








Measurements of the Cross-spectra of the Cosmic Infrared and Microwave Backgrounds from 95 to 1200 GHz

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Abstract

We present measurements of the power spectra of cosmic infrared background (CIB) and cosmic microwave background (CMB) fluctuations in six frequency bands. Maps at the lower three frequency bands, 95, 150, and 220 GHz (3330, 2000, and 1360 μm) are from the South Pole Telescope, while the upper three frequency bands, 600, 857, and 1200 GHz (500, 350, 250 μm) are observed with *Herschel*/SPIRE. From these data, we produce 21 angular power spectra (6 auto- and 15 cross-frequency) spanning the multipole range $600 \leq \ell \leq 11,000$. Our measurements are the first to cross-correlate measurements near the peak of the CIB spectrum with maps at 95 GHz, complementing and extending the measurements from Planck Collaboration et al. at 143–857 GHz. The observed fluctuations originate largely from clustered, infrared-emitting, dusty star-forming galaxies, the CMB, and to a lesser extent radio galaxies, active galactic nuclei, and the Sunyaev–Zel’dovich effect.

Key words: cosmic background radiation – cosmology: observations – galaxies: evolution – infrared: galaxies – large-scale structure of universe – submillimeter: galaxies

1. Introduction

Maps of the cosmic microwave background (CMB) provide a snapshot of the early universe, and lead to some of the most powerful tests of cosmology today (e.g., Louis et al. 2017; Henning et al. 2018; Hou et al. 2018; Planck Collaboration et al. 2018). The CMB is by far the brightest signal at millimeter (mm) wavelengths from scales of a few degrees to a few arcminutes. However, on smaller angular scales or at higher frequencies, the maps begin to be dominated by a combination of the thermal and kinematic Sunyaev–Zel’dovich (SZ) effects, radio galaxies, and thermal emission from dusty star-forming galaxies (DSFGs; Hauser & Dwek 2001; Lagache et al. 2005; Casey et al. 2014). This complex mixture encodes information about structure growth and the connection between galaxies, star formation, and the underlying dark matter halos.

DSFGs are actively star-forming galaxies (with typical star formation rates $>10 M_{\odot} \text{ yr}^{-1}$ and $L_{\text{IR}} > 10^{11} L_{\odot}$), enshrouded at varying levels by interstellar dust grains (Draine & Lee 1984; Draine 2003). The dust efficiently absorbs the ultraviolet light from the hot, young stars and thermally reradiates as a modified blackbody with a characteristic temperature of $T_d \sim 30$ K and a peak in emission at $\lambda_{\text{rest}} \sim 100 \mu\text{m}$. Thermal emission from the DSFGs is collectively referred to as the cosmic infrared background (CIB). The CIB accounts for approximately half of the total energy released over the history of cosmic star formation (Dole et al. 2006).

Despite the brightness of the CIB and the correspondingly abundant population of DSFGs, directly resolving a typical DSFG has proven extremely challenging, mostly because of the blending together of sources by large instrumental beams (source confusion; e.g., Blain et al. 1998; Lagache et al. 2003; Nguyen et al. 2010). While the most luminous sources are often easily identified (e.g., Smail et al. 1997; Barger et al. 1998; Hughes et al. 1998)—even at very high redshifts (e.g., Marrone et al. 2018)—these luminous DSFGs make up at most 15% of the CIB (Viero et al. 2013b). Most of the remaining intensity is found in “luminous infrared galaxies,” a class of galaxies that is become increasingly common at $z \gtrsim 0.5$, with infrared luminosities of $\log(L/L_{\odot}) = 11\text{--}12$, star formation rates of $10\text{--}100 M_{\odot} \text{ yr}^{-1}$, stellar masses of $\log(M/M_{\odot}) = 10\text{--}11$ (generally around the knee of the stellar-mass function, M_* ; e.g., Ilbert et al. 2013; Muzzin et al. 2013), and 600 GHz flux densities of 1–5 mJy. The only way to measure the signal from sources this faint is statistically. Generally, this is done in real space through the covariance of an image with ancillary data (also known as stacking; e.g., Dole et al. 2006; Marsden et al. 2009; Viero et al. 2012, 2013b); or in Fourier space through correlations in the spatial distribution of their projected emission (e.g., Bond et al. 1986; Haiman & Knox 2000; Knox et al. 2001).

The first detection of galaxy clustering in the CIB anisotropy was made at 1.9 THz (160 μm) in *Spitzer* data (Grossan & Smoot 2007; Lagache et al. 2007), followed by measurements at 600, 857, and 1200 GHz with BLAST (Viero et al. 2009), and at 150 and 220 GHz with the South Pole Telescope (SPT; Hall et al. 2010). Subsequent observations with *Herschel*/SPIRE at 600, 857, and 1200 GHz (Amblard et al. 2011; Thacker et al. 2013; Viero et al. 2013a) confirmed and extended these measurements to include cross-frequency spectra. Other works began connecting the millimeter and submillimeter backgrounds, using data from *Planck* at 217, 353, 545, and 857 GHz (Planck Collaboration et al. 2011), or from a combination of BLAST and

the Atacama Cosmology Telescope (ACT) at 148 and 218 GHz (Hajian et al. 2012). At millimeter wavelengths, ACT (Dunkley et al. 2011) and SPT (Reichardt et al. 2012; George et al. 2015, hereafter **G15**) robustly measured power originating from DSFGs and radio galaxies, with **G15** placing constraints on the level of correlation between CIB and thermal SZ (tSZ) of $\xi = 0.113 \pm 0.056$.

In this work we build upon previous efforts bridging the CIB and CMB by combining millimeter data observed with the SPT (Carlstrom et al. 2011) at 95, 150, and 220 GHz, and submillimeter data imaged with the SPIRE instrument (Griffin et al. 2010) aboard the *Herschel Space Observatory* (Pilbratt et al. 2010) at 600, 857, and 1200 GHz. Our measurements complement those made on larger scales by *Planck*—which are particularly sensitive to the linear clustering term—by adding data on smaller angular scales, where nonlinear clustering and shot noise in the galaxy counts dominate. We find strong correlations in and between maps at all wavelengths, increasing the number of bands where correlated signal is robustly detected.

The paper is organized as follows. In Section 2 we describe the SPIRE and SPT data and lay out how we estimate bandpowers. In Section 3 we present the bandpowers and quantify the degree of correlations between observing frequency bands. We summarize our results in Section 4.

2. Data and Analysis

We present power spectrum measurements based on observations of roughly 100 deg² of sky in six frequency bands with *Herschel*/SPIRE and the SPT. Specifically, 102 deg² are used for the SPT-only bandpowers, 86 deg² are used for the SPT \times SPIRE bandpowers, and 90 deg² are used for the SPIRE-only bandpowers. Bandpowers are estimated using a pseudo- C_{ℓ} method, with the covariance matrix estimated with a combination of the scatter in the data and Monte Carlo simulations.

The SPT was used to observe the field at 95, 150 and 220 GHz; maps and power spectra from the SPT frequency bands will hereafter be referred to as SPT. The *Herschel*/SPIRE maps are at 600, 857, and 1200 GHz (500, 350, and 250 μm), and will be labeled by SPIRE. We will refer to cross-spectra between the sets as SPIRE \times SPT.

2.1. SPT Data and Power Spectra

Between 2008 and 2011 the SPT-SZ camera on the SPT was used primarily to survey 2540 deg² of the sky at 95, 150, and 220 GHz. The survey region covers decl. between -40° and -65° and R.A. from 20^h to 7^h. This work is based on one of two deep fields that have $\sqrt{2}$ lower noise at 150 GHz than the full survey; deep field noise levels are $\lesssim 13 \mu\text{K arcmin}$ at 150 GHz. The field used in this work is approximately $10^{\circ} \times 10^{\circ}$ centered at 23^h30^m, $-55^{\circ}00^{\text{m}}$, and was observed in 2008 and 2010. A full list of the SPT-SZ fields can be found in Story et al. (2013).

The SPT-SZ data, maps, and power spectrum analysis used in this work are described by **G15**. Briefly, the data are bandpass filtered to remove atmospheric emission at low frequencies and to avoid aliasing high-frequency noise into the signal band. The data are then binned into 0.5 pixels, and the power spectrum is estimated using a pseudo- C_{ℓ} method (Hivon et al. 2002; Polenta et al. 2005; Tristram et al. 2005). We emphasize that except for

the calibration factor the CMB-only bandpowers in this work are identical to the bandpowers for this field in G15, and should therefore only be combined with the publicly available G15 bandpowers that do not include the RA23H30DEC-55 field.

The SPT beams are determined as in G15. Briefly, the beam is measured using observations of Venus and Jupiter (see, e.g., Story et al. 2013). The approximate FWHMs of the beam mainlobes are $1''.7$, $1''.2$, and $1''.0$ at 95, 150, and 220 GHz, respectively. The absolute calibration of the maps has been updated since G15. As described by Hou et al. (2018), the new calibration is determined by comparing the SPT maps to *Planck* maps over the same footprint. The uncertainty in the SPT power calibration at [95, 150, 220] GHz is [0.43%, 0.34%, 0.84%]. The correlated part of these uncertainties is 0.34%. The beam and calibration uncertainties are included as a correlation matrix in the data release.

For estimating the SPT \times SPIRE bandpowers, we also coadd the $O(100)$ complete, independent SPT maps used by G15 into a single map at each SPT frequency. Each individual map is assigned equal weight when coadding to match the weighting used in the SPT \times SPT bandpowers. By coadding, we reduce the number of FFTs required in the bandpower estimation. Using a single coadded SPT map does not incur a noise bias as the SPT and SPIRE noise is uncorrelated. We will discuss the SPIRE \times SPT bandpower estimation more in the next section.

2.2. Herschel/SPIRE Data

The SPIRE maps at 600, 857, and 1200 GHz (500, 350, and 250 μm) used in this work are the same as those used in Holder et al. (2013) with minor modifications, described below. The maps were constructed from observations designed to target large scales by observing in fast-scan mode ($60'' \text{ s}^{-1}$) to minimize the impact of $1/f$ noise. The full observation consists of twelve 10×3.3 degree scans, resulting in four complete passes of the entire region. The scan direction is alternated such that half of the scans are perpendicular to the other half. The 100 deg^2 map is constructed from a mosaic of these 12 scans.

Data are reduced with standard ESA software and the custom software package, SMAP (Levenson et al. 2010; Viero et al. 2013a). Maps are made using SMAP/SHIM (Levenson et al. 2010), an iterative map-maker designed to separate large-scale noise from signal. Initial processing uses the Herschel Interactive Processing Environment (HIPE³⁹) release version 13.0.4887, which includes that calibration tree version `spire_cal_12_3`. Practically, this represents a change in the calibration from maps used in previous SPT-SPIRE studies (e.g., Hanson et al. 2013; Holder et al. 2013) of 1.1%, 1.3%, and 1.3% at 600, 857, and 1200 GHz, respectively.

Two sets of maps with different pixel sizes are made: one with pixels $15''$ on a side, and the other with pixels $30''$ on a side. The smaller pixels are used for the SPIRE \times SPIRE analysis, in which the target signal is detected strongly at scales smaller than $30''$; this is not the case for SPIRE \times SPT (because of the larger SPT beams), so we can save computing time and storage by using coarser maps for SPIRE \times SPT.

The time-ordered data are split equally into two halves and made into two separate maps, each of which covers the full area. Hereafter, these half-data maps are referred to as jackknife maps or map pairs, and full-data maps as coadded. Note, 1 of

the 12 scans is discarded because of a voltage bias swell (or “cooler-burp” Sauvage et al. 2014) that occurred during a cooler cycle, which if included would lead to large-scale striping. The result is that one of the jackknife maps is not fully sampled; this is taken into account in all stages of bandpower and uncertainty estimation. All sets of maps are made in Lambert azimuthal equal-area projection (also known as zenithal equal area, ZEA), with astrometry identical to that of the SPT map.

The SPIRE map noise levels are 5.6, 4.0, and 2.8 mJy arcmin, and the instrument effective beams are $36''6$, $25''2$, and $18''1$ FWHM at 600, 857, and 1200 GHz, respectively. The maps are converted from their native units of Jy beam^{-1} to Jy sr^{-1} by dividing them by the effective beam areas (see below). The absolute calibration uncertainty is 5%, and is accounted for in the reported beam and calibration correlation matrix.

SPIRE beams are measured with Neptune; with an angular diameter of $\lesssim 2''.5$, Neptune is effectively a point source to SPIRE. Because the effective beam is mildly sensitive to the source spectrum through the passband, the effective solid angle of the beam must be color-corrected (Bendo et al. 2013; Griffin et al. 2013). Following the SPIRE Observers Manual⁴⁰ for a graybody spectrum representative of the CIB ($T = 13.6 \text{ K}$ and $\beta = 1.4$; e.g., Gispert et al. 2000; Planck Collaboration et al. 2014), and fully illuminated beam (passbands scaled by $\nu^{1.7}$), the effective solid angles are 3.878, 1.873, and $1.080 \times 10^8 \text{ sr}$, at 600, 857, and 1200 GHz, respectively. Note that these differ slightly from the solid angles in Viero et al. (2013a), which were 3.688, 1.730, $1.053 \times 10^{-8} \text{ sr}$.⁴¹ As described in detail in Viero et al. (2013a), the beam power spectra are estimated from the Neptune maps after masking background sources with flux densities greater than 30 mJy at 1200 GHz and all pixels beyond $10 \times$ FWHM radius. We check that the exact flux density of masked sources and choice of masking radius do not significantly bias the measurement, and include the differences as part of the Monte Carlo procedure described in Section 2.3.3.

Lastly, the effective band centers for the SPIRE bands with fully illuminated beams and a CIB spectral energy distribution (SED) are 546.0, 796.0, and 1092.4 GHz (549.5, 376.9, and 274.6 μm). The SPT bands have effective CIB band centers of 99.0, 154.2, and 219.6 GHz (3.030, 1.946, and 1.367 mm), respectively.

2.3. Estimating Bandpowers

Bandpowers are estimated using cross-spectrum-based pseudo- C_ℓ methods (Hivon et al. 2002; Tristram et al. 2005). There are minor implementation differences between the analysis of each of the data sets: SPT-only, SPIRE-only, and SPT \times SPIRE.

The SPT-only and SPIRE-only bandpowers (six frequency combinations each) are calculated as in previous SPT and SPIRE power spectrum papers (see George et al. 2015 for the former, and Viero et al. 2013a for the latter). To match George et al. (2015), the SPT-only bandpowers start at $\ell > 2000$. At larger angular scales, the SPT data are dominated by the CMB. The SPT \times SPIRE bandpowers are calculated similarly to the

⁴⁰ Table 5.5 of HERSCHEL-DOC-0798, version 2.5; which can be found at http://herschel.esac.esa.int/Docs/SPIRE/html/spire_om.html.

⁴¹ Across the multipole range $\ell = 1000\text{--}2000$, the changes to HIPE and beam solid angles amount to multiplying the bandpowers presented by Viero et al. (2013a) by factors of 1.05, 0.93, and 0.99 at 600, 857, and 1200 GHz respectively.

³⁹ <http://herschel.esac.esa.int/hipe/>

SPIRE only case; however, full coadded maps from each experiment are used in this case because the noise in SPT and SPIRE maps are uncorrelated. We outline these methods below.

2.3.1. Apodization Mask and Mode-coupling Matrix

For each cross-frequency spectrum we construct a unique mask \mathbf{W} , which has values of unity where the two maps overlap, zero outside, and the boundary is tapered with a 1° Hanning function. Three sets of sources are also masked: (1) sources with flux densities greater than 300 mJy at 1200 GHz; (2) local, extended sources (e.g., resolved IRAS sources); and (3) sources with flux densities greater than 6.4 mJy at 150 GHz. Sets 1 and 2 are masked from any spectrum involving a SPIRE map, set 3 is masked from any spectrum involving an SPT map. As in previous SPT power spectrum measurements (e.g., Reichardt et al. 2012; George et al. 2015), source masks consist of an inner disk that is tapered outside the disk with a Gaussian taper of width $\sigma_{\text{taper}} = 5'$. The inner disk has radius $5'$ for sources above 50 mJy at 150 GHz, $2.5'$ for sources above 6.4 mJy at 150 GHz, and zero for sources selected at 1200 GHz. This procedure is followed for each masked pixel in the extended source case. Finally, the maps are padded with zeros to final sizes greater than twice the original map size.

To correct for the expected mode-coupling induced by the finite sky coverage, we analytically calculate the mode-coupling matrix $M_{kk'}$ [\mathbf{W}]. The binned mode-coupling matrix is inverted in the final step of pseudo- C_ℓ methods to recover an unbiased estimate of the true power spectrum.

2.3.2. Transfer Function and Beams

In addition to the mode-coupling induced by the partial sky coverage and removal of bright point sources, we must account for the effects of filtering during map-making and the instrumental beams. This filtering could include, for example, high-pass filtering to reduce the impact of $1/f$ noise on the final maps, or polynomial fits to temperature data iteratively removed by HIPE. For SPIRE, minimal high-pass filtering is required to make well-behaved maps, as the noise properties are relatively well behaved on large scales (e.g., Pascale et al. 2011). SPT, on the other hand, suffers from large-scale atmospheric noise, which is dealt with by (i) removing a polynomial from each constant-elevation scan and (ii) removing a common mode across each detector wafer for each time sample.

The transfer functions are determined with the iterative method described in Hivon et al. (2002) on simulated maps that were made with the same map-making pipelines on mock data. They are estimated from 400 simulations of each field and wavelength. A unique set of transfer functions is measured for SPIRE, SPT, and SPIRE \times SPT. We have confirmed that the transfer functions are insensitive to the steepness of the input spectra, and that the transfer functions have converged.

In addition to the beams, we include the effects of the finite pixel size in the maps according to the approximation in Wu et al. (2001): 0.5 for maps used in cross-spectra involving SPT data and 0.25 for the *Herschel* maps used in the *Herschel* auto-spectra.

2.3.3. Covariance Matrix

The covariance matrix is estimated in one of two ways depending on the frequency combination. In all cases, we assume that the instrumental noise in each frequency band is independent. For the SPT \times SPT bandpowers, the covariances are calculated exactly as in G15; sample variance is estimated from simulations, and the sum of noise and signal-cross-noise variance is estimated from the scatter in cross-spectra. The covariance estimator changes when SPIRE data appears in the covariance element. Covariance elements that include SPIRE data are calculated through a Monte Carlo simulation that creates many realizations of the sky signal and noise terms. These noise realizations are drawn from the null-map PSD for each frequency. The sky realization is divided into terms simulated as Gaussian fields (CMB, tSZ, kSZ, radio galaxies) and non-Gaussian fields (CIB). The Gaussian terms are fully described by G15. The CIB mock maps are made with correlated sources such that their clustering signal resembles that of the CIB, with fluxes drawn from the Béthermin et al. (2012) model. Note that the Gaussian and non-Gaussian terms are assumed to be uncorrelated. Each sky realization is filtered identically to the real data and added to a noise realization to create mock maps. The power spectrum of the mock maps is calculated with the same pipeline as that used for the real data.

The ensemble of estimated binned power spectra, P_b , are used to measure, \mathbf{V} , the covariance matrix

$$\mathbf{V}_{bb'} = \langle (P_b - \tilde{P}_b)(P_{b'} - \tilde{P}_{b'}) \rangle_{\text{MC}}, \quad (1)$$

where the tilde denotes the mean over all realizations in bin b . The reported errors in the tables and plots are based on the diagonal entries of \mathbf{V} :

$$\sigma_{P_b} = \sqrt{\mathbf{V}_{bb}}. \quad (2)$$

The non-Gaussianity of the CIB realizations leads to substantial off-diagonal terms in \mathbf{V} . We follow Fowler et al. (2010) and check that the simulations are realistic by testing that the four-point function measured directly from data is consistent with that of the simulations. We find that the non-Gaussian contribution ranges are between 5% and 10% of the total error in the regime where the Poisson term dominates.

We also test the robustness of the covariance estimate by splitting the field into four quarters. One quarter is not used due to the voltage bias swell mentioned in Section 2.2. We estimate bandpowers from null maps created by differencing combinations of the other three quarters, and we calculate a χ^2 using the covariance matrix. We find a reasonable χ^2 for the number of degrees of freedom (303, 244, and 303, respectively, for 297 d. o.f.), lending confidence to the covariance estimate.

The reported bandpower error bars and covariance matrix do not include the SPT or SPIRE absolute calibration uncertainties nor the beam uncertainties. The released data files do include a correlation matrix encapsulating these uncertainties that should be combined with the model bandpowers and added to the covariance matrix when evaluating the quality of fit to a model.

2.3.4. Handling Galactic Cirrus

The survey region was carefully chosen to minimize Galactic cirrus; nonetheless, it is important to quantify the small cirrus contribution. We adopt an approach similar to that taken by Viero et al. (2013a). As described in the A.1, this approach

Table 1
Auto- and Cross-frequency Power Spectra and 1σ Uncertainties ($\text{Jy}^2 \text{sr}^{-1}$)

$\ell_{\min} - \ell_{\max}$	ℓ_{eff}	C_{ℓ}^{95}	$C_{\ell}^{95 \times 150}$	$C_{\ell}^{95 \times 220}$	C_{ℓ}^{150}	$C_{\ell}^{150 \times 220}$	C_{ℓ}^{220}
2001–2200	2068	18.33 ± 0.93	30.08 ± 1.29	34.33 ± 1.81	52.08 ± 2.16	65.16 ± 3.03	94.55 ± 5.67
2201–2500	2323	9.14 ± 0.48	13.84 ± 0.52	15.64 ± 0.86	23.86 ± 0.82	31.22 ± 1.25	51.74 ± 2.98
2501–2800	2630	4.04 ± 0.31	6.43 ± 0.30	8.29 ± 0.61	11.84 ± 0.45	17.79 ± 0.73	34.95 ± 1.90
2801–3100	2932	2.12 ± 0.31	3.19 ± 0.20	3.83 ± 0.42	6.19 ± 0.25	10.39 ± 0.48	23.61 ± 1.74
3101–3500	3288	1.36 ± 0.24	1.90 ± 0.13	1.97 ± 0.40	3.59 ± 0.15	7.35 ± 0.35	23.24 ± 1.28
3501–3900	3690	0.63 ± 0.24	1.07 ± 0.11	1.67 ± 0.39	2.50 ± 0.12	5.84 ± 0.26	19.64 ± 0.99
3901–4400	4143	1.17 ± 0.25	0.73 ± 0.11	1.86 ± 0.28	1.88 ± 0.09	5.02 ± 0.23	17.49 ± 0.96
4401–4900	4645	0.26 ± 0.27	0.65 ± 0.10	1.43 ± 0.36	1.67 ± 0.09	4.70 ± 0.21	17.09 ± 0.93
4901–5500	5198	0.67 ± 0.30	0.64 ± 0.10	0.87 ± 0.32	1.48 ± 0.07	4.53 ± 0.17	16.81 ± 0.73
5501–6200	5851	0.37 ± 0.36	0.40 ± 0.10	1.05 ± 0.33	1.40 ± 0.06	4.24 ± 0.15	16.14 ± 0.67
6201–7000	6604	0.10 ± 0.46	0.51 ± 0.12	1.16 ± 0.39	1.38 ± 0.07	4.20 ± 0.16	14.81 ± 0.68
7001–7800	7406	1.01 ± 0.66	0.43 ± 0.16	0.86 ± 0.49	1.33 ± 0.08	3.72 ± 0.18	15.07 ± 0.77
7801–8800	8309	...	0.32 ± 0.20	1.88 ± 0.62	1.09 ± 0.09	4.18 ± 0.19	14.29 ± 0.82
8801–9800	9312	...	0.44 ± 0.32	1.39 ± 0.95	1.31 ± 0.12	4.22 ± 0.25	14.06 ± 1.04
9801–11000	10416	1.23 ± 0.15	3.74 ± 0.30	15.06 ± 1.21

Note. Bandpowers for the SPT frequency bands in units of $\text{Jy}^2 \text{sr}^{-1}$ under the photometric convention $\nu I_{\nu} = \text{constant}$. The reported uncertainties are based on the diagonal of the covariance matrix, and do not include beam or calibration uncertainties.

assumes that the cirrus can be described by a single map (i.e., 100% correlation between observing bands) with an amplitude that scales with frequency as a modified blackbody. While a modified blackbody spectrum has two free parameters, $T_{\text{eff},c}$ and β_c , the two are highly degenerate for the current set of observing frequencies. Therefore, as we are mostly interested in obtaining a good fit for the purposes of removal (as opposed to the exact qualities of the cirrus) we fix $\beta_c = 1.8$ (e.g., Martin et al. 2010). Furthermore, we assume that the cirrus spatial power spectrum follows a power law with index α_c . Under these assumptions, the cirrus power in all bands can be fit with two variables, α_c and $T_{\text{eff},c}$.

To determine the power-law index, we take advantage of the fact that Galactic cirrus is well-traced by nearby HI in the Galactic disk (e.g., Boulanger et al. 1996), with velocities $|\nu_{\text{LSR}}| < 30 \text{ km s}^{-1}$ with respect to the local standard of reference, and column densities $N_{\text{H}} \leq 5 \times 10^{20} \text{ cm}^{-2}$ (e.g., Viero et al. 2014). H_2 begins to form at higher column densities $N_{\text{H}} \leq 5 \times 10^{20} \text{ cm}^{-2}$ (Planck Collaboration et al. 2014), causing the correlation to break down. This field, however, is of low enough Galactic latitude and column density⁴² that this is not an issue. We take HI maps from Parkes Galactic All-Sky Survey survey (GASS; McClure-Griffiths et al. 2009; Kalberla et al. 2010), and measure the power spectrum of the local velocity component of HI across the 100 deg^2 field. We find that the HI exhibits a power-law behavior at $\ell < 600$ (after which the beam attenuates the signal) with slope $\alpha_c = -3.1 \pm 1.4$. We assume that that behavior can be extrapolated to larger ℓ , noting that given the steep fall off there is very little cirrus power in practically all of the reported bandpowers. We also check that contributions from the higher velocity components of the velocity cube are negligible.

We then perform a Monte Carlo simulation to estimate the cirrus contribution to the SPIRE/SPT bands, and in effect the cirrus correction and its associated uncertainties. For each iteration, the cirrus slope and temperatures are drawn from normal distributions of $\alpha_c = -3.1 \pm 1.4$ and

$T_{\text{eff},c} = 19.0 \pm 1.5 \text{ K}$, respectively, and then the spectra are fit with a cirrus power law, templates for the clustered CIB power,⁴³ and a Poisson level. In addition to SPIRE and SPT we include spectra at $100 \mu\text{m}$ —where cirrus has a much higher contribution relative to CIB (Pénin et al. 2012)—from reprocessed IRAS (Neugebauer et al. 1984) observations⁴⁴ (IRIS; Miville-Deschênes & Lagache 2005). Note that we assume the IRIS transfer function on these scales is unity (Hajian et al. 2012; Pénin et al. 2012). The variation in the residual cirrus power (after subtracting the mean) is added to the bandpower covariance matrix.

The cirrus levels are shown as dashed gray lines in Figure 1. We find the corrections overall to be very small, with the only significant corrections in SPIRE \times SPIRE spectra including $250 \mu\text{m}$. Even in these spectra, the correction is only significant in the lowest- ℓ bin and peaks at 24% in the first bin of the $250 \mu\text{m}$ auto-spectrum.

3. Bandpowers

The analysis described above is applied to the $\sim 100 \text{ deg}^2$ of sky in common between the *Herschel*/SPIRE and SPT-SZ surveys. The resulting bandpowers are shown in Figure 1 and tabulated for SPT \times SPT, SPIRE \times SPT, and SPIRE \times SPIRE in Tables 1, 2, and 3, respectively. They are reported in units of $\text{Jy}^2 \text{sr}^{-1}$ with the photometric convention $\nu I_{\nu} = \text{constant}$. Point sources with a $250 \mu\text{m}$ flux $\gtrsim 300 \text{ mJy}$ are masked in the SPIRE maps, while sources with 150 GHz flux $\gtrsim 6.4 \text{ mJy}$ are masked in the SPT maps before calculating the bandpowers. The bandpowers, covariance matrix, beam and calibration correlation matrix, and window functions are available for download on the SPT.⁴⁵

Cirrus-subtracted power spectra are shown as red circles with black error bars in Figure 1. A Poissonian distribution of galaxies at random positions would yield constant power as a function of ℓ in this plot. The upturn in power toward lower ℓ

⁴² The field's mean column density is $N_{\text{H}} = 1.0 \times 10^{20} \text{ cm}^{-2}$ and the peak is N_{H} of $2.3 \times 10^{20} \text{ cm}^{-2}$.

⁴³ We use the one- and two-halo model templates from Planck Collaboration et al. (2011).

⁴⁴ <http://www.cita.utoronto.ca/~mamd/IRIS/IrisDownload.html>

⁴⁵ <http://pole.uchicago.edu/public/data/viero18/>

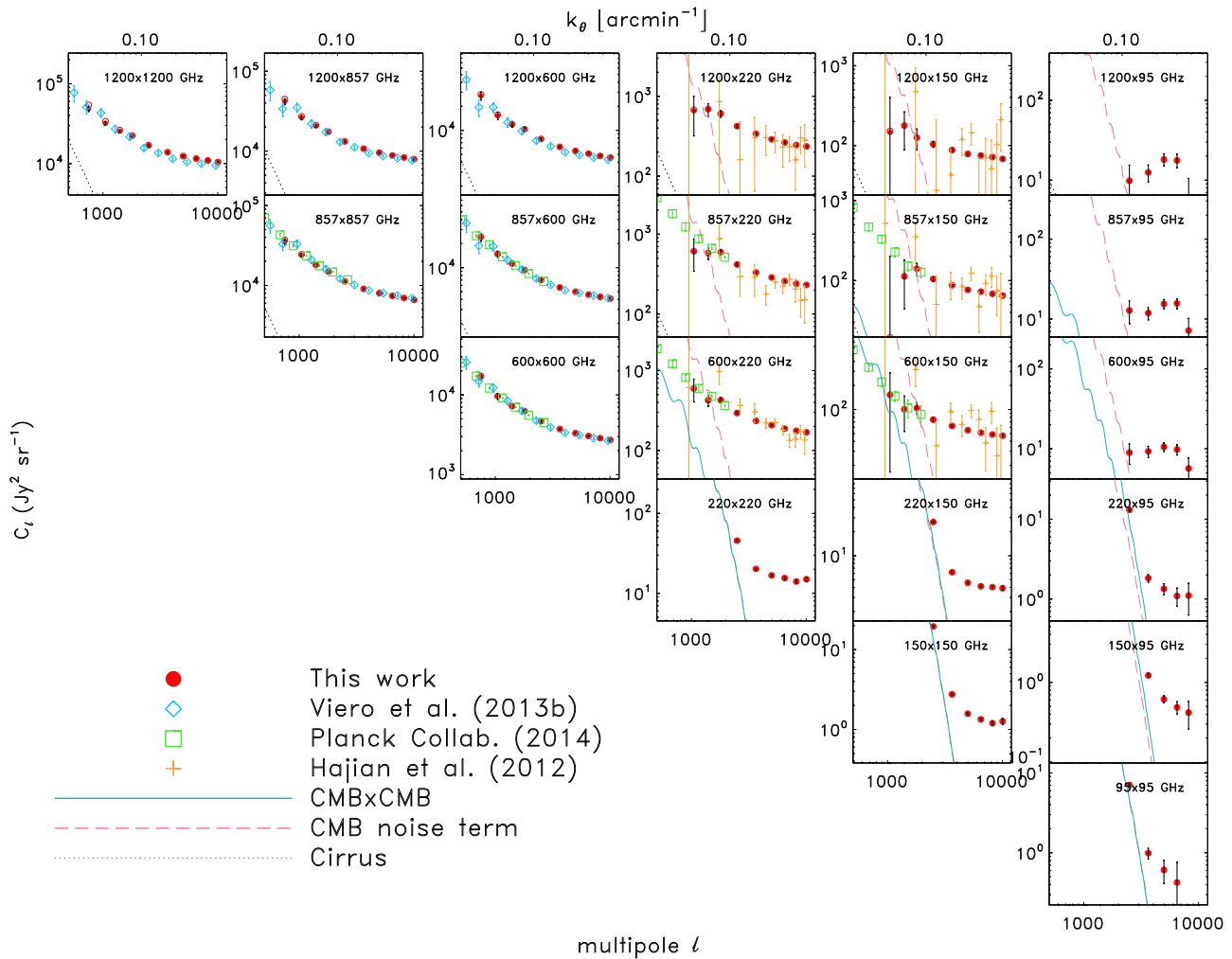


Figure 1. Auto- and cross-frequency power spectra of the sky (solid red circles with black error bars), after accounting for mode-coupling, transfer function, and instrumental beams. Bright point sources have been masked as described in Section 2.3.1 and an estimate of the Galactic cirrus power subtracted. The largely occluded open circles show the results before cirrus-subtraction. Gray dashed lines show the modeled level of Galactic cirrus in each cross-spectrum, while light blue lines show the expected CMB power. The variance due to the CMB (shown by the red, dashed line) can be higher, since it includes a term that scales with the CMB power in each band as well as the cross-spectrum. The plotted error bars are derived from the diagonal of the covariance matrix, as described in Section 2.3.3; there are significant correlations between bandpowers. For this reason and because the spectra change slowly with angular scale, we have rebinned the bandpowers to wider ℓ -bins for plotting purposes. Also shown are measurements from Viero et al. (2013a, blue diamonds), Hajian et al. (2012, orange crosses), and the Planck Collaboration et al. (2014, green squares). Note that to compare *Planck* data at 143, 217, 545, and 857 GHz to that of SPIRE/SPT at 150, 220, 600, and 857 GHz, the *Planck* values are multiplied by 0.423, 1.64, 1.32, and 0.98 respectively.

(larger angular scales) is due primarily to the clustering of DSFGs, with the expected $\text{tSZ} \times \text{CIB}$ anticorrelation also modifying the observed signal in the SPIRE \times SPT bands.

At the SPT frequencies, these bandpowers include power from the CMB, tSZ, and kSZ, radio galaxies and CIB. The situation simplifies toward higher frequencies where the CIB becomes dominant; however, properly modeling the DSFGs of the CIB touches upon a number of open questions about the history of star formation in the universe and what kind of dark matter halos host star-forming galaxies (Planck Collaboration et al. 2014; Mak et al. 2017). Undertaking this modeling effort is beyond the scope of this work; however, we review some of the basics in the Appendix.

3.1. Correlation Coefficients

One question that may be addressed with these data is the degree to which the CIB is correlated across frequencies. We define a correlation coefficient between maps at different

frequencies to be

$$\xi_\ell = \frac{C_\ell^{\nu_1 \times \nu_2'}}{\sqrt{C_\ell^{\nu_1'} \cdot C_\ell^{\nu_2'}}}, \quad (3)$$

which are presented as red circles with black error bars in Figure 2. Note that C_ℓ' here represents “CIB-only” bandpowers—including only the CIB and any tSZ-CIB correlation. Thus the reported correlation coefficient will be sensitive to the magnitude of the tSZ-CIB correlation as well as the actual CIB correlations. Suppressing the other components is necessary because each component will have its own correlation structure. In particular, the CMB is extremely bright on large angular scales in the SPT bands and perfectly correlated across frequencies. Thus, including CMB power would tend to bring the correlation between the SPT bands to unity at low- ℓ . To create these CIB-only bandpowers, we subtract the best-fit values (including calibration factors from that point in the

Table 2
Auto- and Cross-frequency Power Spectra and 1σ Uncertainties ($\text{Jy}^2 \text{sr}^{-1}$)

$\ell_{\min} - \ell_{\max}$	ℓ_{eff}	$C_{\ell}^{95 \times 600}$	$C_{\ell}^{95 \times 857}$	$C_{\ell}^{95 \times 1200}$	$C_{\ell}^{150 \times 600}$	$C_{\ell}^{150 \times 857}$	$C_{\ell}^{150 \times 1200}$	$C_{\ell}^{220 \times 600}$	$C_{\ell}^{220 \times 857}$	$C_{\ell}^{220 \times 1200}$
801–1000	900	913. \pm 472.	1281. \pm 597.	1276. \pm 757.
1001–1200	1100	231. \pm 141.	116. \pm 192.	317. \pm 254.	742. \pm 191.	706. \pm 268.	914. \pm 362.
1201–1400	1300	133. \pm 82.	182. \pm 121.	263. \pm 153.	491. \pm 115.	749. \pm 172.	937. \pm 217.
1401–1600	1500	69. \pm 51.	44. \pm 72.	94. \pm 100.	360. \pm 73.	413. \pm 103.	450. \pm 145.
1601–1800	1700	86. \pm 29.	109. \pm 43.	117. \pm 61.	469. \pm 46.	658. \pm 66.	719. \pm 94.
1801–2000	1900	123. \pm 19.	171. \pm 27.	134. \pm 40.	385. \pm 31.	535. \pm 45.	495. \pm 63.
2001–2200	2100	13.3 \pm 8.5	24. \pm 12.	18. \pm 18.	90. \pm 14.	142. \pm 21.	127. \pm 29.	335. \pm 23.	496. \pm 34.	477. \pm 48.
2201–2500	2350	3.4 \pm 4.7	1.5 \pm 6.9	2. \pm 10.	65.9 \pm 7.6	80. \pm 11.	85. \pm 15.	300. \pm 16.	411. \pm 23.	427. \pm 31.
2501–2800	2650	8.3 \pm 3.8	15.9 \pm 5.6	13.8 \pm 8.0	76.7 \pm 5.3	110.4 \pm 7.8	113. \pm 10.	273. \pm 12.	400. \pm 17.	407. \pm 22.
2801–3100	2950	12.2 \pm 3.0	13.0 \pm 4.8	10.2 \pm 6.8	71.4 \pm 3.7	99.6 \pm 5.5	98.6 \pm 7.7	264.9 \pm 9.3	367. \pm 14.	377. \pm 19.
3101–3500	3300	10.6 \pm 2.7	11.6 \pm 4.1	14.2 \pm 6.0	65.3 \pm 2.6	89.8 \pm 3.9	91.8 \pm 5.3	244.9 \pm 6.8	335. \pm 10.	341. \pm 14.
3501–3900	3700	10.3 \pm 2.3	15.8 \pm 3.6	17.5 \pm 5.3	60.2 \pm 2.1	84.7 \pm 3.2	84.6 \pm 4.7	234.0 \pm 6.2	336.8 \pm 8.8	349. \pm 12.
3901–4400	4150	7.9 \pm 2.1	9.1 \pm 3.1	6.3 \pm 4.7	56.6 \pm 1.9	81.4 \pm 2.7	81.9 \pm 3.8	217.3 \pm 5.2	307.7 \pm 8.0	314. \pm 11.
4401–4900	4650	9.7 \pm 2.1	14.4 \pm 3.1	18.4 \pm 5.0	55.9 \pm 1.6	77.3 \pm 2.4	79.7 \pm 3.4	214.7 \pm 4.6	305.3 \pm 7.1	305.0 \pm 10.0
4901–5500	5200	10.4 \pm 2.0	17.4 \pm 3.1	18.7 \pm 4.7	55.2 \pm 1.4	75.7 \pm 2.0	78.2 \pm 3.0	202.5 \pm 3.9	277.4 \pm 5.7	280.2 \pm 8.5
5501–6200	5849	11.1 \pm 2.0	15.3 \pm 3.1	15.2 \pm 4.6	52.2 \pm 1.2	72.6 \pm 1.8	75.1 \pm 2.8	198.3 \pm 3.3	273.2 \pm 5.0	281.4 \pm 7.4
6201–7000	6599	7.1 \pm 2.2	12.3 \pm 3.3	16.1 \pm 4.9	51.5 \pm 1.2	71.7 \pm 1.8	75.3 \pm 2.6	182.6 \pm 3.2	254.2 \pm 4.9	261.5 \pm 7.1
7001–7800	7399	6.6 \pm 2.5	9.6 \pm 4.0	15.1 \pm 5.9	49.9 \pm 1.2	71.2 \pm 1.7	73.7 \pm 2.6	184.8 \pm 3.4	248.5 \pm 4.9	247.4 \pm 7.3
7801–8800	8299	5.9 \pm 2.7	9.9 \pm 4.1	5.5 \pm 6.2	48.4 \pm 1.1	68.1 \pm 1.6	72.1 \pm 2.4	171.4 \pm 3.0	234.2 \pm 4.3	242.8 \pm 6.4
8801–9800	9299	20.1 \pm 3.6	20.9 \pm 5.6	24.7 \pm 8.3	46.4 \pm 1.2	64.6 \pm 1.9	67.5 \pm 2.7	170.8 \pm 3.5	232.4 \pm 5.0	235.4 \pm 7.4
9801–11000	10399	47.9 \pm 1.2	65.5 \pm 1.9	68.9 \pm 2.9	169.0 \pm 3.2	232.7 \pm 4.8	238.3 \pm 6.7

Note. Bandpowers for the SPTxSPIRE frequency bands in units of $\text{Jy}^2 \text{sr}^{-1}$ under the photometric convention $\nu I_{\nu} = \text{constant}$. The reported uncertainties are based on the diagonal of the covariance matrix, and do not include beam or calibration uncertainties.

Table 3
Auto- and Cross-frequency Power Spectra and 1σ Uncertainties ($1000 \text{ Jy}^2 \text{ sr}^{-1}$)

$\ell_{\min} - \ell_{\max}$	ℓ_{eff}	$C_\ell^{600 \times 600}$	$C_\ell^{600 \times 857}$	$C_\ell^{600 \times 1200}$	$C_\ell^{857 \times 857}$	$C_\ell^{857 \times 1200}$	$C_\ell^{1200 \times 1200}$
601–800	700	18.9 ± 2.4	26.5 ± 3.7	30.8 ± 5.3	39.3 ± 5.4	48.2 ± 7.7	$57. \pm 12.$
801–1000	900	12.4 ± 1.5	19.0 ± 2.1	21.0 ± 3.0	30.4 ± 2.8	34.9 ± 3.9	43.3 ± 5.6
1001–1200	1100	8.88 ± 0.96	13.5 ± 1.4	14.0 ± 2.1	22.8 ± 1.8	25.0 ± 2.5	31.9 ± 3.5
1201–1400	1300	7.44 ± 0.66	12.01 ± 0.92	13.0 ± 1.4	18.9 ± 1.2	22.7 ± 1.7	28.6 ± 2.2
1401–1600	1500	7.03 ± 0.48	10.52 ± 0.67	10.9 ± 1.0	17.45 ± 0.90	19.6 ± 1.3	24.1 ± 1.6
1601–1800	1700	6.42 ± 0.37	9.54 ± 0.57	10.62 ± 0.86	15.55 ± 0.74	18.4 ± 1.0	23.9 ± 1.3
1801–2000	1900	6.12 ± 0.30	9.11 ± 0.43	10.03 ± 0.62	14.31 ± 0.57	16.55 ± 0.74	21.05 ± 0.97
2001–2200	2100	5.22 ± 0.23	7.89 ± 0.35	8.76 ± 0.54	12.72 ± 0.46	14.75 ± 0.63	18.91 ± 0.81
2201–2500	2350	4.67 ± 0.16	6.96 ± 0.26	7.80 ± 0.39	11.20 ± 0.34	13.29 ± 0.46	17.28 ± 0.57
2501–2800	2650	4.57 ± 0.13	6.97 ± 0.20	7.67 ± 0.30	11.22 ± 0.25	13.21 ± 0.35	16.87 ± 0.44
2801–3100	2950	4.27 ± 0.11	6.35 ± 0.17	6.98 ± 0.27	9.91 ± 0.22	11.69 ± 0.33	14.99 ± 0.40
3101–3500	3300	3.797 ± 0.084	5.79 ± 0.13	6.32 ± 0.21	9.32 ± 0.17	10.94 ± 0.25	14.04 ± 0.31
3501–3900	3700	3.717 ± 0.070	5.57 ± 0.12	6.14 ± 0.18	8.88 ± 0.14	10.59 ± 0.22	13.77 ± 0.26
3901–4400	4150	3.509 ± 0.055	5.375 ± 0.099	5.91 ± 0.16	8.72 ± 0.13	10.29 ± 0.19	13.31 ± 0.23
4401–4900	4650	3.428 ± 0.052	5.175 ± 0.087	5.72 ± 0.15	8.30 ± 0.11	9.86 ± 0.18	12.80 ± 0.22
4901–5500	5200	3.267 ± 0.044	4.898 ± 0.081	5.42 ± 0.13	7.82 ± 0.10	9.33 ± 0.16	12.18 ± 0.19
5501–6200	5849	3.103 ± 0.039	4.681 ± 0.074	5.19 ± 0.13	7.460 ± 0.093	8.90 ± 0.16	11.68 ± 0.19
6201–7000	6599	3.030 ± 0.035	4.576 ± 0.061	5.09 ± 0.11	7.350 ± 0.076	8.82 ± 0.13	11.59 ± 0.15
7001–7800	7399	2.963 ± 0.033	4.485 ± 0.060	4.97 ± 0.11	7.290 ± 0.075	8.66 ± 0.13	11.36 ± 0.16
7801–8800	8299	2.836 ± 0.030	4.274 ± 0.057	4.74 ± 0.11	6.914 ± 0.068	8.28 ± 0.12	10.91 ± 0.14
8801–9800	9299	2.796 ± 0.028	4.182 ± 0.056	4.64 ± 0.10	6.650 ± 0.066	8.00 ± 0.12	10.56 ± 0.14
9801–11000	10399	2.690 ± 0.027	4.079 ± 0.054	4.51 ± 0.11	6.583 ± 0.063	7.89 ± 0.11	10.43 ± 0.14

Note. Bandpowers for the SPIRE frequency bands in units of $(1000 \text{ Jy}^2 \text{ sr}^{-1})$ under the photometric convention $\nu I_\nu = \text{constant}$. The reported uncertainties are based on the diagonal of the covariance matrix, and do not include beam or calibration uncertainties.

chain) from G15 for the power from the CMB, tSZ, kSZ, radio galaxies, and galactic cirrus from the measured bandpowers.

Figure 2 shows the resulting correlation coefficients as a function of multipole. The observed correlations are largely independent of angular scale, although there is a suggestion of a slope in the terms involving 220 GHz and the SPIRE bands. There is a visual hint of a slope in the 95 GHz correlation coefficients as well, which is intriguing as the slope matches the expected direction for an anticorrelation between the tSZ and CIB power (i.e., the tSZ-CIB anticorrelation should reduce the cross-correlation coefficient as defined here around $\ell \sim 3000$). However, we stress that the uncertainties are large and the predicted variations in the G15 model on these scales is small compared to the current error bars. In the SPIRE-only maps, correlation coefficients are effectively independent of angular scale. The measured correlation coefficients, averaged across $\ell \in [2000, 7000]$, are reported in Table 2. For the SPIRE bands, we find correlation values of $\langle \xi \rangle = 0.970 \pm 0.010$, 0.861 ± 0.012 , 0.9551 ± 0.0099 for 600×857 , 600×1200 , and 857×1200 GHz, respectively. These values agree with those found by Viero et al. (2013a). We report the average correlation between all frequency pairs in Table 4.

Our expectation is that the CIB should be highly correlated in neighboring frequency bands, with the correlation dropping as the frequency separation increases. Even if all DSFGs had identical SEDs in their local restframe, their observed SEDs would peak at different frequencies based on their individual redshifts. Effectively different frequency bands are weighted toward DSFGs at different redshifts. As the frequency separation increases, there is less overlap in which DSFGs are contributing to each band’s power spectrum and more decorrelation. Variations in the restframe SED will also add to the decorrelation. We can measure this decoherence in the data, as shown in Figure 3. In this plot, the average (from $\ell = 2000$

to 7000) cross-correlation coefficients are shown for each of the 15 unique frequency pairs. The colored symbol encodes the lower frequency in the pair, e.g., open purple circles for the five pairs involving the 95 GHz band and an open red triangle for the last pair between 857 and 1200 GHz. The x -axis encodes the logarithmic frequency difference between the two bands in the pair. An overly simplistic model for the decoherence is simply assuming each galaxy has a different β for its modified blackbody, drawn from a Normal distribution with some variance σ^2 . The correlation factors are insensitive to T and β , so we fix these parameters to $T = 18 \text{ K}$ and $\beta = 2.0$. We conduct a fit to this toy model, and find $\sigma^2 = 0.277 \pm 0.009$ (or $\sigma = 0.53$). The quoted error on σ^2 is based on the change that increases the χ^2 by one; this is likely to be optimistic given the poor overall fit (the best-fit $\chi^2 = 109$). The dotted line in Figure 3 shows the predictions for the best-fit to this toy model. The data are qualitatively consistent with the degree of correlation depending only on the ratio of the frequencies, as would be expected for variations in the power-law spectral index between DSFGs. We stress that one should be very cautious in interpreting the toy model physically—the toy model does not include a DSFG redshift distribution and vacuums up the effects of different redshifts into variations in β .

We can compare the measured cross-correlation coefficients to the predictions of the CIB modeling work in Béthermin et al. (2013). Table 1 in that work presents predicted correlation coefficients for the clustering component at $\ell = 1000$ and the Poisson component at higher multipoles; the measurement in this work across $\ell = 2000$ to 7000 should fall in between the two. There is also the caveat that the predictions are for frequencies close (but not identical) to the actual band centers. The agreement is reasonable at a qualitative level (a careful statistical comparison is difficult given the caveats). We

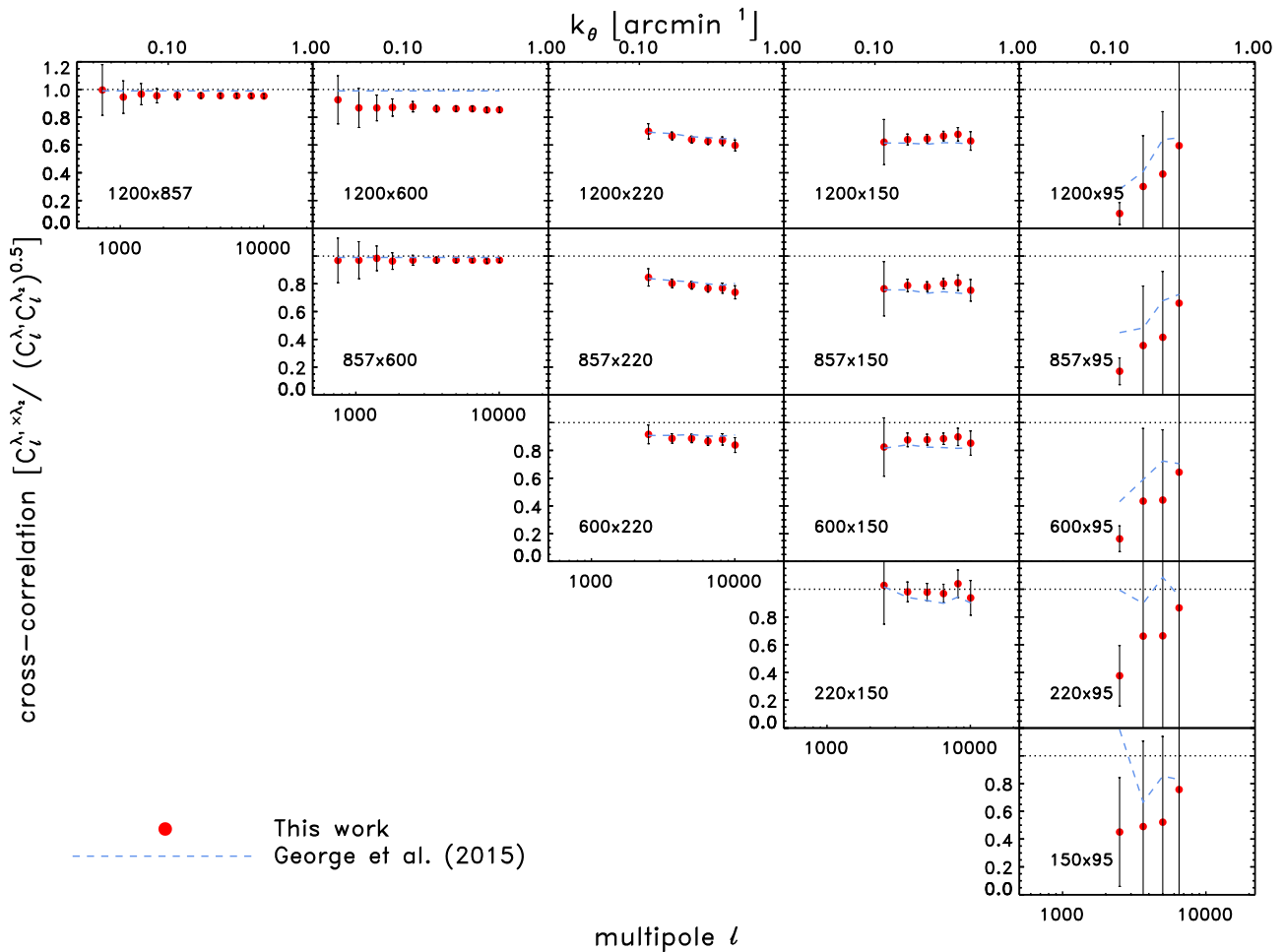


Figure 2. Correlation levels between bands for the “CIB-only” spectra (see Section 3.1 for details). Dotted lines represent unity, or what would be expected for two identical maps. For spectra including SPT bands, we also show (with a dashed blue line) the correlation predicted by the best-fit model in the baseline analysis of G15. The agreement is excellent at the SPT frequencies with the exception of the largest angular scales at 95 GHz. Recall that this work uses only $\sim 100 \text{ deg}^2$ of the 2500 deg^2 analyzed by G15. The agreement is also poor for the SPIRE-only frequencies because the simplified CIB model in G15 has no variation between galaxy SEDs across the DSFG population. This simplified model clearly breaks down in the high S/N measurement of CIB power from SPIRE.

measure a correlation from 600 to 857 GHz (recall the effective CIB band centers are 546 and 796 GHz) of 0.970 ± 0.010 . Béthermin et al. (2013) predict the correlation between 545 and 857 GHz to be 0.916 (Poisson) to 0.971 ($\ell = 1000$). The prediction for 220–857 GHz is 0.785 (Poisson) to 0.902 ($\ell = 1000$); the actual observed correlation is 0.786 ± 0.016 . The prediction for 100–857 GHz is 0.743 (Poisson) to 0.919 ($\ell = 1000$); the actual observed correlation is 0.40 ± 0.32 . There is a suggestion, especially in the 95 GHz band, that the observed correlations are lower than predicted; however, the significance is low at the current level of uncertainty. A low value would not necessarily point to a flaw in the CIB modeling either, because the model did not include the expected anticorrelation of the tSZ and CIB. The anticorrelation of the tSZ and CIB is most significant in the cross-frequency spectra including 95 GHz. We conclude that the observed correlations are in rough agreement with the predicted correlations of the Béthermin et al. (2013) CIB model.

3.2. Comparison to Previous Measurements

It is interesting to compare the spectra from this work with other CIB studies. Figure 1 shows other recent measurements along with the SPIRE \times SPT bandpowers. CIB measurements

from SPIRE (Viero et al. 2013a, blue diamonds from 600 to 1200 GHz) and *Planck* (green squares from 600 to 857 GHz Planck Collaboration et al. 2014) are in excellent agreement. Note that we have scaled the *Planck* bandpowers at 660 and 857 GHz to account for differences in the passbands of SPIRE and *Planck*.

For the CIB \times CMB measurements, we show measurements from BLAST \times ACT (orange crosses over 150–220 \times 600–1200 GHz; Hajian et al. 2012), and again from *Planck* (green squares over 150–220 \times 600–857 GHz). The different data sets are in excellent agreement. As before, *Planck* values are adjusted to account for passband differences. It is notable how the SPIRE \times SPT and *Planck* spectra complement each other, with the two data sets overlapping at $\ell \sim 2000$. This is because the *Planck* points are limited on smaller angular scales by the $\sim 5'$ beam, while the SPIRE \times SPT points are limited on larger scales by the presence of CMB in the SPT maps—which acts as a noise term and, unlike in the *Planck* measurements, is not subtracted. The extra variance due to the CMB can be substantially larger than the expected CMB power in the SPIRE \times SPT cross-spectrum because the variance includes terms proportional to the SPT \times SPT auto-spectrum (which is dominated by the CMB). For instance, the variance of the 1200 \times 150 GHz cross-spectrum has terms proportional to,

Table 4
Mean Correlation Coefficients between Each Frequency Pair

	95 GHz	150 GHz	220 GHz	600 GHz	857 GHz	1200 GHz
95 GHz	1	0.53 ± 0.43	0.68 ± 0.55	0.46 ± 0.36	0.40 ± 0.32	0.36 ± 0.28
150 GHz	...	1	0.976 ± 0.039	0.879 ± 0.025	0.789 ± 0.022	0.650 ± 0.020
220 GHz	1	0.879 ± 0.018	0.786 ± 0.016	0.643 ± 0.014
600 GHz	1	0.970 ± 0.010	0.861 ± 0.012
857 GHz	1	0.9551 ± 0.0099
1200 GHz	1

Note. Correlation coefficients from the weighted average of bandpowers on angular scales $\ell \in [2000, 7000]$. Except for 220 GHz, the correlation is consistent with being independent of angular scale. Unsurprisingly, the correlation decreases for frequency bands that are farther apart.

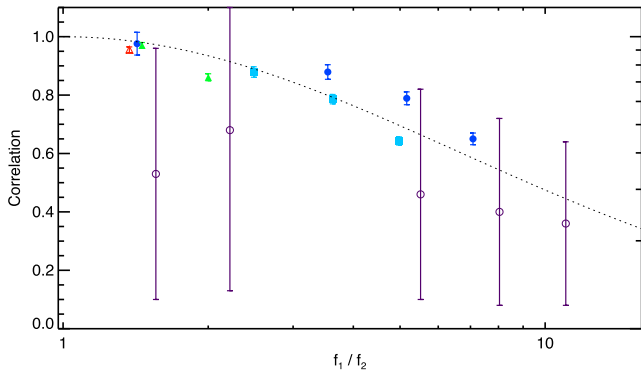


Figure 3. Measured correlation between bands declines quickly as the frequency separation increases. The plot shows the correlation coefficients, as defined in Equation (3), averaged across $\ell \in [2000, 7000]$ as a function of ratio of the frequency for each band. The dotted line shows a toy model prediction for this correlation if the β in the modified blackbody for each CIB galaxy is drawn from a Normal distribution with $\sigma = 0.53$. While the toy model is a poor fit to the measured correlation coefficients ($\chi^2 = 109$ for 14 d.o.f.), it does capture the qualitative behavior of the correlation coefficient. Frequency pairs where the lower frequency band is 95 GHz are marked by open purple circles, 150 GHz by filled blue circles, 220 GHz by filled turquoise squares, 600 GHz by filled green triangles, and 857 GHz by an open red triangle.

$C_\ell^{150 \times 150} C_\ell^{1200 \times 1200} + (C_\ell^{150 \times 1200})^2$, and the CMB is extremely bright in $C_\ell^{150 \times 150}$ despite being negligible in the other terms. The magnitude of this extra variance due to the CMB is shown by a red dashed line.

4. Conclusion

We have presented high-angular-resolution temperature power spectra from a cross-frequency power spectrum analysis of an approximately 100 deg² field observed with *Herschel*/SPIRE and the SPT. We show for the first time the cross-frequency spectra between the CIB (at 600, 857, and 1200 GHz; or 500, 350, and 250 μ m) and maps at 95 GHz (3.2 mm). These cross-spectra show the qualitative behavior predicted for the expected anticorrelation between the CIB and tSZ signals. From $2000 < \ell < 11,000$, the reported bandpowers also dramatically improve upon earlier measurements of the cross-spectra between the CIB and maps near the peak of the CMB at 150 and 220 GHz. The measurements at $\ell < 2000$ are consistent with earlier *Planck* results.

We also measure the observed correlation between the CIB maps across this 12-fold frequency range (from 95 to 1200 GHz). Decorrelation between frequency bands is expected to be introduced by differences in the SED from one DSFG to another. This model predicts a high degree of correlation for nearby bands, dropping toward zero with increasing frequency

separation. The observed correlations are largely consistent with this picture.

The bandpowers, covariance matrix and bandpower window functions from this work are publicly available (see footnote 45). The data presented here may be of interest to testing halo-occupation models for the CIB, for probing the correlation between galaxy clusters and the DSFGs, and for putting limits on the epoch of reionization through the kSZ effect.

The SPT-3G survey began taking data in 2017. With roughly 10-fold more detectors than SPT-SZ and equal detector counts at 95, 150, and 220 GHz, SPT-3G has embarked upon a 1500 deg² survey (including this field) that will have significantly lower noise levels than the SPT-SZ survey. These data can be used to make further improvements on our modeling of the CIB and tSZ-CIB correlations.

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Appendix Signals in the Maps

Anisotropy in the cosmic microwave and infrared backgrounds can be introduced by primordial fluctuations, emission from DSFGs and radio galaxies, the kinematic and thermal SZ effects, and contamination from Galactic foregrounds. The power spectrum at a given wavelength can be written as:

$$C_\ell^{\text{Tot}} = C_\ell^{\text{CMB}} + C_\ell^{\text{CIB}} + C_\ell^{\text{radio}} + C_\ell^{\text{tSZ-CIB}} + C_\ell^{\text{tSZ}} + C_\ell^{\text{kSZ}} + C_\ell^{\text{cirrus}} \quad (4)$$

where C_ℓ is the angular power spectrum at multipole ℓ .⁴⁶

Relative to the CMB, the CIB and Galactic cirrus power rises toward higher frequencies, while the radio galaxy and tSZ power is more significant at lower frequencies. Wavelengths longer than roughly $500 \mu\text{m}$ are more sensitive to higher-redshift DSFGs (for a review, see Casey et al. 2014). Cross-spectra between frequency bands provide additional information about how the signals are correlated between bands, and allow one to disentangle signals that might otherwise be degenerate with one another. As a practical matter, only the CIB (from DSFGs) and cirrus terms are significant at the SPIRE frequency bands.

A.1. Galactic Foreground Terms

Diffuse Galactic cirrus introduces a foreground signal on large scales to the extragalactic submillimeter/millimeter-wave power spectrum. Other Galactic foregrounds such as synchrotron and free-free emission are negligible in the area of the sky and frequencies considered here and thus are ignored.

Galactic cirrus can be approximated as a power law

$$C_\ell^{\text{cirrus}} = P_{0,\lambda} \left(\frac{\ell}{\ell_0} \right)^{\alpha_c}, \quad (5)$$

with the amplitude $P_{0,\lambda}$ dependent on the observing frequency λ , and the index α_c independent of observing frequency (e.g., Gautier et al. 1992; Miville-Deschênes et al. 2007). In the first studies of high Galactic latitude cirrus, the index had been found to have a value of around -3.0 (e.g., Gautier et al. 1992); however, more recent measurements have found that both the amplitude and index are quite direction-dependent, with values for α_c ranging from -1 to -4 (e.g., Roy et al. 2010; Boothroyd et al. 2011; Bracco et al. 2011).

We also need to consider the spectral dependence of the Galactic cirrus. At submillimeter/millimeter wavelengths, cirrus emission follows a modified blackbody, $\nu^{\beta_c} B_{T_{\text{eff},c}}(\nu)$. Here $B_{T_{\text{eff},c}}(\nu)$ is the Planck function for temperature $T_{\text{eff},c}$ and β_c is the emissivity index (Draine & Lee 1984). Past studies have found $T_{\text{eff},c} = 16\text{--}20 \text{ K}$ and $\beta_c \approx 1.8$ (e.g., Bracco et al. 2011).

⁴⁶ In some studies the angular power spectrum is expressed as a function of the angular wavenumber, k , which is related to multipole number ℓ as $\ell = 2\pi k$.

A.2. Cosmic Infrared Background (CIB)

The CIB power term in Equation (4) is sourced by DSFGs and can be further split into Poisson and clustering components. The Poisson (or shot noise) term results from the discrete sampling of dusty galaxies. The power spectrum of the Poisson term is independent of angular scale, with amplitude

$$C_\ell^{\text{Poisson}} = \int_0^{S_{\text{cut}}} S_\nu^2 \frac{dN}{dS_\nu}(S_\nu) dS_\nu, \quad (6)$$

where dN/dS_ν is the distribution of flux densities of sources, and S_{cut} is the level at which sources with greater flux densities are masked.

The clustering term arises from overdensities in the background that trace the dark matter distribution. It can be described with a ‘‘halo model’’ approximation (e.g., Seljak et al. 2001), which consists of a linear (or two-halo) term on large scales ($\ell \lesssim 3500$ for the frequency bands in this work) and nonlinear (or one-halo) term on small scales ($\ell \gtrsim 3500$). The linear term is simply the dark matter power spectrum multiplied by an effective bias (e.g., Kaiser 1984). The nonlinear term is more subtle, as the bias can be both scale- and mass-dependent largely because galaxy properties (stellar masses, star formation rates, bolometric luminosities, etc.) are tied to those of their host dark matter halos (halo mass, concentration, etc.; e.g., Shang et al. 2012; Viero et al. 2013a).

A.3. Radio Galaxies

Radio galaxies also contribute to the Poisson term detailed in Equation (6). After masking sources above 6.4 mJy at 150 GHz (see Section 2.3.1), dusty galaxies are the dominant contributors to the Poisson term in all but the 95 GHz band. At 95 GHz , $80\text{--}90\%$ of the power is expected to be due to radio galaxies. As argued by G15 and others, we do not expect a detectable clustering term for the radio galaxies.

A.4. The Thermal Sunyaev–Zel’dovich (tSZ) Effect and tSZ-CIB Correlations

The galaxy clusters that give rise to the tSZ power spectrum similarly trace the dark matter distribution. Accurately modeling the tSZ power spectrum is challenging because of the complicated astrophysics affecting the intracluster medium in galaxy clusters; for instance, nonthermal pressure support due to merger shocks. Different prescriptions for the astrophysics can change the predicted power for a given cosmology by up to 50% (e.g., Battaglia et al. 2010, 2012; Shaw et al. 2010; Trac et al. 2011; Efstathiou & Migliaccio 2012).

Additionally, since both galaxies and clusters trace the same dark matter, correlations between the two populations reveal insights into their relationship. The first to demonstrate the power of this relationship was Addison et al. (2012), who showed that the strength and shape of the cross-correlation spectrum—which, again, appears as a negative signal—is largely influenced by the HOD of star-forming galaxies in the most massive dark matter halos. Furthermore, they show that, since shorter wavelengths favor lower redshifts, the strength of the effective anticorrelation is highest between $250 \mu\text{m}$ and CMB channels. The bandpowers reported in this work can be used to improve measurements of the tSZ-CIB correlation.

A.5. The Kinematic Sunyaev–Zel’dovich (kSZ) Effect

The bulk motion of electrons can impart a Doppler shift upon scattered photons, an effect known as the kSZ effect (Sunyaev & Zel’dovich 1970, 1980). The amplitude of the kSZ signal from a given volume scales as $(v/c) \delta_e$, where c is the speed of light and δ_e is the overdensity of free electrons. As a result, significant kSZ power is sourced during the epoch of reionization (when velocities and mass overdensities are small, but there is a high contrast in the free electron density between ionized and neutral regions) and at late times ($z < 2$, when velocities and mass overdensities have grown larger). We expect current models for the post-reionization kSZ power spectrum to be more accurate than tSZ models because, unlike the tSZ, the kSZ signal is not weighted by gas temperature. Thus, the kSZ spectrum is less dependent on the nonlinear physics in dense halos. However, the kSZ power from reionization is highly uncertain, and offers a unique window into how reionization occurred (Mortonson & Hu 2010; Mesinger et al. 2012; Zahn et al. 2012; George et al. 2015).

A.6. Cosmic Microwave Background (CMB)

Finally, the CMB is present in all of these maps. At SPIRE frequencies, the CMB is much fainter than the CIB and largely neglectable, but below 280 GHz the CMB quickly overwhelms the CIB at large angular scales. Although the two backgrounds are uncorrelated (lensing notwithstanding, e.g., Holder et al. 2013), CMB sample variance introduces a large noise signal to the cross-correlations between SPT and SPIRE frequency bands, and washes out the CIB cross-correlation signal (e.g., Hajian et al. 2012, Appendix B). The Planck Collaboration et al. (2014) overcame this limitation by subtracting the CMB directly from their maps, which they did by using their 100 GHz map as a template and scaling the signal as a perfect 2.73 K blackbody. The drawback of this technique is that cross-frequency correlation measurements with 100 GHz cannot be made—a measurement that arguably contains the most novel information for the tSZ-CIB correlation.

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