.4-2.6	0.5	0.6
2.6-2.8	0.4	0.5

lepton is added; if the original X_s is neutral, the lower-energy lepton is chosen. The invariant-mass distribution of the D meson candidate in the $X_s J/\psi$ control sample has a broad peak at the nominal D mass region for $M_{X_s} > 2.0 \text{ GeV}/c^2$, just as in the signal sample. The difference in the D -veto efficiency between the MC and data is evaluated by this control sample.

The uncertainty due to the $q\bar{q}$ background suppression is evaluated using a control sample of $B \rightarrow D\pi$ decays, which provides sufficient statistical power ($\sim 2 \times 10^5$ events). In the reconstruction of $B \rightarrow D\pi$, the prompt pion from the B meson is treated as the photon candidate of the signal. The neural network is trained and optimized using the same methods as in the signal analysis. We take the difference in the efficiency between the data and MC as the systematic uncertainty.

The uncertainty due to the BCS is evaluated by again using a control sample of $B \rightarrow X_s J/\psi$ ($J/\psi \rightarrow \ell^+ \ell^-$, $\ell = e, \mu$) decays. The reconstruction procedure is the same as that in the D -veto uncertainty study. We assign the efficiency discrepancy between the MC and data as the systematic uncertainty. The uncertainties of the D -veto, $q\bar{q}$ background suppression and BCS are summed quadratically and given as ‘‘Background rejection’’ in Table VII.

In order to evaluate the uncertainty due to the signal PDF, we use the variation in the signal yield after changing the parameter values by one standard deviation (1σ) around the central value of the fit. To evaluate the uncertainty from the cross-feed histogram PDF, we perform two sets of 1σ systematic variations: on the

bin-by-bin content in the PDF and on the ratio of the cross-feed yield to the signal yield. The variation on the signal yield is taken as the systematic uncertainty. To evaluate the uncertainty due to the peaking background PDF, we vary the parameter values by 1σ and repeat the fits to data. To evaluate the uncertainty due to the $q\bar{q}$ background PDF, we use the variation in the signal yield when varying the parameter values by 1σ in the fits to the off-resonance data. The uncertainties due to the M_{bc} PDF are reported in Table VII.

The uncertainty due to the fragmentation model is determined by varying the decay channel proportions given in Table IV by their respective uncertainties. The exception is for the proportion of $K2\pi^0$ (mode category 8) in $2.0\text{ GeV}/c^2 < M_{X_s} < 2.8\text{ GeV}/c^2$, where we use the proportions in MC and a variation of $^{+100\%}_{-50\%}$ as the uncertainty. The fragmentation uncertainties for each M_{X_s} bin are obtained by summing in quadrature the changes for each of the ten mode categories. Since the threshold between K^* and the inclusive X_s used in the MC modeling is fixed at $1.15\text{ GeV}/c^2$, we change this boundary to $1.10\text{ GeV}/c^2$ and $1.20\text{ GeV}/c^2$ to evaluate the uncertainty due to the threshold. These uncertainties are included in the fragmentation uncertainty.

The proportion of missing final states that are not included in our reconstructed modes affects the reconstruction efficiency. The uncertainty on the relative proportion of each of the 38 measured final states is evaluated by varying the parameters of the fragmentation model used in the calibration of the MC within their allowed ranges as determined from data. We take the difference from the nominal value as the systematic uncertainty on the missing proportion, as given in Table VII.

The following uncertainties are considered correlated across M_{X_s} bins: the $B\bar{B}$ -counting, detector-response and background-rejection uncertainties. We take the uncertainties on all M_{bc} PDFs except for the cross-feed to be uncorrelated across all mass bins, and the uncertainty on the cross-feed PDF is considered completely correlated. The total uncertainties due to the fragmentation and missing proportion factors are evaluated in four different M_{X_s} mass regions ($1.15\text{-}1.5$, $1.5\text{-}2.0$, $2.0\text{-}2.4$, $2.4\text{-}2.8\text{ GeV}/c^2$). The uncertainties across these mass regions are considered to be uncorrelated, but the uncertainties across the mass bins within a given mass region are considered to be correlated.

BRANCHING FRACTIONS

The signal yields are obtained in $100\text{ MeV}/c^2$ -wide bins in the low mass region, $0.6\text{ GeV}/c^2 < M_{X_s} < 2.2\text{ GeV}/c^2$, and $200\text{ MeV}/c^2$ -wide bins in the high mass region, $2.2\text{ GeV}/c^2 < M_{X_s} < 2.8\text{ GeV}/c^2$. The binned approach minimizes the sensitivity to modeling of the X_s mass distribution. In Table VIII, the signal yields in each mass

bin are reported from the fit to data. Figures 2, 3 and 4 show the M_{bc} distribution fits in each M_{X_s} bin. The partial branching fraction for each bin is defined as

$$\mathcal{B}_i = N_i / (N_{B\bar{B}} \times \epsilon_i), \quad (4)$$

where N_i and ϵ_i are the signal yield and the efficiency, respectively, in bin i and $N_{B\bar{B}}$ is the sum of number of \bar{B}^0 and B^- events. The results are listed in Table VIII and plotted in Fig. 5. Both statistical and systematic uncertainties in M_{X_s} above $2.2\text{ GeV}/c^2$ are large. We also report the total branching fraction for $M_{X_s} < 2.8\text{ GeV}/c^2$,

$$\mathcal{B}(\bar{B} \rightarrow X_s \gamma) = (3.51 \pm 0.17 \pm 0.33) \times 10^{-4}, \quad (5)$$

where the first uncertainty is statistical and the second is systematic. This branching fraction is the sum of 19 bins, with a 1.9 GeV lower threshold on the photon energy. The total statistical uncertainty is based on the quadratic sum of the statistical uncertainty in each X_s mass bin.

CONCLUSION

We measure the branching fraction of $\bar{B} \rightarrow X_s \gamma$ with the sum-of-exclusives approach using the entire $\Upsilon(4S)$ data set of the Belle experiment. The branching fraction in the region $M_{X_s} < 2.8\text{ GeV}/c^2$ (corresponding to a minimum photon energy of 1.9 GeV) is measured to be $\mathcal{B}(\bar{B} \rightarrow X_s \gamma) = (3.51 \pm 0.17 \pm 0.33) \times 10^{-4}$, where the first uncertainty is statistical and the second is systematic. This result is consistent with the measurement at BABAR [19] and achieves the best precision of any sum-of-exclusives approach. This measurement supersedes our previous result [8].

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TABLE VII. Systematic uncertainties (%) in each M_{X_s} mass bin.

M_{X_s} bin (GeV/ c^2)	$B\bar{B}$ counting	Detector response	Background rejection	Signal PDF	Cross-feed PDF	Peaking BG PDF	$q\bar{q}$ PDF	BG	Frag.	Missing proportion	Total
0.6-0.7	1.4	2.7	3.4	0.0	0.0	0.0	0.0	-	-	-	4.5
0.7-0.8	1.4	2.6	3.4	0.1	12.2	7.8	0.0	-	-	-	15.3
0.8-0.9	1.4	2.6	3.4	0.2	0.4	0.5	0.0	-	-	-	4.5
0.9-1.0	1.4	2.6	3.4	0.1	0.5	0.4	0.0	-	-	-	4.5
1.0-1.1	1.4	2.6	3.4	0.1	2.9	1.1	0.3	-	-	-	5.4
1.1-1.2	1.4	3.0	3.4	0.4	3.1	1.7	0.2	32.1	1.2	32.1	
1.2-1.3	1.4	3.2	3.4	0.2	1.6	0.9	0.0	2.1	1.0	5.6	
1.3-1.4	1.4	3.2	3.4	0.2	1.6	0.2	0.0	2.6	1.9	6.0	
1.4-1.5	1.4	3.1	3.4	0.2	2.0	0.1	0.0	4.0	1.3	6.7	
1.5-1.6	1.4	3.3	3.4	0.6	2.2	0.1	0.0	2.4	1.3	6.1	
1.6-1.7	1.4	3.5	3.4	0.1	1.7	2.1	0.2	2.8	1.9	6.7	
1.7-1.8	1.4	3.6	3.4	0.1	2.2	1.7	0.2	3.4	1.0	6.8	
1.8-1.9	1.4	3.7	3.4	0.1	1.9	2.0	0.1	3.6	2.1	7.2	
1.9-2.0	1.4	3.7	3.4	0.1	4.2	4.0	0.1	3.7	1.6	8.8	
2.0-2.1	1.4	3.8	3.4	0.1	5.6	0.6	0.2	17.8	2.2	19.5	
2.1-2.2	1.4	3.8	3.4	0.3	3.7	2.5	0.4	21.9	1.9	23.1	
2.2-2.4	1.4	3.8	3.4	0.1	7.4	7.1	0.0	25.5	1.6	28.0	
2.4-2.6	1.4	3.8	3.4	0.1	11.5	21.8	0.3	29.6	1.0	38.9	
2.6-2.8	1.4	3.8	3.4	0.1	44.7	101.0	0.9	29.4	2.0	113.9	

TABLE VIII. The yields and partial branching fraction in each M_{X_s} mass bin.

M_{X_s} bin (GeV/ c^2)	Yield	$\mathcal{B}(10^{-6})$
0.6-0.7	-6 ± 10	$-0.1 \pm 0.1 \pm 0.0$
0.7-0.8	36 ± 14	$0.3 \pm 0.1 \pm 0.1$
0.8-0.9	2032 ± 54	$19.8 \pm 0.5 \pm 0.9$
0.9-1.0	1689 ± 49	$15.7 \pm 0.5 \pm 0.7$
1.0-1.1	301 ± 27	$2.9 \pm 0.3 \pm 0.2$
1.1-1.2	310 ± 31	$4.8 \pm 0.5 \pm 1.5$
1.2-1.3	1019 ± 46	$18.7 \pm 0.8 \pm 1.1$
1.3-1.4	1117 ± 50	$21.8 \pm 1.0 \pm 1.3$
1.4-1.5	1090 ± 52	$21.2 \pm 1.0 \pm 1.4$
1.5-1.6	806 ± 50	$22.0 \pm 1.4 \pm 1.3$
1.6-1.7	723 ± 37	$22.4 \pm 1.1 \pm 1.5$
1.7-1.8	664 ± 37	$24.8 \pm 1.4 \pm 1.7$
1.8-1.9	652 ± 54	$26.7 \pm 2.2 \pm 1.9$
1.9-2.0	542 ± 60	$26.3 \pm 2.9 \pm 2.3$
2.0-2.1	403 ± 54	$23.3 \pm 3.1 \pm 4.5$
2.1-2.2	285 ± 35	$21.0 \pm 2.6 \pm 4.9$
2.2-2.4	449 ± 80	$40.3 \pm 7.2 \pm 11$
2.4-2.6	273 ± 84	$27.9 \pm 8.6 \pm 11$
2.6-2.8	87 ± 82	$11.5 \pm 11 \pm 13$

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- [1] M. Misiak *et al.*, Phys. Rev. Lett. **98**, 022002 (2007).
- [2] M. Ciuchini, G. Degrossi, G. Gambino and G.F. Giudice, Nucl. Phys. B **534**, 3-20 (1998).
- [3] A. Freitas and U. Haisch, Phys. Rev. D **77**, 093008 (2008).
- [4] T. Becher and M. Neubert, Phys. Rev. Lett. **98**, 022003 (2007).

- [5] Particle Data Group, Chin. Phys. C Vol.38, No. 9 (2014) 090001.
- [6] A. Abashian *et al.* (Belle Collaboration), Nucl. Instr. and Meth. A **479**, 117 (2002); also, see the detector section in J. Brodzicka *et al.*, Prog. Theor. Exp. Phys., 04D001 (2012).
- [7] S. Kurokawa and E. Kikutani, Nucl. Instr. and Meth. A **499**, 1 (2003), and other papers included in this volume; T. Abe *et al.*, Prog. Theor. Exp. Phys., 03A001 (2013) and following articles up to 03A011.
- [8] K. Abe *et al.* (Belle Collaboration), Phys. Lett. B **511**, 151-158 (2001).
- [9] A. L. Kagan, M. Neubert, Eur. Phys. J. C. **7**, 5-27 (1999).
- [10] A. Limosani *et al.* (Belle Collaboration), Phys. Rev. Lett. **103**, 241801(2009).
- [11] T. Sjöstrand, S. Mrenna and P. Skands, JHEP 0605:026(2006).
- [12] E. Nakano, Nucl. Instrum. Meth. A **494**, 402 (2002).
- [13] NeuroBayes software package based on Bayesian statistics, M. Feindt and U. Kerzel, Nucl. Instrum. Meth. A **559** (2006) 190-194.
- [14] The Fox-Wolfram moments were introduced in G. C. Fox and S. Wolfram, Phys. Rev. Lett. **41**, 1581 (1978).
- [15] S. H. Lee *et al.* (Belle Collaboration), Phys. Rev. Lett. **91**, 261801 (2003).
- [16] H. Kakuno *et al.* (Belle Collaboration), Nucl. Instr. and Meth. A **533**, 516 (2004).
- [17] T. Skwarnicki, Ph.D. thesis, Institute for Nuclear Physics, Krakow 1986; DESY Internal Report, DESY F31-86-02 (1986).
- [18] H. Albrecht *et al.* (ARGUS Collaboration), Phys. Rev. D **75** 032005 (2007).
- [19] J.P. Lees *et al.* (BABAR Collaboration), Phys. Rev. D **86**, 052012 (2012).

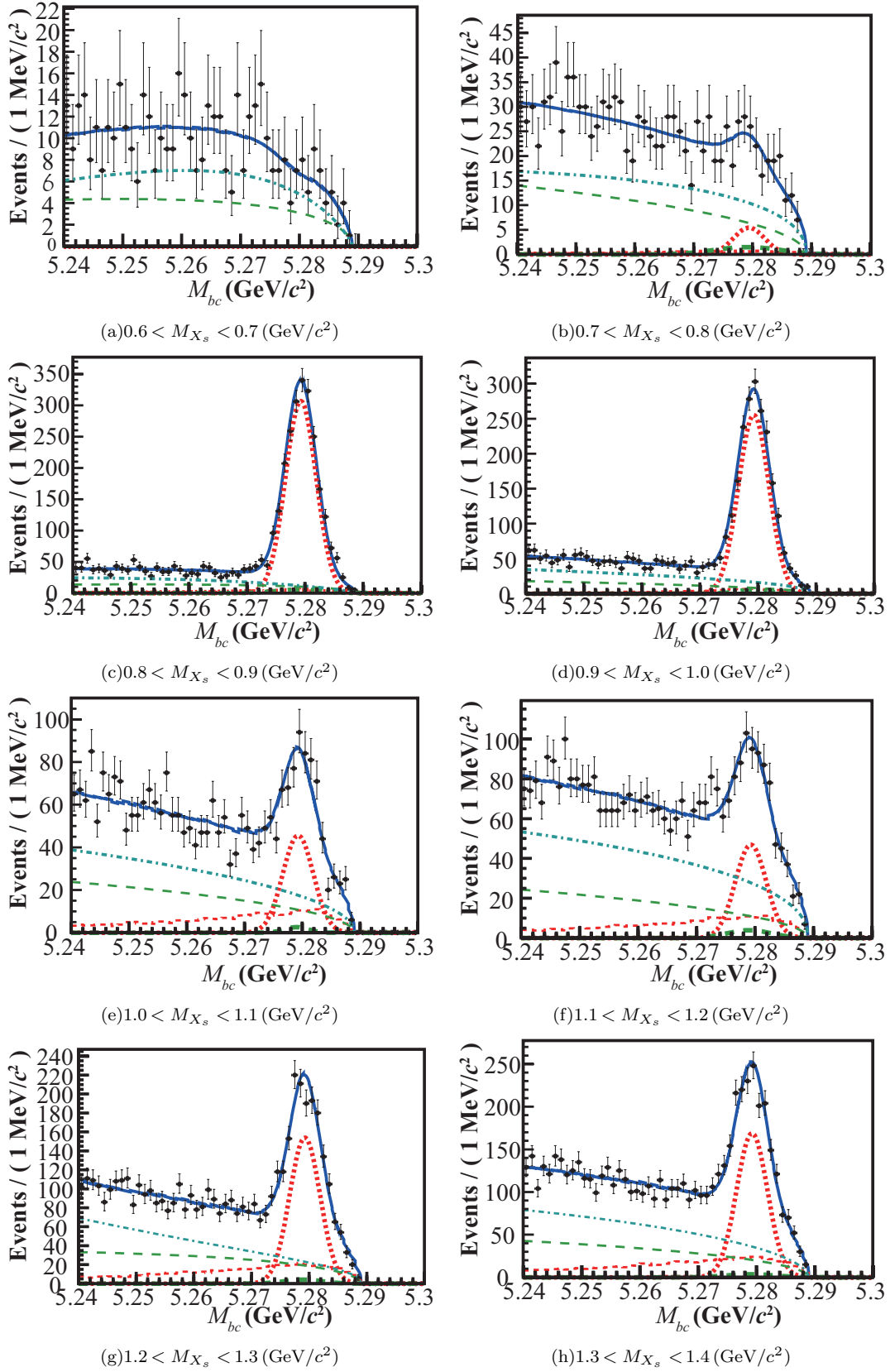


FIG. 2. M_{bc} fits in M_{X_s} bins in $0.6 \text{ GeV}/c^2 < M_{X_s} < 1.4 \text{ GeV}/c^2$. The plot shows the data (black points), and the fit function (blue solid line). The fit components correspond to signal (red thick short dashed line), cross-feed (red thin short dashed line), peaking $B\bar{B}$ background (green thick long dashed line), non-peaking $B\bar{B}$ background (green thin long dashed line) and $q\bar{q}$ background (blue dot-dashed line).

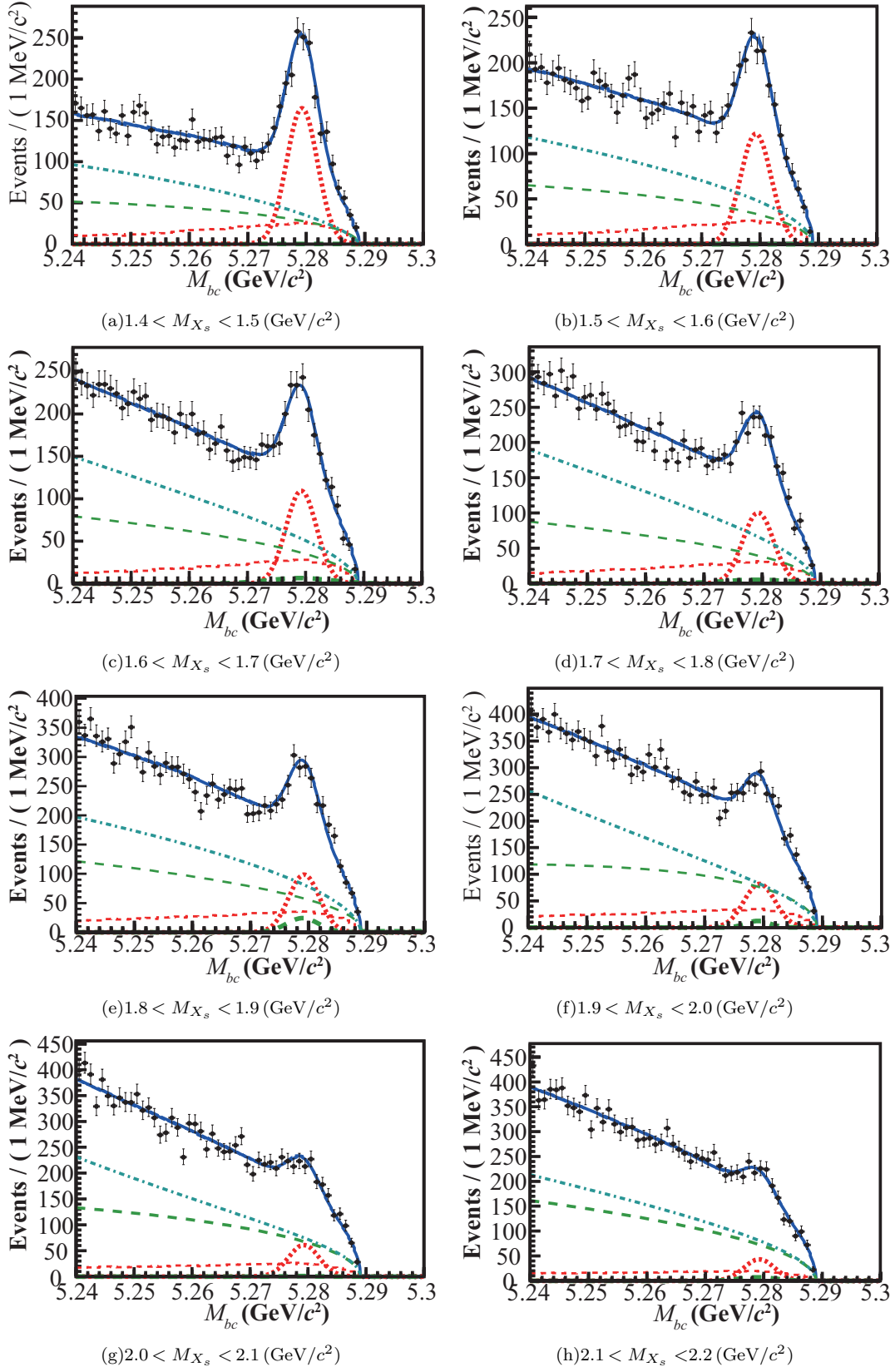


FIG. 3. M_{bc} fits in M_{X_s} bins in $1.4 \text{ GeV}/c^2 < M_{X_s} < 2.2 \text{ GeV}/c^2$. The plot shows the data (black points), and the fit function (blue solid line). The fit components correspond to signal (red thick short dashed line), cross-feed (red thin short dashed line), peaking $B\bar{B}$ background (green thick long dashed line), non-peaking $B\bar{B}$ background (green thin long dashed line) and $q\bar{q}$ background (blue dot-dashed line).

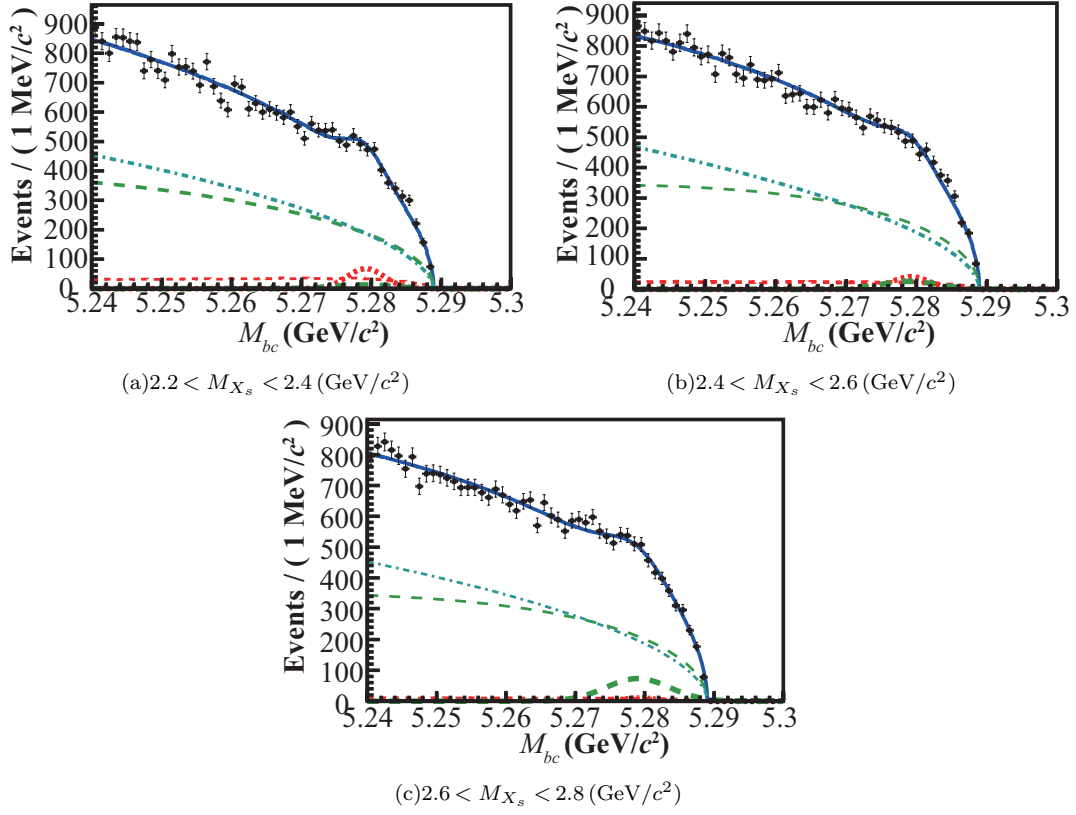


FIG. 4. M_{bc} fits in M_{X_s} bins in $2.2 \text{ GeV}/c^2 < M_{X_s} < 2.8 \text{ GeV}/c^2$. The plot shows the data (black points), and the fit function (blue solid line). The fit components correspond to signal (red thick short dashed line), cross-feed (red thin short dashed line), peaking $B\bar{B}$ background (green thick long dashed line), non-peaking $B\bar{B}$ background (green thin long dashed line) and $q\bar{q}$ background (blue dot-dashed line).

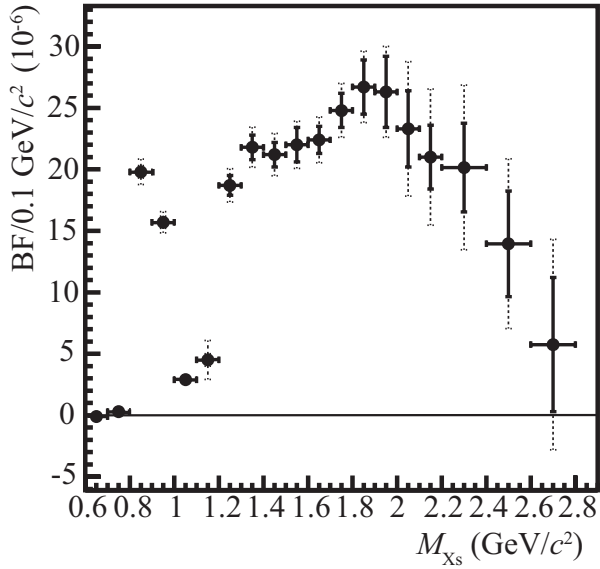


FIG. 5. Partial branching fraction as a function of M_{X_s} . The error bars correspond to the statistical (solid) and the quadratic sum of the statistical and systematic (dashed).