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**Title:**

Defining the fire trap: Extension of the persistence equilibrium model in mesic savannas

**Date:**

2017-12-01

**Citation:**

Freeman, M. E., Vesk, P. A., Murphy, B. P., Cook, G. D., Richards, A. E. & Williams, R. J. (2017). Defining the fire trap: Extension of the persistence equilibrium model in mesic savannas. *Austral Ecology*, 42 (8), pp.890-899. <https://doi.org/10.1111/aec.12516>.

**Persistent Link:**

<https://hdl.handle.net/11343/216907>

1 **Running Head:** Savanna fire trap persistence and escape

2 **Defining the fire trap: extension of the persistence equilibrium model**  
3 **in mesic savannas**

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14 **Abstract**

15           Mesic savannas are dominated by trees that are strong resprouters caught in a frequent  
16 fire trap. Persistence within this fire trap has been described by a resprout curve of  $\text{SizeNext}$   
17  $\sim f(\text{Pre-fire size})$ , defined by the Michaelis-Menten function. A key feature of this resprout  
18 curve is a stable persistence equilibrium that represents the size of individual plants upon  
19 which a population will converge over successive inter-fire time steps under a given fire  
20 regime. Here, we contend that such a resprout curve does not adequately describe resprout  
21 tree dynamics in frequently burnt mesic savannas because it is constrained to an asymptote.  
22 We propose a new framework for modelling the resprout curve, which recognises that local  
23 environmental stochasticity and growth patterns can interact to change the growth response  
24 function entirely, and thus more readily reflect the range of feasible resprout responses.  
25 Importantly, we define an unstable equilibrium representing the size above which individuals  
26 have escaped the fire trap. Further, we explore mechanisms that can shift an individual from  
27 persistence to escape. Through a case study from northern Australia, we confirm that our  
28 framework provides a simple yet practical approach to defining these critical aspects of  
29 savanna tree growth dynamics: persistence and escape.

30 **Keywords**

31 demographic bottleneck; fire trap; persistence niche; resprouting; savanna

32 **Introduction**

33           Topkill by fire in small tree size classes ( $\sim < 5\text{cm}$  diameter at breast height (DBH)) is a  
34 predominant feature of woody dynamics in mesic savannas. Frequent fire can trap these small  
35 trees in a cycle of above-ground biomass loss followed by resprouting, which results in a  
36 demographic bottleneck limiting transition to the canopy (Hoffmann 1998, Higgins et al.  
37 2000, Bond 2008, Prior et al. 2010, Bond et al. 2012, Werner and Prior 2013). This

38 phenomenon necessitates that tree species are strong resprouters able to persist in the shrub  
39 layer, potentially for decades (Bellingham and Sparrow 2000, Bond and Midgley 2001,  
40 Higgins et al. 2007). As such, frequent fire maintains a tree community height structure that  
41 is broadly bimodal, with abundant multi-stemmed resprouts, very few saplings, and canopy  
42 tree density maintained below the site potential (Sankaran et al. 2005, Higgins et al. 2007,  
43 Bond 2008, Lehmann et al. 2009, Holdo et al. 2014). Surprisingly, despite significant interest  
44 in consequences of the demographic bottleneck on stand structure and tree species dominance  
45 (Williams et al. 1999, Ryan and Williams 2011, Bond et al. 2012, Hoffmann et al. 2012),  
46 conceptual models that describe persistence in, and escape from, the fire trap remain ill-  
47 defined.

48 Grady and Hoffmann (2012) proposed a stable size ‘persistence equilibrium model’  
49 that describes resprout population persistence within the fire trap. It is defined by a ‘resprout  
50 curve’ of size in successive inter-fire time steps and features an ‘equilibrial size’; an  
51 expression of the resprout persistence niche (Bond and Midgley 2001) at a given site and fire  
52 regime. This persistence model provides a basis from which to explore resprout growth  
53 dynamics as mediated by size of individuals, disturbance and environmental conditions. Here,  
54 ‘resprout’ refers primarily to trees <1.5m tall, but does also include all small trees up to 5cm  
55 DBH (i.e. saplings). However, in its current form the Grady and Hoffmann (2012) model  
56 does not accommodate one of the most critical aspects of savanna dynamics: escape from the  
57 fire trap. Specifically, it is constrained to an asymptotic height by the Michaelis-Menten  
58 function meaning, from a model perspective, individuals can never advance beyond a  
59 persistence equilibrium. But, for canopy trees to exist in savannas, some individuals must  
60 escape.

61 Here, we extend the Grady and Hoffmann (2012) persistence model to reflect the  
62 range of resprout responses feasible in savannas under different fire scenarios or species life-

63 history strategies. We propose that species characteristics, length of fire interval, fire season  
64 and growing conditions will not only result in a shift in stable “persistence equilibrium” size,  
65 as was found by Grady and Hoffmann (2012), but can alter the response function entirely.  
66 This framework uses a data-driven approach to define the limits of the fire trap and identify  
67 mechanisms that lead to persistence or escape. We begin with an exploration of theoretical  
68 growth response models and then illustrate use of the framework through a case study from  
69 three fire experiments in northern Australia.

## 70 **Beyond the Stable Size Equilibrium**

71 The topkill-resprout cycle and environmental conditions, such as dry-season water  
72 stress, can lead to positive, negative or zero net individual growth increments within an inter-  
73 fire period (Prior and Eamus 2000, Hoffmann and Solbrig 2003, Murphy et al. 2015). In the  
74 persistence model (Grady and Hoffmann 2012), resprouts that are smaller than the  
75 equilibrium size before a fire will on average increase in size by the end of the inter-fire  
76 period, but those that are larger will decrease because there is insufficient time or resources to  
77 recover their pre-fire size (**Error! Reference source not found.**; A). This relationship  
78 between an individuals’ pre-fire size and size before the next fire (SizeNext) remains  
79 consistent, regardless of whether the measure is diameter, height or total biomass (Grady and  
80 Hoffmann 2012, Schafer and Just 2014).

81 The persistence response curve represents species that are strong resprouters  
82 suppressed to the shrub layer in perpetuity by frequent fire. If this were the only possible  
83 growth trajectory, the system would eventually shift away from a wooded savanna toward a  
84 (grassy) shrubland as canopy trees die.

85 For a savanna to exist, some resprouts must pass through a ‘window of opportunity’  
86 (Balke et al. 2014) (see below) that allows their periodic transition out of the fire trap at a  
87 sufficient rate to retain a level of canopy cover (Jeltsch et al. 2000). Accordingly, a model of

88 escape includes a stable persistence equilibrium and an unstable equilibrium, above which the  
89 individual is resistant to topkill by fire (**Error! Reference source not found.**; B).

90 Grady and Hoffmann (2012) allude to such an extension of their model. They offer  
91 that eucalypts are able to escape because their persistence size (stable equilibrium) is very  
92 close to their escape size (unstable equilibrium), requiring only a minor shift in conditions to  
93 move an individual from persisting in the fire trap to escaping the fire trap. This may be one  
94 pathway to escape, however it is not a prerequisite. For example, Fensham and Bowman  
95 (1992) found remarkable height growth of eucalypt resprouts with overstorey removal. With  
96 such growth rates being possible, the difference between persistence and escape heights may  
97 not need to be small, but could be in the range of meters.

98 Two other possible resprout curve forms describe populations that are not limited by  
99 fire; where pre-fire size is always exceeded by SizeNext (Figure 1, C), and, conversely,  
100 populations where pre-fire size is never recovered; where individuals embark on a “death  
101 spiral” (Grady and Hoffmann 2012) (**Error! Reference source not found.**, D).

102 In all our theoretical models, we purposefully do not express response curves  
103 originating at zero. By doing so, we introduce another unstable equilibrium that represents  
104 the size below which persistence is not viable, i.e. a mortality size threshold.

### 105 **Shifting between Persistence and Escape**

106 On average, size recovery of individuals following fire converges on the stable  
107 persistence equilibrium but diverges from the unstable equilibria (mortality and escape sizes).  
108 This means that occasional bursts of size growth or shrinkage, mediated by a temporary  
109 change in conditions (“window of opportunity” sensu Balke et al. (2014)), must occur if  
110 resprouts are to pass the unstable equilibria to escape or die. Factors creating a window of  
111 opportunity to escape in savannas may include top-down mechanisms, such as milder or  
112 patchier fires (Werner and Franklin 2010, Werner and Prior 2013), and browsing removal

113 (Staver and Bond 2014); bottom-up mechanisms such as release from competition (Fensham  
114 and Bowman 1992) and efficient resource allocation strategies (Schutz et al. 2009); or a  
115 combination of these. The opposite may tip an individual below the lower unstable  
116 equilibrium to mortality.

117         The scale of the window of opportunity required to catalyse an individuals' shift from  
118 persistence at the stable size, to escape (or mortality) will depend on species' ecology and site  
119 resources (Balke et al. 2014). At the population level, as a window of opportunity closes, the  
120 resprout curve may revert from escape to persistence-only if enough individuals are affected.  
121 Because of this, the escape curve may not always be detected when modelling the average  
122 population response.

123         Escape size is important to estimate because it represents the ceiling to the fire trap  
124 and therefore has implications for the effects of fire on stand structure. In populations for  
125 which we observe the persistence resprout curve, an escape size is not visually evident, but  
126 this does not mean it does not exist. In these cases, the size range within which the 'true'  
127 value of escape size lies is delimited by the upper bound of uncertainty (prediction interval)  
128 around the persistence equilibrium and the maximum potential size of individuals (Figure 2).  
129 This maximum size (eg. canopy height) represents another stable equilibrium upon which  
130 populations will converge once individuals have escaped. We use the prediction interval in  
131 this framework because it encompasses individual-level variation, and is thus wider and more  
132 reflective of the range of growth responses likely to be observed than the confidence interval,  
133 which represents uncertainty around the population mean.

#### 134 **Applying the framework**

135         Application of our framework to data depends on the inclusion of non-topkilled  
136 individuals for identifying escape size – the size at which a tree is no longer suppressed by  
137 fire. If all individuals are topkilled, we would expect to only detect the persistence curve, as

138 in Grady and Hoffmann (2012). In existing field-collected datasets the level of detail that  
139 differentiates trees that were not topkilled because they were large enough to withstand  
140 burning compared to trees that were not topkilled because they were not directly impacted by  
141 fire is often not available. This doesn't impact the utility of the framework, but should be  
142 acknowledged when interpreting results. If data consists of both locally burnt and unburnt  
143 (due to fire patchiness) individuals, the resprout curve will be more uncertain. Ideally, if the  
144 detail is available, a best-estimate of persistence and escape size would be obtained by  
145 applying the framework only to burnt individuals.

146 Another feature of the framework is that it can be applied to any level of fire  
147 frequency. The critical aspect is that size is measured immediately before fire and sizeNext  
148 immediately before the next fire. If applying the framework to combined data from various  
149 sources, the length of time between size and sizeNext censuses must be consistent.

150 Accounting for fire history before the collection of census data is not a feature of our  
151 framework given that longevity of savanna resprouts in the shrub layer (Bond and Midgley  
152 2001, Higgins et al. 2007) will generally preclude any ability to determine an individual's  
153 pre-census history. It's also unlikely that an understanding of fire history could resolve all  
154 observed individual-level variation. Again, such individual-level variation is accounted for in  
155 uncertainty around the resprout curve. Depending on the aim of the researcher, the data used  
156 to infer persistence and escape size could be highly localised, giving precise estimates for a  
157 given environment, or could combine datasets to yield a more accurate landscape average.

## 158 **Case Studies**

159 To demonstrate use of this framework we undertook graphical analysis of data from  
160 three fire response studies in mesic savannas of the Northern Territory of Australia. One  
161 dataset was drawn from the Kapalga fire experiment (Andersen et al. 2003, Andersen et al.  
162 2005, Williams et al. 1999), another from an independent study of sub-adult trees in Kapalga

163 (Werner and Prior 2013) and third from recent work in experimental fire plots on the Tiwi  
164 Islands (Richards et al. 2012). Data collection methods for each dataset are included in  
165 Appendix S1 of the Supporting Information, and, for the Kapalga data, in the original studies  
166 (Williams et al. 1999, Prior et al. 2010, Werner and Prior 2013, Werner 2012). All study  
167 areas are dominated by mesic eucalypt (*Eucalyptus* and *Corymbia* spp.) savanna  
168 characterised by highly seasonal rainfall, occurring almost entirely over the six month wet  
169 season; roughly November to April. Sub-dominant trees include a range of predominantly  
170 deciduous non-eucalypt species of pantropical affiliation, which are more likely to become  
171 caught in the frequent fire trap (Prior et al. 2010, Bond et al. 2012), and more negatively  
172 impacted by increased fire frequency and intensity, than the canopy-dominant eucalypts  
173 (Williams et al. 1999, Russell-Smith et al. 2003, Murphy et al. 2015, Scott et al. 2012).

174 Datasets were filtered to only include species that have the potential to become trees,  
175 which we defined as woody dicotyledons at least 6 m in height. Only the top three most  
176 common eucalypt and non-eucalypt species (across all datasets) were used in our case study  
177 (Table 1). Fire treatments and species counts for each dataset are summarised in Appendix  
178 S1. Treatments included in the case study were early dry season fires (EDS, applied in June  
179 or July) and late dry season fires (LDS, applied in November). Due to higher fuel loads and  
180 increased Forest Fire Danger Index (FFDI), LDS fires are usually more intense with more  
181 complete fuel combustion than EDS fires (Cook and Corbett 2003, Williams et al. 2003,  
182 Russell-Smith and Edwards 2006), providing a greater challenge to escape (Werner and  
183 Franklin 2010, Werner 2012). The window of opportunity to escape under LDS fires is also  
184 presumably much narrower than for EDS fires, not only due to differences in intensity, but  
185 due to lower small-scale patchiness of burns (Werner and Franklin 2010).

186 Each dataset did contain a fire-exclusion treatment, which was not considered here  
187 given our interest in defining the fire trap. Datasets were composed of annual height

188 measurements of tagged individuals, taken at the start of the dry season before burning took  
189 place. Accordingly, HeightNext corresponds to pre-fire height of the following year. New  
190 recruits (pre-fire height = 0) were not included, but otherwise we include all individuals, both  
191 topkilled and not (Table 2). The studies varied in length, as detailed in Appendix S1.

192 Accordingly, the data included in this case study were:

- 193 — “Williams”: dataset of EDS and LDS fire treatments containing trees that were unburnt  
194 for one year before the first census, and then were burnt annually for the next 5 years  
195 resulting in 5 censuses;
- 196 — “Tiwi”: dataset of EDS fire treatment only, containing trees that had experienced 6 years  
197 of annual burning before the 2 annual censuses used here;
- 198 — “Werner”: dataset of EDS and LDS fire treatments containing trees that were unburnt for  
199 one year and then were burnt once resulting in a single one-year census.

200 Resprout curves were modelled by Robust Locally Weighted Least Squares  
201 Regression (LOESS) using the bisquare estimation method in R (R Core Team 2016) using  
202 ggplot. This was done separately for each species, fire treatment and dataset, and repeated for  
203 each species and fire treatment combining all datasets. Each year of data was used, meaning  
204 individuals are represented more than once in both the Williams and Tiwi datasets, which  
205 comprised more than one census (Appendix S1). We used LOESS regression so as not to  
206 restrict the relationship between pre- and post-fire to a functional form that might bias our  
207 evaluation of the response curve, and bisquare estimation to reduce the influence of outliers.  
208 Curves were plotted with 95% confidence intervals.

209 We expected that, under these fire regimes:

- 210 1. eucalypt resprout curves would show evidence of escape and pantropical non-eucalypts  
211 would conform to the persistence resprout curve;
- 212 2. escape resprout curves would be more prevalent in the EDS fire treatment than LDS;

213 3. the difference between persistence height and escape height in the LDS fire treatment  
214 would be greater than EDS.

215 There was generally high agreement between the shapes of resprout curves for each  
216 dataset; therefore here we present single curves combining all datasets. Resprout curves for  
217 each dataset, species and fire treatment are included in Appendix S2 of the Supporting  
218 Information.

### 219 **Case Study Results and Discussion**

220 The most apparent feature of the height response field data is large individual-level  
221 variability across all size classes. Relatively minimal curvature of most resprout curves is due  
222 to almost equal numbers of individuals regressing towards the stable equilibrium and  
223 advancing in size towards escape. The individuals within each dataset had experienced  
224 different pre-census fire regimes and also different within-census fire effects, with un-  
225 accounted-for variation in local patchiness and fire intensity. Further, we did not delimit the  
226 datasets to include only individuals that were burnt by fire. Our model fits truly are  
227 population “averages”, encompassing the full range of individual, site and geographic effects  
228 that may cause individual-level variation in height response. The result of this is that our  
229 resprout curves provide conservative estimates of persistence and escape under two different  
230 seasons of fire.

231 Despite these ‘subtle’ population mean resprout curves, we can discern different curve  
232 shapes corresponding to our proposed forms and equilibrium heights at which individuals are  
233 more likely to persist or escape (Figures 3 and 4).

234 The escape curve is apparent in the three eucalypts; *Corymbia nesophila* (EDS: Figure  
235 3A and LDS: Figure 3B), *Eucalyptus miniata* (EDS: Figure 3C) and *Eucalyptus tetradonta*  
236 (LDS: Figure 3F); as well as in *Erythrophleum chlorostachys* (EDS: Figure 4A, and LDS:  
237 Figure 4B). In each of these cases, except *E. miniata* EDS, escape height was more than three

238 meters greater than persistence height, indicating the large range of height classes that are  
239 caught within the fire trap. This is contrary to the suggestion that eucalypt persistence sizes  
240 are very close to their escape size (Grady and Hoffmann 2012). *Planchonia careya* (EDS:  
241 Figure 4C and LDS: Figure 4D) and *Terminalia ferdinandiana* (LDS: Figure 4F) exhibit the  
242 persistence curve. In the Williams et al. (1999) dataset, all individuals within a defined  
243 transect were marked and measured. Accordingly, the restriction of *P. careya* LDS to a  
244 discrete cluster of individuals below 1 m is evidence that the population had already  
245 converged on the persistence equilibrium at the outset of the study. In fact, the high density of  
246 datapoints below 2 m height, evident across all species, illustrates the highly left-skewed  
247 resprout/sapling population distributions that result from individuals converging on the  
248 persistence equilibrium. *Eucalyptus miniata* (LDS: Figure 3D), *Eucalyptus tetradonta* (EDS:  
249 Figure 3E) and *Terminalia ferdinandiana* (EDS: Figure 4E) show (weak) curves of constant  
250 growth. Given the proximity of these constant growth curves to the 1:1 line, a conservative  
251 interpretation is that individuals are, on average, able to at least recover their pre-fire height  
252 across this range of resprout/sapling sizes. This was unexpected, given substantial evidence  
253 of the sensitivity of saplings to fire. It is possible that the greater patchiness of EDS fire (both  
254 spatially and in intensity) is responsible for a relatively high proportion of saplings avoiding  
255 deleterious effects of burning and thus retaining their pre-fire height (Table 2).

256         The persistence curve was only evident in the LDS fire treatment of pantropical non-  
257 eucalypts, which conformed to our expectations. Only for *T. ferdinandiana* and *P. careya*  
258 does fire regime shift the response curve from complete recovery across all size classes under  
259 EDS fire to a persistence curve under LDS. Our case study confirms the previously  
260 recognised negative impacts of intense LDS fire on these non-eucalypts. Similarly, the escape  
261 potential of eucalypts under both EDS and LDS fires is substantiated (Bond et al. 2012), as is  
262 that of the non-eucalypt *E. chlorostachys* (Russell-Smith et al. 2003). There is no conclusive

263 evidence that escape height is taller in LDS than in EDS, which we expected to see due to on  
264 average greater scorch heights resulting from higher fire intensity (Williams et al. 2003).  
265 There is also no evidence of any population embarking on a ‘death spiral’ (as per **Error!**  
266 **Reference source not found.**D), which was expected, given the strong persistence potential  
267 of these fire-prone savanna species.

268 Allocation patterns to above and below-ground biomass may be the critical  
269 determinant of whether a species is likely to conform to the persistence model (Tomlinson et  
270 al. 2012, Tomlinson et al. 2013), as in long-leaf pine savanna (Grady and Hoffmann 2012,  
271 Schafer and Just 2014), Brazilian cerrado (Hoffmann and Solbrig 2003) and here, with the  
272 example of the non-eucalypts *T. ferdinandiana* and *P. careya* under LDS. Escape sizes for  
273 these populations lie somewhere between the upper limit of the prediction interval around the  
274 stable persistence equilibrium and maximum potential height of the species (Table 1).  
275 Preferential allocation of carbon to the below-ground bud bank implies a strategy based on  
276 achieving long-term persistence in the shrub layer (Bond and Midgley 2001, Clarke et al.  
277 2013). To some extent, all resprouting individuals in savanna do this, however the difference  
278 between a persistence population and an escape-curve population is that once an individual,  
279 whose life-strategy relies on escape, has accumulated enough resources, it will use these  
280 stores to bolt through a window of opportunity (Wigley et al. 2009, Werner 2012). Such an  
281 escape strategy is particularly exemplified by the eucalypts in this case study.

282  
283 The dynamics around zero height cannot be clearly characterised using these datasets,  
284 which include only established resprouts (not seedlings) and use height as a size measure.  
285 There is no evidence in these data of a height below which mortality is more likely. The  
286 concept of a mortality threshold in this case study can therefore not be evaluated. Further, the  
287 minimum size that a seedling must attain to exceed the mortality equilibrium and become an

288 established resprout is part of a separate process that cannot be resolved here. Size of the  
289 lignotuber or starch reserve, rather than any measure of above-ground biomass, may be a  
290 more consistent predictor of the unstable equilibrium between persistence and mortality  
291 (Fensham and Bowman 1992, Iwasa and Kubo 1997, Canadell and López-Soria 1998)

292 High individual variation in height recovery suggests localised environmental  
293 conditions and factors beyond only fire season significantly influence growth responses  
294 (Clark 2010, Clark et al. 2012). Using data or modelling techniques such as quantile  
295 regression that represent only exceptional individuals (Wakeling et al. 2011), or including  
296 model covariates that describe site-specific or fine-scale patch conditions, may lead to greater  
297 precision in estimates of fire trap limits for specific scenarios. Estimated escape and  
298 persistence heights in our case study reflect the full range of variation that a population may  
299 experience under EDS and LDS fire season regimes. This approach is of interest because it  
300 takes into account the mechanisms that lead to escape (i.e. windows of opportunity) without  
301 explicitly having to define them. If we only modelled topkilled or exceptional individuals, or  
302 a single site, our estimations of persistence and escape would reflect a more homogeneous  
303 population and could not be assumed to apply to an “average” population of that species.

304 Our flexible approach to modelling the resprout curve provides improved capacity to  
305 determine the limits of, and uncertainty around, the fire trap compared to Grady and  
306 Hoffmann (2012). LOESS regression has proven a useful method for exploring responses of  
307 resprout tree populations to fire without the restriction of a particular functional form. A  
308 problem with LOESS, however, is that although it may be used for prediction, it cannot  
309 inform, for example, the growth kernel of an Integral Projection Model (Easterling et al.  
310 2000). If a parametric function is required, we suggest a linear modelling framework with  
311 polynomial terms would approximate response curves best and have the benefit of generality.

312 **Conclusions – Defining the Fire Trap**

313 Estimating persistence and escape sizes is fundamental to predicting the impact of fire  
314 on savanna composition and structure. As we have presented here, visualising tree growth  
315 responses in the context of persistence and escape provides an opportunity to conceptualise  
316 tree population dynamics in highly fire-prone landscapes.

317 Our case study confirmed that a variety of resprout curves are possible beyond the  
318 persistence model proposed by Grady and Hoffmann (2012). Although simple, such a  
319 graphical analysis is a flexible tool for defining the fire trap for different species under  
320 different fire regimes. The approach could be strengthened by incorporating other fire,  
321 competition and environmental covariates for extension to predictive studies of population  
322 dynamics.

323 **Acknowledgements**

324 We thank Dick Williams, Patricia Werner and Lynda Prior for use of their data. We  
325 thanks Patricua Werner and William Hoffmen for critical comments that both sharpened our  
326 understanding and improved the manuscript, even if we did not agree with all. Tiwi data were  
327 collected with invaluable field assistance provided by Jon Schatz, Willy Rioli, Willy Roberts,  
328 Colin Kerinauia, Vivian Kerinauia, José Puruntameri and Kim Brooks. In particular, we  
329 acknowledge the support provided by the Tiwi Land Council and CSIRO TERC in Darwin  
330 and funding provided through the Australian Government Department of Environment. BPM  
331 was supported by a grant from the Australian Research Council (DE130100434). PAV was  
332 supported by The Australian Research Council Centre of Excellence for Environmental  
333 Decisions.

**Commented [PV1]:** Will you still leave this in , now that Dick is an author?

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#### 461 **Supporting Information**

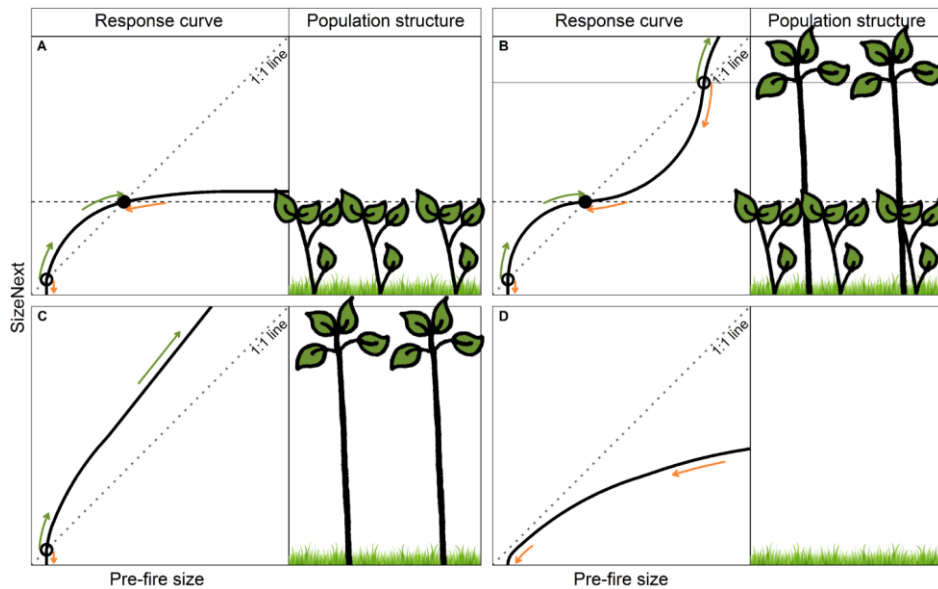
462 Additional Supporting Information may be found in the online version of this article at the  
463 publisher's web-site:

464 **Appendix S1:** Summary of the data used in our case study, including descriptions and  
465 methods of collection of the three datasets.

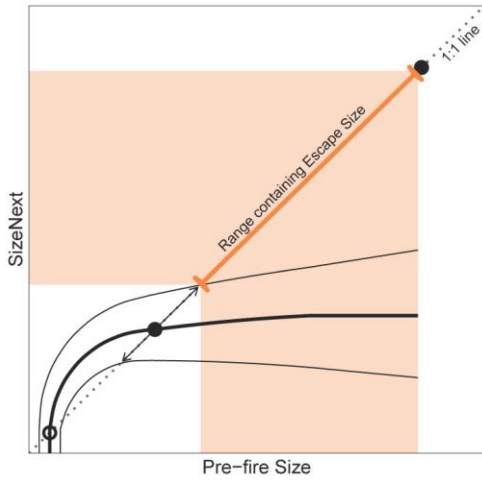
466 **Appendix S2:** Resprout curves for each species, fire treatment and dataset modelled  
467 separately

Species	Family	Maximum height (m)	Habit
<i>Corymbia nesophila</i> (Blakely) Hill & Johnson	Myrtaceae	25	Evergreen
<i>Eucalyptus miniata</i> Cunn. Ex Schauert	Myrtaceae	20	Evergreen
<i>Eucalyptus tetradonta</i> F. Muell.	Myrtaceae	30	Evergreen
<i>Erythrophleum chlorostachys</i> (F.Muell.) Baillon	Fabaceae	18	Semi-deciduous
<i>Planchonia careya</i> (F. Muell.) Knuth	Lecythidaceae	10	Deciduous
<i>Terminalia ferdinandiana</i> Exell	Combretaceae	10	Deciduous

**Table 1:** Species included in the case study. Maximum heights are from Brock and Dunlop (2007)



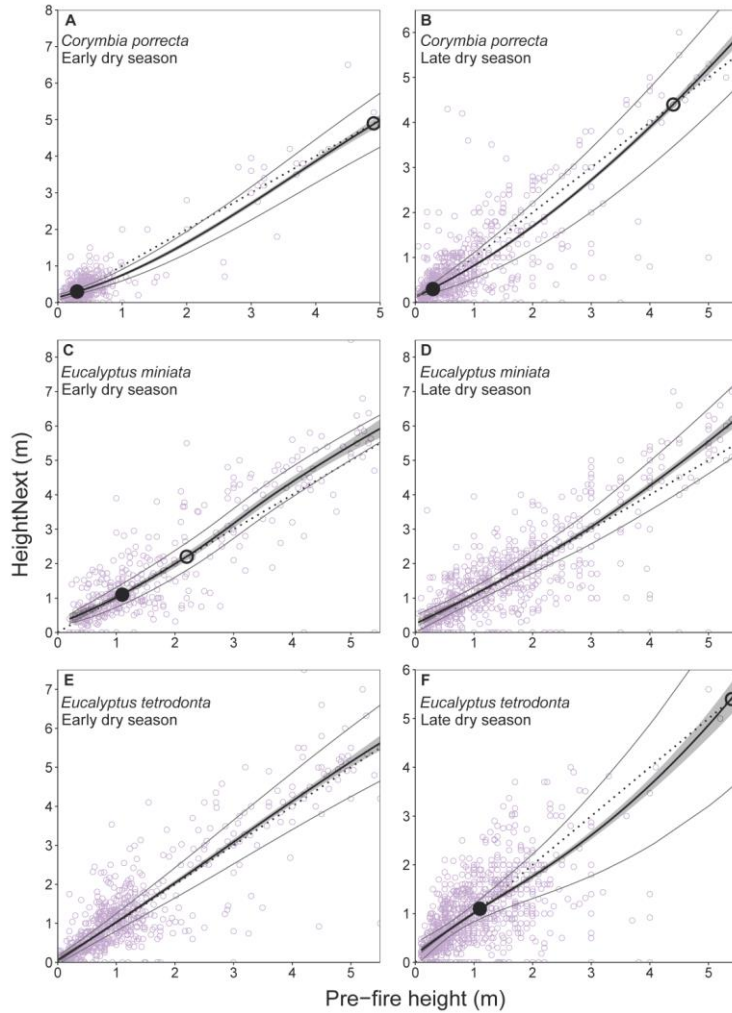
**Figure 1:** Conceptual models: possible forms of the resprout curve and resultant population structure under recurrent fire: **A:** the Grady and Hoffmann (2012) persistence equilibrium curve; **B:** the escape curve; **C:** the curve of constant growth; **D:** the death spiral. ● : stable equilibrium; ○ : unstable equilibrium. When the curve is above the one-to-one line, there is positive growth, i.e. the individual is able to recover and exceed its pre-fire size in the inter-fire period. If below the one-to-one line, the individual experiences negative growth i.e. it cannot recover its pre-fire size in the inter-fire period. Arrows indicate direction of size growth through subsequent inter-fire periods. The depicted population structures represent a single cohort of resprouts and/or canopy trees, however we acknowledge multiple cohorts might occur, particularly in scenario C.



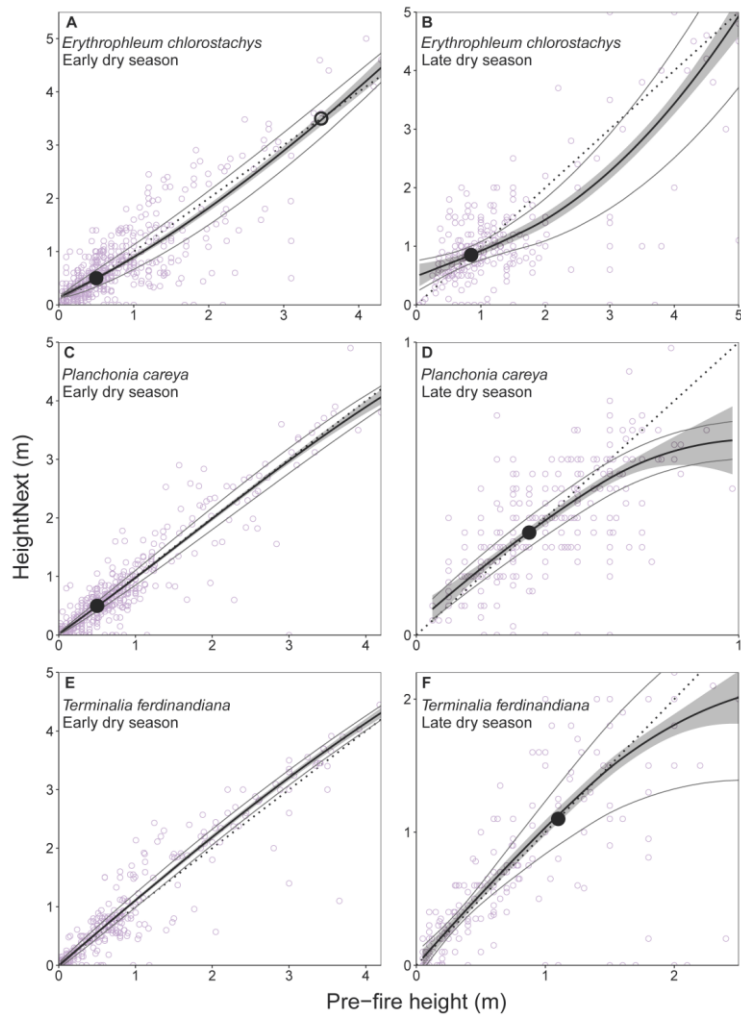
**Figure 2:** Size range containing 'escape size' (shaded region) for a population where only the persistence equilibrium curve (—) is detected. The maximum entropy distribution of escape size is between the upper bound of the prediction interval (---) around 'persistence size' and the 'maximum size' (for example canopy height) of the species. Escape size defines the upper limit of the fire trap. ● : stable equilibrium (here, lowest is persistence size, uppermost is maximum size); ○ : unstable equilibrium (here, mortality threshold).

	Height Class	Topkilled	Not Topkilled	Topkilled %
<i>Early Dry Season Fire Treatment</i>				
Tiwi Dataset	<0.5 m	554	179	75.58
	0.5 - 1.5 m	127	17	88.19
	>1.5 m & <5 cm DBH	228	239	48.82
Werner dataset	<0.5 m	138	40	77.53
	0.5 - 1.5 m	121	52	69.94
	>1.5 m & <5 cm DBH	7	29	19.44
<i>Late Dry Season Fire Treatment</i>				
Werner dataset	<0.5 m	129	0	100.00
	0.5 - 1.5 m	192	0	100.00
	>1.5 m & <5 cm DBH	14	3	82.35

**Table 2:** Counts and percentage of individuals by size class that were topkilled compared to not topkilled in two of the case study datasets. The “Williams” dataset did not contain topkill information and so is not included here. The lower number of individuals topkilled in the Early Dry Season regime reflects lower fire intensity and greater patchiness of this fire treatment compared to the Late Dry Season



**Figure 3:** Eucalypt resprout curves of the relationship between pre-fire height and height before the next fire (HeightNext). Fire treatments were early dry season burning and late dry season burning with each census spanning 1 year. ● : stable (persistence) equilibrium; ○ : unstable (escape size) equilibrium. Data are combined from 3 separate datasets. Each data point (○) represents height growth response of one individual within one year, with fire occurring soon after the pre-fire height measurement. Curves are robust LOESS smooths with 95% confidence intervals (shaded) and 50% prediction intervals (thin lines). Figures A, B, C, and F conform show the escape resprout curve. Figures D and E are curves of constant growth (although close, the fitted curves do not actually cross the 1:1 line). These results indicate the strong ability of eucalypts to persist in and escape from the fire trap under both early and late dry season fire.



**Figure 4:** Non-eucalypt

resprout curves of the relationship between pre-fire height and height before the next fire (HeightNext). Fire treatments were early dry season burning and late dry season burning with each census spanning 1 year. ● : stable (persistence) equilibrium; ○ : unstable (escape size) equilibrium. Data are combined from 3 separate datasets. Each data point (○) represents the height growth response of one individual within one year, with fire occurring soon after the pre-fire height measurement. Curves are robust loess smooths with 95% confidence intervals (shaded) and 50% prediction intervals (thin lines). Figures A and B conform to the escape resprout curve (B escape height is just outside the limits of the data). Figures C, D and F conform to the persistence resprout curve. Figure E is a curve of constant growth. *Erythrophleum chlorostachys* performs similarly to eucalypts under these fire regimes. Late dry season fires, on average, indefinitely trap *Planchonia careya* and *Terminalia ferdinandiana* resprouts at their persistence equilibrium size.