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**Author/s:**

Johnston, ST;Faria, M;Crampin, EJ

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# Isolating the sources of heterogeneity in nano-engineered particle-cell interactions

Stuart T Johnston<sup>1,2,\*</sup>

Matthew Faria<sup>1,2</sup>

Edmund J Crampin<sup>1,2,3</sup>

## Abstract

Nano-engineered particles have the potential to enhance therapeutic success and reduce toxicity-based treatment side effects via the targeted delivery of drugs to cells. This delivery relies on complex interactions between numerous biological, chemical and physical processes. The intertwined nature of these processes has thus far hindered attempts to understand their individual impact. Variation in experimental data, such as the number of particles inside each cell, further inhibits understanding. Here we present a mathematical framework that is capable of examining the impact of individual processes during particle delivery. We demonstrate that variation in experimental particle uptake data can be explained by three factors: random particle motion; variation in particle-cell interactions; and variation in the maximum particle uptake per cell. Without all three factors, the experimental data cannot be explained. This work provides insight into biological mechanisms that cause heterogeneous responses to treatment, and enables precise identification of treatment-resistant cell subpopulations.

**Keywords:** Cell heterogeneity, nano-engineered particles, mathematical modelling, particle-cell interactions, cell cycle.

1. Systems Biology Laboratory, School of Mathematics and Statistics, and Department of Biomedical Engineering, University of Melbourne, Parkville, Victoria 3010, Australia.
2. ARC Centre of Excellence in Convergent Bio-Nano Science and Technology, Melbourne School of Engineering, University of Melbourne, Parkville, Victoria 3010, Australia.
3. School of Medicine, Faculty of Medicine Dentistry and Health Sciences, University of Melbourne, Parkville, Victoria 3010, Australia.

\* stuart.johnston@unimelb.edu.au.

# 1 Introduction

Elucidating how individual biological and physical processes dictate the successful cellular uptake of nano-engineered particles is crucial for future developments in areas such as nanomedicine and nanotoxicology [1, 2]. Untangling the role of a particular process requires a detailed understanding of the complex marriage of transport phenomena, physicochemical particle characteristics and biological behaviour that govern particle-cell interactions [1, 2, 3, 4]. It is well established that the physicochemical properties of a nano-engineered particle, such as size, shape and surface charge, impact particle uptake [1, 2, 4, 5]. Note that we use the terminology of nano-engineered particles to follow the FDA definition of nanotechnology: “products that contain or are manufactured using materials in the nanoscale range [6].” This is in contrast to referring to the particles as nanoparticles, as this may imply that the particles are less than 100 nm in diameter. The exact influence of the physicochemical properties of particles on uptake is unclear, as the impact is obscured by both the influence of transport phenomena, such as sedimentation, diffusion and aggregation, and cell-type specific interactions between cells and particles [4, 7, 8, 9]. The inherent variation in cell characteristics within a population further obscures the roles of individual processes, and results in heterogeneous experimental data [10, 11, 12, 13, 14].

Heterogeneity in experimental data may imply that commonly-reported population-averaged measures do not accurately reflect the underlying biology [15, 16, 17]. For example, consider a particle-cell association assay, where the average number of particles associated with a cell is measured after exposure to a particular concentration of particles [8]. This measure, referred to as particle dose, can be used as a proxy for the effectiveness of a putative treatment [18]. Effective treatment of disease via drug-loaded particles may require universal cellular uptake within a population [13], such that all cells interact with the drug. Reporting only the average number of associated particles does not distinguish between the influence of stochastic processes, where all cells are identical but associate with particles at random, and the presence of distinct subpopulations of cells that interact differently with particles due to fundamental differences in biology (Fig. 1). Certain cell subpopulations may not associate with particles, or associate with particles at an inhibited rate [13]. Even if such cell subpopulations are rare, they can nevertheless have a substantial impact on disease progression [15, 19, 20]. Identifying whether a cell population does, in fact, contain heterogeneity in relevant cell characteristics or whether variation in experimental data is merely a by-product of the stochastic nature of particle transport is therefore critical for therapeutic success [10, 11, 12, 13, 14]. Furthermore, understanding how heterogeneity in cell characteristics, such as receptor numbers or vesicle formation rates, manifests itself in commonly-measured experimental data is crucial for isolating and quantifying sources of heterogeneity.

Nano-engineered particle motion is inherently stochastic due to the fundamental length scales involved in the transport process [3, 12]. As such, the measured particle dose per cell will be

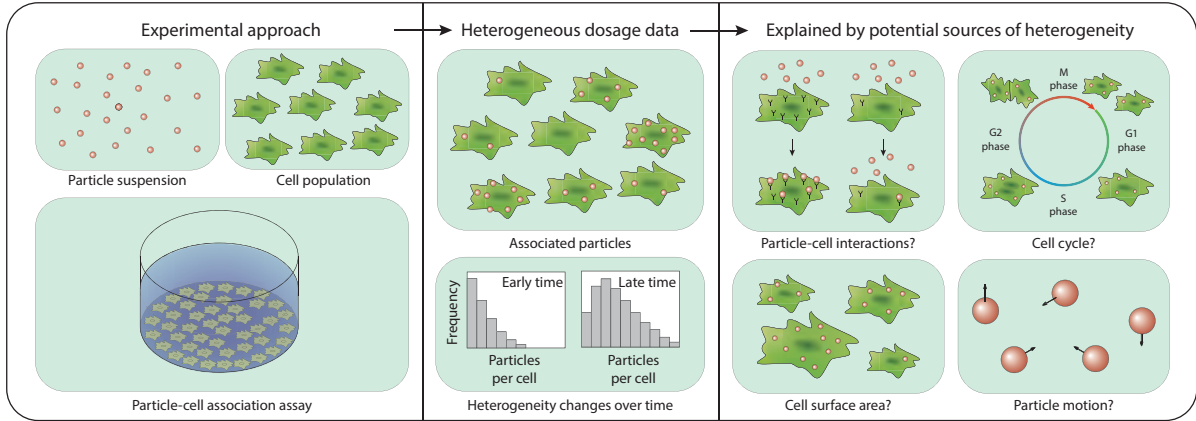


Figure 1: **Schematic highlighting the experimental approach that gives rise to a heterogeneous dosage distribution with potential sources of heterogeneity.** Particle-cell association assays result in heterogeneous dosage distributions, which may be explained by heterogeneity in (i) particle-cell interactions; (ii) the cell cycle; (iii) cell surface area or; (iv) stochastic particle motion.

distributed according to the transport properties, as well as any potential heterogeneity in cell characteristics. Without careful consideration of the contribution of the stochastic nature of transport to the dosage distribution, heterogeneity in cell characteristics can be misidentified or incorrectly estimated. Mathematical models of particle motion are effective at isolating the contribution of particle transport to dosage from biological interactions [3, 5, 7, 8, 9]. However, such models describe the average particle behaviour and dose, and are not suitable for predicting dosage distributions or cell heterogeneity. Statistical approaches allow for the quantification of heterogeneity from experimental data [10, 11, 14], but do not provide mechanistic understanding about how heterogeneity in experimental data arises from heterogeneity in multiple cell characteristics. Further, as we will demonstrate, conclusions obtained from previous statistical approaches are incapable of explaining heterogeneity observed in our time course experiments.

## Results

Here we develop and introduce a model of individual nano-engineered particle behaviour that is capable of describing and predicting cell heterogeneity. This modelling framework mimics experimental conditions while providing detail at both an individual particle and individual cell level. The standard experimental approach for analysing particle-cell interactions is an adherent cell culture association assay [7]. In an association assay, a cell population seeded on a culture dish is incubated in media containing a particle suspension (Fig. 1) [7]. The particles undergo transport through the fluid via a combination of sedimentation and diffusion, and ultimately arrive at the cell-media interface (Fig. 2(c),(e)-(g)) [3, 7, 8, 9]. Particles bind to receptors on the cell surface and are internalised via various endocytic processes [4]. The evolution of the number of particles associated with each cell is measured to provide time course information on the dose (Fig. 2(d)). It is difficult to distinguish between particles that are internalised

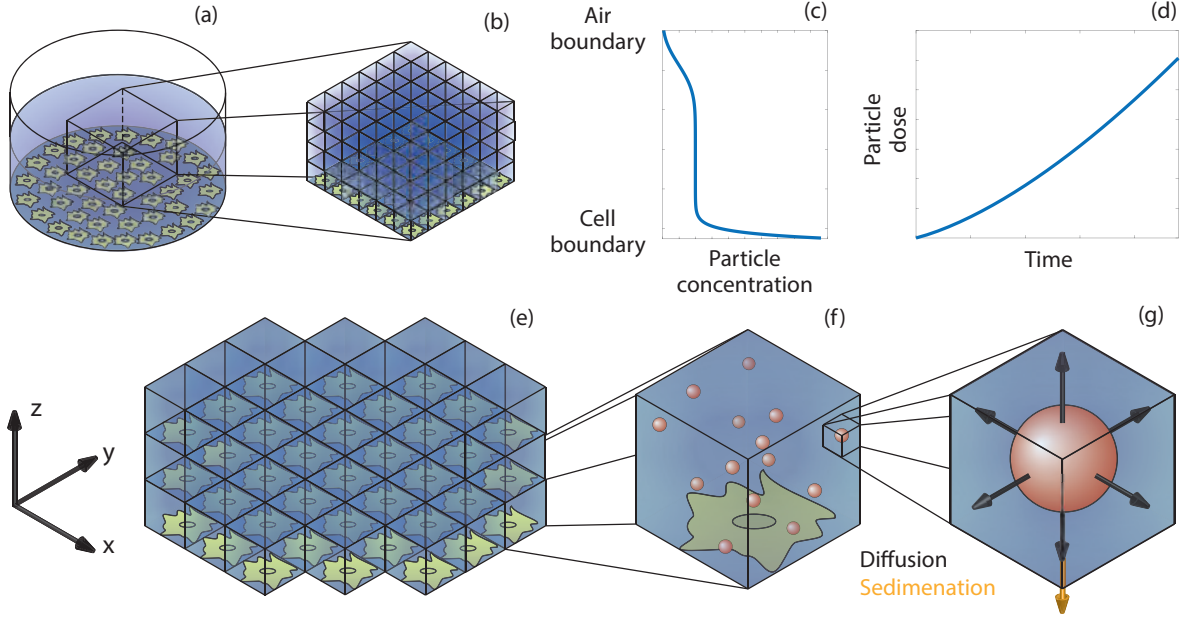


Figure 2: **Experimental and model geometry.** (a) Standard experimental geometry for an *in vitro* adherent cell culture association assay. (b) Representative geometry for the voxel-based modelling framework. (c) Typical particle concentration as a function of depth due to sedimentation and diffusion of particles. (d) Typical particle association curve. (e) Media-cell boundary in the modelling framework highlighting (f) particle locations within a voxel and (g) the contributions of random motion (diffusion) and directed motion (sedimentation) to particle transport.

by a cell or are merely bound to the cell surface, and hence we take the standard approach of using the number of associated particles as a proxy for dose [8, 21]. Due to the ubiquitous use of association experiments to investigate particle efficacy, we calibrate the geometry and conditions in our modelling framework to an association assay.

We implement a voxel-based framework, where the experimental domain is discretised into cube-shaped subdomains known as voxels (Fig. 2(a)-(b)). We model the number of particles within each voxel, which evolves with time due to stochastic transitions of particles between voxels. The transition rates correspond to the combined rates of sedimentation and diffusion [22]. Transition events are sampled via a spatial stochastic simulation algorithm, a modified form of the well-established Gillespie’s algorithm [23]. To replicate experimental conditions, there is no transition of particles through the top of the domain, corresponding to the air-media interface. At the cell-media interface, the transition rate of particles from the media into the cell monolayer corresponds to the cell carrying capacity kinetics derived by Faria *et al.* [8]. These kinetics have been demonstrated to be the most suitable kinetics for describing association assays for a wide range of particle-cell combinations [8]. The kinetics rely on two parameters: a *particle-cell affinity* parameter, which represents the rate of interaction between a particle and a cell, and; a *cell carrying capacity* parameter, which is the maximum number of particles that can associate with a cell [8]. Note that the affinity parameter does not imply a specific type of particle-cell

association, such as clathrin-mediated endocytosis or macropinocytosis. Instead, the affinity parameter is an abstraction of the combined effect of all binding and internalisation processes. As such, the modelling framework is applicable across a range of particle sizes, even though the dominant biological process governing particle-cell association changes with particle size [1, 8]. Full details of the voxel-based model, the equivalence of the transition rate used here to the cell carrying capacity kinetics of Faria *et al.* [8], and an efficient method to calculate the average behaviour in the voxel-based model are derived in the Supplementary Information [22, 24].

### Stochastic motion does not account for all observed variation

Our modelling framework describes both individual particles and individual cells and, therefore, we are able to explicitly measure the number of particles associated with each cell. As particle motion is stochastic, the model output will be a distribution of particles per cell. This distribution can be readily compared with experimental data, as flow cytometry techniques can be used to measure the number of particles associated with each cell for an entire cell population [25, 26, 27].

Experimentally, even when all cells have identical characteristics, the number of particles per cell will be heterogeneous due to the inherent stochasticity of particle motion. This dosage distribution is dependent on the association regime of the cells. For example, if the cells are in the linear association regime, where the number of particles per cell is significantly lower than the carrying capacity, then the dosage distribution will be Poisson distributed with an arrival rate equivalent to the average association rate of particles with the cell layer. However, this may not be the case when the particle dose is close to the maximum number of particles per cell.

To determine the influence of stochastic transport on the particle dosage distribution, we perform simulations using our modelling framework and calculate the number of particles associated with each cell. Here we first consider idealised conditions where all cells in an experiment have identical characteristics. These simulations are calibrated to match three different experiments: the first is performed with 1032nm PMA<sub>SH</sub> capsule particles and RAW264.7 cells, the second is performed with 282nm PMA<sub>SH</sub> coreshell particles and HeLa cells, and the third is performed with 150nm PMA<sub>SH</sub> coreshell particles and RAW264.7 cells [8, 28]. Full experimental details can be found in the Supplementary Information.

As noted previously, the dose obtained from the model is only Poisson distributed in the linear association regime (Supplementary Information, Fig. S1). If the number of particles per cell approaches the carrying capacity, the predicted dosage distribution is not well described by the Poisson distribution. Comparing the dosage distribution obtained from the model with the experimental data, we observe that the experimental data is overdispersed compared to the model predictions (Supplementary Information, Fig. S1). This indicates that the cell populations exhibit heterogeneity, and is consistent with previous observations [10, 11, 12, 13, 14].

## Heterogeneity is time dependent

Having established that the experimental data is not consistent with a homogeneous cell population, we next consider implementing heterogeneity in our modelling framework. A natural choice is to allow each cell in the model to have a particle-cell affinity parameter that is sampled from a probability distribution. This represents variation in the biological processes that dictate particle association, such as the number of receptors or vesicle formation rates [11]. Lognormal distributions are prevalent throughout biology, and arise from multiplicative sources of variability [3, 13, 29]. As such, here we make the assumption that affinity is lognormally distributed. Note that other distributions could be considered, and while this would affect the final dosage distribution, the analysis techniques remain the same.

As each cell now has an individual affinity parameter, and the association rate for each cell is proportional to the affinity, the number of particles per cell will follow a Poisson-lognormal distribution [30] (Supplementary Information). Critically, this allows us to determine the relative contributions of stochastic particle motion and cell heterogeneity to the variation in the dosage distribution. The applicability of the Poisson-lognormal distribution relies on the assumption that the number of particles associated with a cell is independent of other cells; that is, competition between cells for particles is minimal. This is appropriate provided that association occurs sufficiently slowly compared to particle transport, as is the case for the particle-cell combinations considered here. There is only a single free parameter in the distribution, the standard deviation, as the mean of the Poisson-lognormal distribution must correspond to the mean number of associated particles. We refer to this standard deviation as the “apparent heterogeneity.”

The apparent heterogeneity is a key concept for the work presented here. As the dosage distribution is described by the Poisson-lognormal distribution, the heterogeneity present in the data is captured via the measure of spread in the Poisson-lognormal distribution: the standard deviation (apparent heterogeneity). It is important to note that this is not the “true” heterogeneity in one (or more) of the cell characteristics. Rather, the apparent heterogeneity represents how the “true” heterogeneity manifests itself in the experimental dosage distribution. As the particle dose can be indicative of therapeutic success, it is therefore necessary to understand how the apparent heterogeneity arises from the “true” heterogeneity in the cell characteristics.

To examine the apparent heterogeneity present in the experimental data, we fit the Poisson-lognormal distribution to the experimental data at each measured time point. In Fig. 3 we present both the distribution fit and the evolution of the apparent heterogeneity. Fig. 3(d)-(f) shows that the Poisson-lognormal describes the data well for all three experiments, indicating that the assumption of lognormally-distributed cell characteristics is appropriate. Notably, the apparent heterogeneity changes with time (Fig. 3(a)-(c)). For each particle-cell pair, the appar-

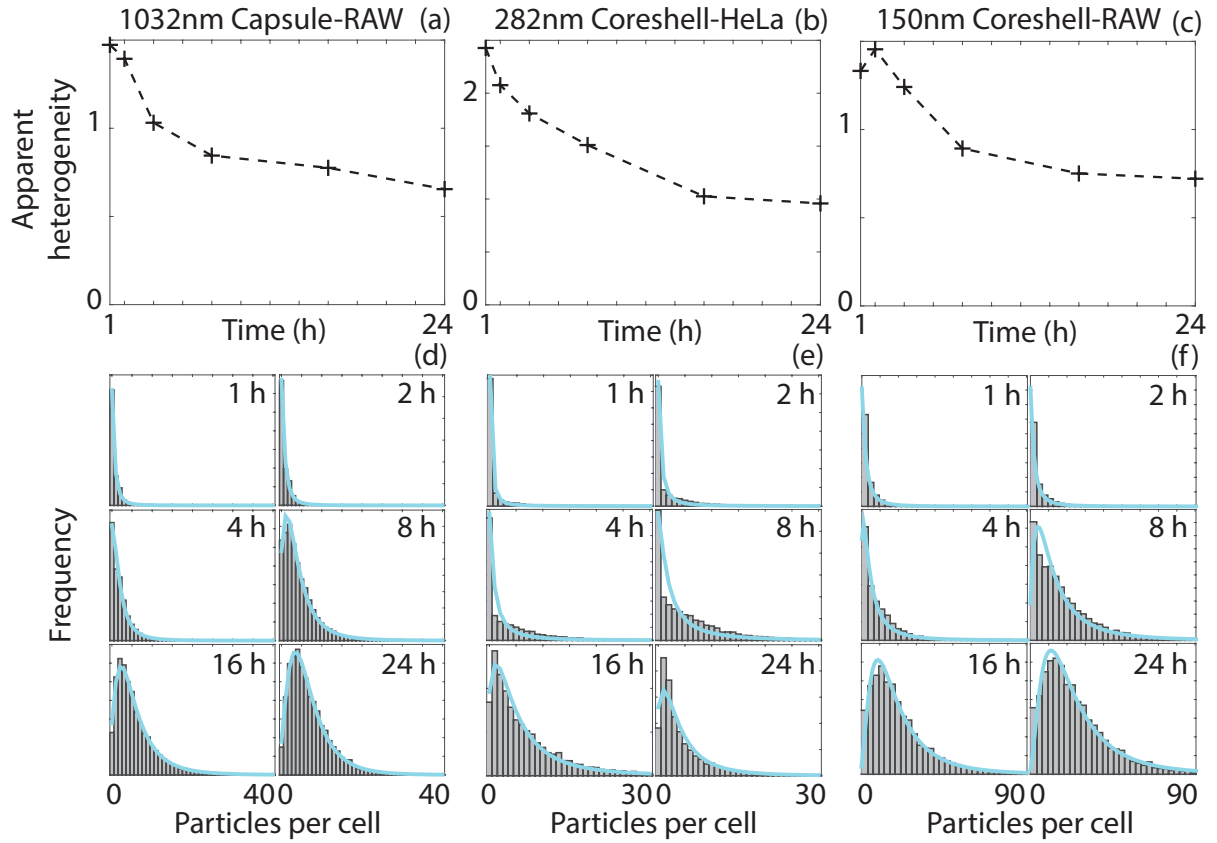


Figure 3: **Heterogeneity appears to change with time.** (a)-(c) Evolution of apparent heterogeneity obtained from experimental data for three particle-cell pairs. (d)-(f) Dosage distributions for the three particle-cell pairs after 1, 2, 4, 8, 16 and 24 hours. The cyan line corresponds to the Poisson-lognormal distribution that best fits the dosage distribution.

ent heterogeneity decreases rapidly at early time before beginning to plateau towards the final experimental observation. This observation suggests that previous investigations into heterogeneity in particle-cell interactions, where the heterogeneity is assumed to be constant [11], do not represent a complete picture due to the time-dependent nature of particle-cell interactions. Therefore, we next seek to determine how the time dependence of apparent heterogeneity arises as a consequence of interactions between particles and various cell characteristics.

### Cell size distribution does not account for time-dependent heterogeneity

To determine whether the experimental apparent heterogeneity arises solely from heterogeneous particle-cell association, as suggested previously [11], we introduce cell heterogeneity into our modelling framework via the affinity parameter. A potential explanation for heterogeneous affinity is the heterogeneity in cell surface area due to the cell cycle [11, 31, 32]. Specifically, we assume that a cell with higher surface area is more likely to interact and associate with particles [11]. We calibrate a lognormal distribution to the square of small-angle light scattering intensity obtained via flow cytometry for both HeLA and RAW264.7 cells to estimate the cell surface area heterogeneity [33]. This heterogeneity is used to create the lognormal distribution for the affinity parameter. We note that the cell morphology may be different for cells in suspension in the flow cytometer, compared to cells adhering to the culture dish. As such, obtaining estimates of cell surface area distributions via *in situ* microscopy images of the adherent cell culture, as in [11], may represent an area of potential improvement for the experimental protocol. However, such an improvement would only impact the accuracy of the affinity parameter, which is not the main focus of this work.

We perform simulations representing the three previously-described experiments, now incorporating heterogeneous particle-cell affinity, and present the results in Fig. 4(a)-(f). To obtain robust estimates of the apparent heterogeneity, we use an efficient approach that provides the average particle dose for each cell, and fit the Poisson-lognormal distribution to this dosage data. This approach provides results that are consistent with the average output of the voxel-based model (Supplementary Information, Fig. S3.), and avoids fluctuations in the apparent heterogeneity due to the stochastic nature of the voxel-based model.

As predicted, the dosage distribution obtained from the model is Poisson-lognormal distributed in the linear association regime, but does not follow the Poisson-lognormal distribution near the carrying capacity. For the simulation of the experiment that remains in the linear association regime (Fig. 4(d)) the apparent heterogeneity stays close to the “true” heterogeneity in the cell characteristics, that is, the standard deviation of the particle-cell affinity distribution (Fig. 4(a)). For the simulation of the two experiments where the number of particles per cell approaches the carrying capacity (Fig. 4(e),(f)), the apparent heterogeneity decreases as time increases, even though the “true” heterogeneity is constant (Fig. 4(b),(c)).

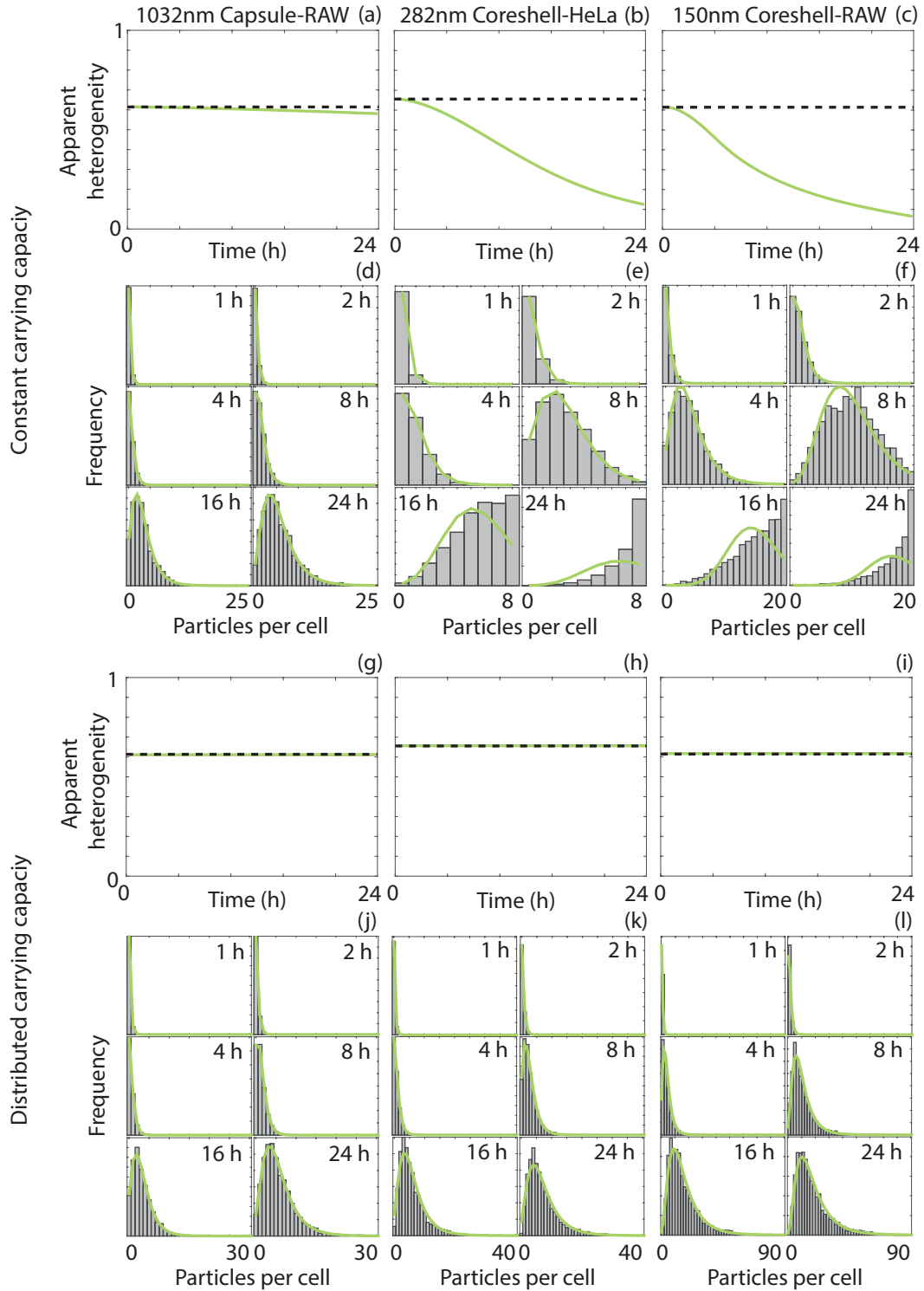


Figure 4: **Cell size distribution does not explain changes in heterogeneity.** (a)-(c), (g)-(i) Evolution of apparent heterogeneity obtained from the modelling framework for three particle-cell pairs. The affinity parameter for each cell is sampled from a lognormal distribution with a standard deviation corresponding to the dashed black line. The cell carrying capacity parameter is either (a)-(c) constant or (g)-(i) lognormally distributed with a standard deviation corresponding to the dashed black line. (d)-(f), (j)-(l) Dosage distributions for the three particle-cell pairs after 1, 2, 4, 8, 16 and 24 hours obtained from the voxel-based model. The green line corresponds to the Poisson-lognormal distribution that best fits the dosage distribution.

While this is a potential explanation for the decrease in apparent heterogeneity observed experimentally, the model predicts that the apparent heterogeneity approaches zero as time increases, whereas the apparent heterogeneity in the experimental data appears to approach a finite positive value (Fig. 3). Further, the time dependence in the apparent heterogeneity obtained from the model results from a breakdown in the match between the dosage distribution and the Poisson-lognormal distribution as the number of particles per cell approaches the carrying capacity (Fig 4(d)-(f)). In contrast, the experimental dosage distribution is well-described by the Poisson-lognormal distribution in all cases, even though the number of particles per cell approaches the carrying capacity in the 282nm coreshell-HeLa and 150nm coreshell-RAW264.7 experiments (Fig. 3). This suggests that the model assumption of a homogeneous carrying capacity is incompatible with the experimental data.

An increase in cell surface area may increase the maximum number of particles that can associate with a cell. As such, we now impose a lognormal distribution on the cell carrying capacity parameter, where this lognormal distribution has the same standard deviation as the cell surface area distribution. We make the assumption that the particle-cell affinity and cell carrying capacity parameters are correlated, that is, a cell with higher affinity due to a higher surface area will also have a higher carrying capacity. We perform simulations, again representing the three previously-described experiments, with heterogeneous particle-cell affinity and heterogeneous cell carrying capacity, and present the results in Fig. 4(g)-(l). The apparent heterogeneity is consistent with the cell surface area heterogeneity in each case (Fig. 4(g)-(i)), and the model dosage distributions are all described well by the Poisson-lognormal distribution (Fig. 4(j)-(l)). However, the model-predicted apparent heterogeneity due to the variation in cell surface area is constant with respect to time, and therefore insufficient to explain the evolution in the apparent heterogeneity obtained from the experimental data.

## Cell cycle does not introduce time-dependent heterogeneity

The previous results assumed that the cells present in the population are representative of all phases within the cell cycle. To investigate whether the progression through the cell cycle during the experiment affects the apparent heterogeneity, we now incorporate the cell cycle explicitly in our modelling framework. We implement a multistage model of cell cycle progression, where cells exist in one of  $m$  states, representing different phases of the cell cycle [34]. Cells transition between states at rates corresponding to the average time spent in a particular phase. Here we choose  $m = 4$ , corresponding to the G1, S, G2 and M phases. We consider two approaches for introducing heterogeneity. First, we impose cell heterogeneity via a lognormal distribution as previously. Second, we introduce a phase-specific mean affinity parameter, representing the change in cell size between phases. The standard deviation is independent of phase. When a cell transitions from M phase to G1 phase, and undergoes mitosis, an additional cell is introduced. The daughter cell either inherits the original cell's affinity parameter, or has the G1 phase affinity parameter, depending on the cell cycle approach considered. The particle load of

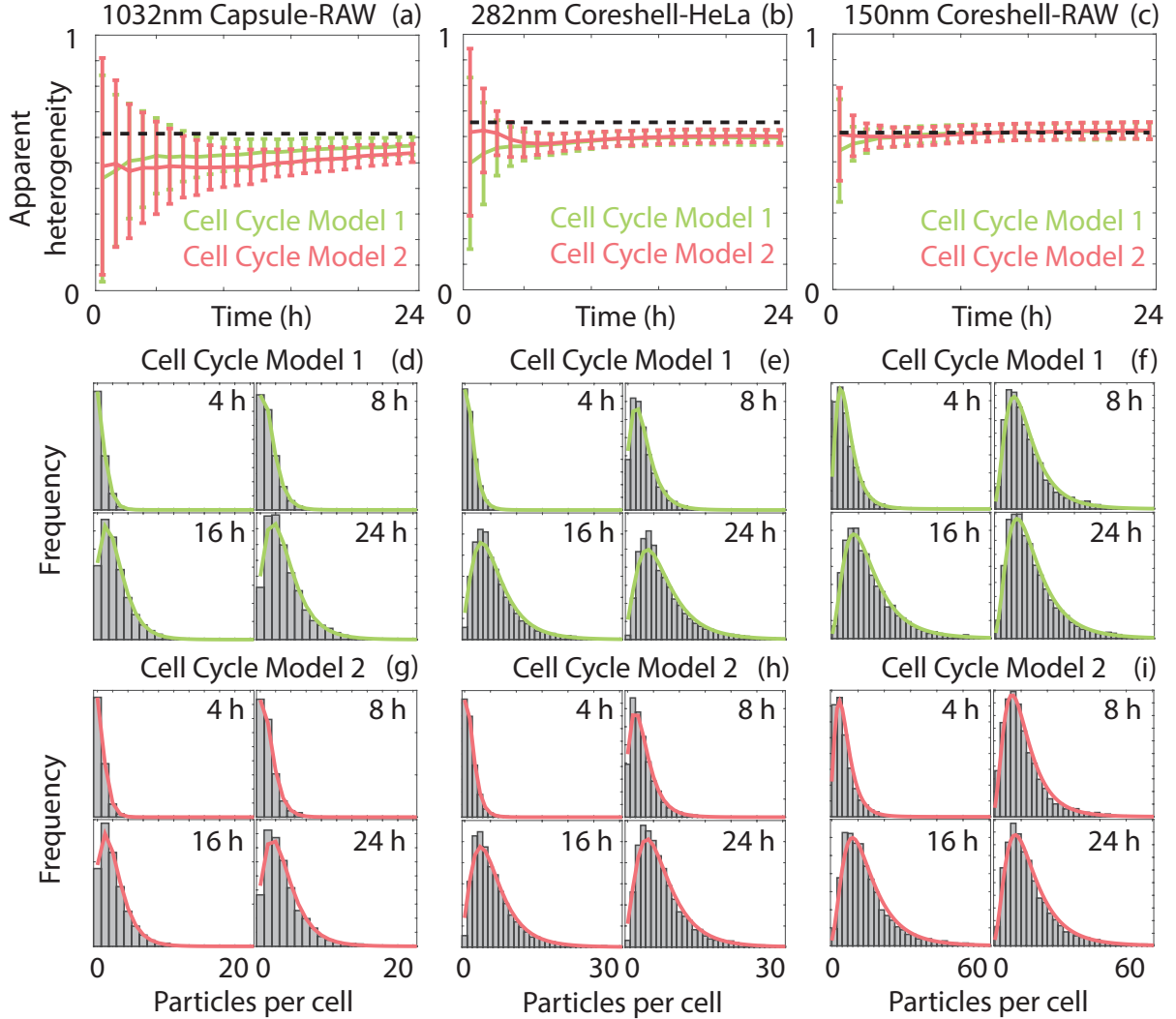


Figure 5: **Cell cycle progression does not explain changes in heterogeneity.** (a)-(c) Evolution of the average apparent heterogeneity obtained from 200 realisations of the voxel-based framework for the three particle-cell pairs if the cell cycle is included in the framework via Model 1 (green) and Model 2 (pink). Error bars correspond to one standard deviation. The dashed black line corresponds to the affinity and capacity heterogeneity. (d)-(i) Dosage distributions for the three particle-cell pairs after 4, 8, 16 and 24 hours obtained from the voxel-based model for (d)-(f) Model 1 and (g)-(i) Model 2. The (d)-(f) green and (g)-(i) pink lines correspond to the Poisson-lognormal distribution that best fit the dosage distribution.

the original cell is split evenly between the original cell and the daughter cell. Full details of the cell cycle model can be found in the Supplementary Information.

We perform simulations representing the three experiments described previously, with the addition of the two approaches for modelling heterogeneity via cell cycle progression, ensuring that the mean affinity is consistent with the previous model simulations. The efficient approach used above to obtain the average particle dose per cell cannot be used here to obtain the apparent heterogeneity as cell behaviour must be explicitly described, and as such we revert to the full voxel-based model. For both approaches we observe that the apparent heterogeneity is relatively consistent, though slightly reduced, compared to the true heterogeneity in the cell characteristics (Fig. 5(a)-(c)). This slight reduction is associated with mitosis; splitting the particle load into two cells reduces the number of cells carrying high numbers of particles. In both cases the apparent heterogeneity is approximately constant over time, unlike the experimental data, which indicates that the cell cycle cannot explain the apparent evolution of heterogeneity in particle dosage distributions. The choice of modelling approach does not significantly influence either the apparent heterogeneity or the dosage distribution, as highlighted in Fig. 5(a)-(c) and Fig. 5(d)-(i), respectively. Therefore, we do not consider the cell cycle in the remainder of this work. The results presented in Fig. 4 and Fig. 5 clearly demonstrate that conclusions drawn from previous investigations [10, 11, 14] into the sources of particle-cell heterogeneity are incomplete, and are incapable of explaining the observed time-dependence of heterogeneity in particle dosage.

### **Interplay between nano-engineered particle motion, affinity heterogeneity and capacity heterogeneity determines apparent heterogeneity**

The association of particles with cells is eventually restricted by the cell carrying capacity [8]. As highlighted by the results in Fig. 4, the heterogeneity in the carrying capacity cannot be neglected. As multiple biological factors may induce heterogeneity in particle-cell affinity or cell carrying capacity, the amount of heterogeneity may differ between different cell characteristics. Therefore, we now relax the assumption that both the cell carrying capacity and the particle-cell affinity are distributed with the same degree of heterogeneity. To determine the heterogeneity for both cell carrying capacity and particle-cell affinity we iteratively calibrate the modelling framework to both the mean particle dose and the apparent heterogeneity obtained from the experimental data. This allows us to extract estimates of the heterogeneity in the cell carrying capacity and the particle-cell affinity, while ensuring that the mean dosage is consistent with the experimental data, as shown in Fig. 6. For each experimental dosage curve, we observe that the model accurately describes the mean experimental dose. By varying the particle-cell affinity heterogeneity and cell carrying capacity heterogeneity independently we are able to match the evolution of the apparent heterogeneity obtained from the experimental data.

At early time, where the rate of particle association predominantly depends on the particle-cell

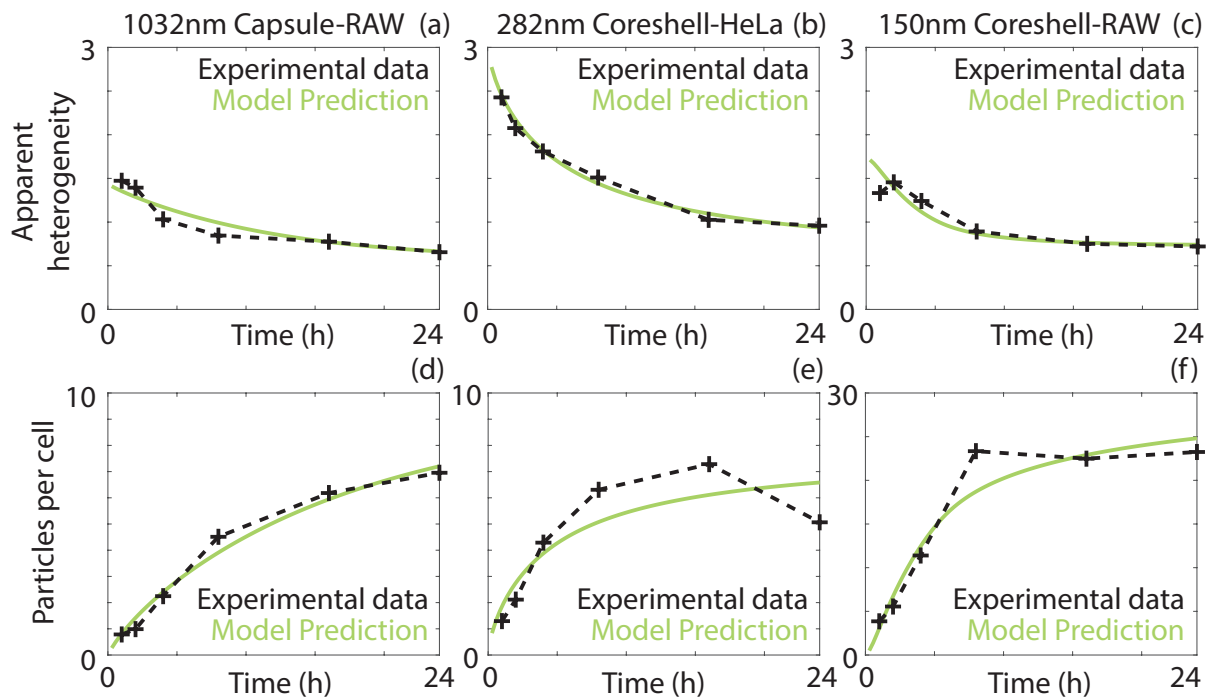


Figure 6: **Combining stochastic transport, particle-cell affinity heterogeneity and cell carrying capacity heterogeneity explains experimentally-observed heterogeneity.** Comparison between the model predictions (green) and experimental data (black) for (a)-(c) apparent heterogeneity and (d)-(f) number of particles per cell for the three particle-cell combinations. Here the heterogeneity in particle-cell affinity is different to the heterogeneity in cell carrying capacity.

affinity, the apparent heterogeneity is close to the “true” heterogeneity in the affinity parameter (1.42, 3.05 and 1.71 in Fig. 6(a)-(c), respectively). As time progresses, the number of associated particles per cell becomes more dependent on cell carrying capacity. Therefore, we observe that the apparent heterogeneity decreases and approaches the “true” heterogeneity in the cell carrying capacity parameter (0.61, 0.62 and 0.75 in Fig. 6(a)-(c), respectively). This transition demonstrates how these two sources of heterogeneity interact and, consequently, how the “true” heterogeneity manifests itself in the experimental dosage data. All three sources of heterogeneity, namely, the stochastic particle motion, variation in particle-cell affinity, and variation in cell carrying capacity, are thus required to explain the heterogeneity in the experimental dosage distributions. Critically, the heterogeneity in the particle-cell affinity is different to the heterogeneity in the cell carrying capacity. Without this difference in heterogeneity between the two cell parameters, we do not observe the change in the apparent heterogeneity over time.

## Discussion and Conclusions

Experimental data obtained from nano-engineered particle-cell association assays exhibit variation in the number of particles associated per cell. We demonstrate that this variation arises from a combination of stochastic particle transport and heterogeneity in cell characteristics. In particular, heterogeneity in the affinity between particles and cells, and heterogeneity in the maximum number of associated particles per cell are shown to be the key biological processes driving variation in experimental data. The amount of variation in the experimental data appears to change with time, but we demonstrate that this is a consequence of different amounts of heterogeneity in these two biological processes.

Uncovering the biological and physical mechanisms that impact the ability of specific cells to associate with, and subsequently internalise, nano-engineered particles is necessary for informed particle design [1, 2, 8]. The ability to reliably deliver particles to a target cell population such that the particles are rapidly internalised has the potential to transform disease treatment and diagnosis [35, 36, 37]. However, the journey between particle creation and cellular internalisation is convoluted, and involves a multitude of intertwined biological, physical and chemical processes [1, 2, 3, 4, 8]. The combination of this complex tapestry with heterogeneous experimental data has thus far inhibited understanding of the key mechanisms governing particle-cell interactions.

Here we develop a mathematical framework of individual-level particle-cell interactions that can be used to separate the physical processes governing particle transport from the biological processes dictating the cellular uptake of nano-engineered particles. We employ this framework to explain the apparent temporal evolution of heterogeneity within a cell population. This apparent evolution is driven by the interplay between the inherent stochastic motion of the particles, the heterogeneity in the maximum number of particles internalised by a particular cell, and the

heterogeneity in the affinity between the particles and the cells. When considered in isolation, these three processes are unable to describe the apparent evolution in heterogeneity present in the experimental data. All three sources of heterogeneity in concert are necessary to explain the experimental data. Further, we demonstrate the impact of the cell cycle is insufficient to explain the heterogeneity in particle dose. This is in contrast to results obtained from a recent investigation [11], where it was claimed that the combination of stochastic particle motion and the distribution of cell surface area is sufficient to explain the heterogeneity in particle dosage. While this explanation is valid for the short-time experiments performed in [11], we conclusively demonstrate, using our modelling framework and performing experiments over a longer time period, that this combination does not give rise to the experimental observation that heterogeneity that changes over time. This has important implications for understanding the impact of heterogeneity, as our modelling approach reveals that the critical biological mechanism inducing heterogeneity in particle dosage changes over time.

By recognising that early-time particle-cell association is driven by particle-cell affinity and that late-time particle-cell association is governed by the cell carrying capacity, we provide an intuitive explanation for the apparent evolution of heterogeneity in the experimental data. That is, the apparent heterogeneity is equal to the particle-cell affinity heterogeneity at early time, and will transition to the cell carrying capacity heterogeneity over time, at a rate corresponding to the particle transport and association rate.

Extracting reliable estimates of the true heterogeneity in cell characteristics is critical for therapeutic purposes [13, 19, 20]. If only a fraction of a cell population appears to internalise a therapeutic dose of particles, it is crucial to determine whether this is due to stochastic interactions or an underlying biological process. The former implies that increasing the dosage or exposure time will increase the fraction of the population that are effectively treated, whereas the latter suggests that an alternative treatment protocol may be required. Further, the cells that do have lower particle affinity, and a lower carrying capacity, are more likely to not internalise particles (Supplementary Information, Fig. S9). This imposes a selective pressure on the cell population toward lower particle-cell affinity and cell carrying capacity values, as such cells do not respond to the particle treatment.

The framework presented here demonstrates that mechanistic modelling approaches can be employed to isolate the sources of heterogeneity present in a cell population from particle-cell association data. Subsequently, this provides insight into whether cell subpopulations exist, and the degree to which such subpopulations are resistant to treatment. More generally, this work highlights how mechanistic insight can be utilised to explain the presence and origin of heterogeneity in experimental data. The influence of cell heterogeneity is a current question of interest across a diverse range of fields, including cancer biology [19, 20], molecular biology [38], nanomedicine [11, 14] and microbiology [39]. Mechanistic models that incorporate heterogeneity and examine its associated impact, such as the one presented here, may provide the key

required to understand the influence of cell heterogeneity.

## **Materials and Methods**

Detailed information regarding the mathematical framework and experimental protocol can be found in the Supplementary Information.

## **Data and code availability**

Certain experimental data used in this analysis have been previously published [8] and raw data are available at [https://figshare.com/projects/In\\_vitro\\_cell-particle\\_association/59162](https://figshare.com/projects/In_vitro_cell-particle_association/59162). The code used to implement the mathematical framework is available at <https://github.com/DrStuartJohnston/nanoparticle-cell-interactions>.

## **Author contributions**

STJ conceived the study. STJ, MF and EJC designed the numerical experiments. STJ designed and performed the analysis. STJ wrote the manuscript. STJ, MF and EJC edited the manuscript. All authors gave final approval for publication.

## **Competing interests**

The authors declare that there are no conflicts of interest.

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