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# Flux Mapping: a new approach to evaluating model process representation under uncertainty

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**Key Points:**

- Characterised different facets of model-equifinality and discussed them within the context of conceptual hydrological modelling.
- Introduced the new model evaluation method of Flux Mapping to explore model behaviour, particularly process-representation.
- Even within a very narrow margin of model error/performance, different modes of model response (i.e. internal flux dynamics) can be equally active.

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## Abstract

Uncertainty analysis is an integral part of any scientific modelling, particularly within the domain of hydrological sciences given the various types and sources of uncertainty. At the centre of uncertainty rests the concept of *equifinality*, i.e. reaching a given endpoint (*finality*) through different pathways. The operational definition of equifinality in hydrological modelling is that various model structures and/or parameter sets (i.e. *equal pathways*) are *equally* capable of reproducing a *similar* (not necessarily *identical*) hydrological outcome (i.e. *finality*). Here we argue that there is more to model-equifinality than model structures/parameters, i.e. other model components can give rise to model-equifinality and/or could be used to explore equifinality within model space. We identified six facets of model-equifinality namely model structure, parameters, performance metrics, initial and boundary conditions, inputs, and internal fluxes. Focusing on model internal fluxes, we developed a methodology called *Flux Mapping* that has fundamental implications in understanding and evaluating model process-representation within the paradigm of multiple working hypotheses. To illustrate this, we examine the equifinality of runoff fluxes of a conceptual rainfall-runoff model for a number of different Australian catchments. We demonstrate how flux maps can give new insights into the model behaviour that cannot be captured by conventional model evaluation methods. We discuss the advantages of flux space, as a sub-space of the model space not usually examined, over parameter space. We further discuss the utility of flux mapping in hypothesis generation and testing, extendable to any field of scientific modelling of open complex systems under uncertainty.


## 1 Introduction

Understanding, modelling and predicting hydrological systems—realistically and viably—is the Holy Grail of hydrological sciences. There are barriers in this quest, particularly in a world undergoing rapid and large-scale changes (Peel & Blöschl, 2011). Among numerous difficulties with modelling and prediction of real-world hydrological processes are the issues of: scale (Blöschl & Sivapalan, 1995) and commensurability (Beven, 2012b, p. 245) between observed and modelled variables; dependency upon the quantity (Boughton, 2007) and quality (Beven & Westerberg, 2011; Yew Gan et al., 1997) of available data and their information content (Nearing & Gupta, 2015); model complexity (Perrin et al., 2001; Yew Gan et al., 1997); the chaotic nature of many hydrological processes (Khatami, 2013a, 2013b; Sivakumar, 2000; Sivakumar et al., 2001); modelling hydrological responses to change (Schaefli et al., 2011) and resilience to disturbance (Peterson & Western, 2014; Peterson et al., 2014); "*numerical daemons*" of conceptual hydrological modelling (Clark & Kavetski, 2010; Kavetski & Clark, 2011); and the ill-conditionedness or ill-posedness of environmental models (Beck, 1987; Yeh, 1986). The latter is also referred to as *equifinality* (Beck, 2002; Beven, 2006; Ebel & Loague, 2006; Kelleher et al., 2017).

Beven (1975, p. 14) first used the term equifinality in the domain of hydrological modelling. Later, Beven (1993) proposed a concept of equifinality for model evaluation and

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uncertainty analysis. Based on his suggested concept, the operational definition of equifinality is that different model structures and/or parameter sets (i.e. *equal pathways*) are *equally* capable of reproducing a *similar* (not necessarily *identical*) hydrological outcome (i.e. *finality*). For example, in the case of rainfall-runoff modelling, for a given criterion of reproducibility (e.g. an objective function), a number of rainfall-runoff models (i.e. distributed or lumped, process-based or black-box, etc. such as TOPMODEL, HBV, Sacramento, etc.) and/or various parameter sets might be able to equally reproduce a particular observed runoff. This operational definition of equifinality is closely related to structural and parameter uncertainty, and is the cornerstone of sensitivity and uncertainty estimation frameworks such as generalised sensitivity (Hornberger & Spear, 1981) and GLUE (Generalised Likelihood Uncertainty Estimation, (Beven & Binley, 1992)).

In this paper we argue that equifinality—like uncertainty—is a multi-faceted concept, and various model components other than model structure and parameters could also give rise to model-equifinality. We first, briefly outline various facets of model-equifinality (section 2); namely equifinality of model structures and/or parameters, objective functions (or model performance metrics), model initial/boundary conditions, model inputs, and model internal fluxes. We should mention that there are other facets of equifinality than model-equifinality that we discussed under a comprehensive theoretical framework of scientific inquiry and modelling of hydrological systems under uncertainty (Khatami et al., under review). While facets of model-equifinality are not mutually exclusive and in fact are intertwined, each facet underscore a particular aspect (sub-space) of the overall model space. We develop a new model evaluation scheme, called *Flux Mapping* (section 3), to examine the degree of equifinality of model internal fluxes, and to explore and characterise model process-representation. Using a modelling experiment (section 3.4), we demonstrate how flux mapping—analysing model-equifinality through the lens of model internal fluxes instead of model parameters—provides new insights into model internal behaviour and process-representation, which cannot be (easily) captured/characterised using conventional model evaluation schemes (e.g. objective functions, dotty plots, and parameter distributions) (sections 4 and 5.1). In other words, reprojecting model behaviour (e.g. response surface) from parameter space to the flux space can give new insights into model internal behaviour that are not inferable from parameter space. To this end, we showcase and discuss the results of flux mapping for a number of Australian catchments (section 4).

Flux mapping is an approach to generate and explore multiple working hypotheses (MWH) based on model internal behaviour and process-representation. Chamberlin (1890) argued for the paradigm of MWH in scientific inquiries as this paradigm is more robust to reduce bias (i.e. assure impartiality) towards a particular hypothesis for explaining a given phenomenon. Theoretically, to explain real-world processes, MWH is a never-ending process within which *hypotheses*, i.e. a set of plausible explanations of real-world phenomenon, are generated, evaluated, revised/refined, and further evaluated with the hope that our refined hypotheses converge towards an approximation of the actual reality. The value and significance of pursuing

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MWH in hydrological modelling is discussed in the literature (Beven, 2012a; Beven et al., 2012; Buytaert & Beven, 2011; Clark et al., 2011, 2012). We further discuss the utility and exploratory power of flux mapping in hypothesis forming/testing and process understanding (section 5.2). Flux mapping is extendable beyond hydrological modelling to any field of scientific modelling dealing with conceptual modelling of open complex systems under uncertainty.

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## 2 Facets of model-equifinality: theoretical discussion

Throughout the hydrological literature when the term equifinality is used it is predominantly referring to model-equifinality; different model structures and/or parameter sets could produce a similar outcome given some available (uncertain) observations and a particular (incomplete) metric of acceptability (e.g. model performance above a subjective value of one/multiple objective functions). So, model-equifinality is conditional on the model configuration, performance metric(s), and the information content of the data used. Beven (1975, p. 14) was the first to use the term equifinality in hydrology, and later Beven (1993) discussed its implication in hydrological modelling in terms of multiple acceptable model structures and/or parameter sets as a preferred alternative to the notion of a single optimum parameter set. There also has been other studies that referred to model-equifinality using other terms such as ambiguity, identifiability, empirical equivalence, non-uniqueness, under-determination or indeterminacy, system convergence, etc (e.g. Beck, 1987; Bethke, 1992; Carrera & Neuman, 1986; Gupta & Sorooshian, 1983; Hornberger & Spear, 1981; Konikow & Bredehoeft, 1992; Oreskes et al., 1994; Quine, 1975; Sorooshian & Gupta, 1983; Yeh, 1986).

The question of model-equifinality is often reduced to model parameter equifinality as parameter uncertainty expressed in probabilistic terms (i.e. parameter distribution), although there are other studies that attempted to take other sources of uncertainty into account such as model inputs (e.g. Blazkova & Beven, 2009; Haydon & Deletic, 2009; Kavetski et al., 2006; Liu et al., 2009; Vrugt et al., 2008) or structural uncertainty (Ajami et al., 2007; Bulygina & Gupta, 2009, 2010, 2011; Butts et al., 2004; Renard et al., 2010). In this section, we make the case that there is more to model-equifinality than parameter uncertainty (distribution) by characterising six different, yet interconnected, facets of model-equifinality.

### 2.1 Equifinality of model structures

Multiple model structures with different degrees of complexity (i.e. number of model parameters, fluxes, and/or other components) that are almost equally capable of reproducing a hydrologic behaviour (e.g. discharge hydrograph) could be seen as MWH; with each model structure *representing* catchment behaviour differently, and hence equifinality of model structures. Various hydrological modelling frameworks have been developed arguably based on this very facet of model-equifinality, whether or not this facet was explicitly acknowledged; including, but not limited to, SUMMA (Clark et al., 2015a; Clark et al., 2015b), FUSE (Clark et

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al., 2008), and SUPERFLEX (Fenicia et al., 2011; Kavetski & Fenicia, 2011). Evaluating the *realism* of model structures (process-representation) is fundamentally difficult, regardless of the number of models utilised and their (dis)agreement; as not all catchment internal processes are known or observed even at the scale of interest. Developing/choosing the model structure is majorly dependent upon the personal judgements and preferences of modellers (Addor & Melsen, 2019; Holländer et al., 2009) and influenced by politics (Heymann & Dalmedico, 2019). Thus there is a "*problem of decidability*" (Beven, 2006) between feasible representations of the real-world, i.e. which conceptual model fits better to our perceptual model. In fact, the choice of model structure, like other subjective decisions in modelling e.g. the choice of objective function (Crochemore et al., 2015) (discussed below), is often an act of *will* (i.e. modeller's personal or institutional preference) rather than *rationality/objectivity* (i.e. model adequacy or fit-for-purpose). For instance, Addor and Melsen (2019) demonstrated that in most cases that they investigated, the affiliation of the first author was a clear predictor of model selection, while the role model adequacy given the research objectives was less clear.

It is worth mentioning that model-structure-equifinality could be seen as a special case of equifinality of modelling approaches. Different modelling approaches, such as a top-down vs bottom-up, process-based vs black box, distributed vs lumped, may lead to similar results in a given modelling case.

### 2.2 Equifinality of model parameters

This is the most widely studied facet of equifinality in hydrology (Arsenault & Brissette, 2014; Beven & Binley, 2014; Kelleher et al., 2017; Kelleher et al., 2015; Kirchner, 2016; Tang & Zhuang, 2008; Teweldebrhan et al., 2018b; Vrugt & Beven, 2018). The operational definition of equifinality in hydrological literature is in fact parameter equifinality. Equifinal parameters are uncertain. Within the hydrological literature parameter equifinality and uncertainty are treated similarly and interchangeably. In simple terms, parameter uncertainty means that there is no certain/true parameter set and it is conventionally represented probabilistically as parameter distributions (commonly presented as marginal distributions). There are multiple acceptable/working parameter sets, i.e. equifinal parameters, within the larger set of all uncertain parameters. Parameter uncertainty is generally addressed by searching for multiple acceptable parameter sets (e.g. set-theoretic approaches and Monte Carlo experiments) given single/multiple measures of model performance. There are different ways to address parameter uncertainty e.g. Bayesian approach where different degrees of belief are assigned to the sampled parameter sets, approaches where parameter sets below a certain threshold of acceptability or outside particular limits of acceptability are rejected (e.g. GLUE) (Beven, 2009; Vrugt & Beven, 2018). Regardless of the approach, parameter uncertainty is typically then expressed in terms of likelihood, i.e. a parameter distribution.

In the above, parameter equifinality is determined based on the model performance—i.e. the value of objective (or likelihood) function(s)—and the physical significance/plausibility of

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the so-called equifinal/behavioural parameter sets is often not examined. While, typically expressed probabilistically, parameter equifinality could be represented in other non-probabilistic forms (see section 4 for more details). It should be further noted that it is difficult to draw a sharp dividing line between model structure and parameter equifinality, as the two are intertwined. Model structures (e.g. equations of model fluxes and storages) can be dependent upon the parameter values (driven by the input data), and parameter values change the function of a model component, sometimes drastically. For instance, for the SIMHYD model used in this study (see Figure 5-A), parameter INSC (Interception Store Capacity) can vary between 0 and 20. INSC = 0 means the interception storage of the model is non-existent, hence a significant change in process description/representation within the model structure. Similarly, K (baseflow recession parameter) can vary between 0 and 1. K = 0 means a non-existent flux, otherwise a linear flux equation with slopes decreasing from 1 (i.e. K = 1) asymptotic to the *x*-axis (horizontal line at 0) as $K \rightarrow 0$. That is, each of these parameter values leads to an effectively different model structure.

### 2.3 Equifinality of model performance metrics (or objective functions)

Objective functions—both their choice and function—are integral parts of the *modelling process*. For instance, the model output or response surface is the product of the interplay between model structure, parameters, objective function, data information content, and modeller's decisions. Objective functions characterise the model performance as an aggregated measure of the matching between modelled and observed; either as metrics of model residuals (Bennett et al., 2013; Davtalab et al., 2017; Fowler et al., 2018; Murphy, 1988) or as signatures of similarity (Addor et al., 2018; Fowler et al., 2016; Gupta et al., 2008; Kelleher et al., 2017; Pfannerstill et al., 2014; Sawicz et al., 2014; Schaefli, 2016; Yilmaz et al., 2008); whether a scalar metric/variable (single criterion) or a vector of metrics/variables (i.e. multiple criteria/multivariable) (Efstratiadis & Koutsoyiannis, 2010; Gupta et al., 1998; Stisen et al., 2018), whether aggregated or distributed (Koch et al., 2017; Koch et al., 2016). Performance metrics reduce the complex behaviour of a system—often the integrated response of the catchment system, i.e. discharge—from a higher dimension (e.g. a time series) to a single, or a few, point values; thus information loss is inevitable (Gong et al., 2013; Gupta & Nearing, 2014; Nearing & Gupta, 2015). Such aggregations, similar to the averaging process discussed by Savenije (2001), give rise to equifinality. That is, a similar model error (i.e. distance between the model output and observed behaviour, e.g. discharge hydrograph) could be the result of different objective functions with different mathematical structures. Although it is possible to improve metrics e.g. by benchmarking (Schaefli & Gupta, 2007; Seibert, 2001) or reformulation (Chiew et al., 1993; Gupta et al., 2009; Legates & McCabe, 1999; Pool et al., 2018; Willmott et al., 2012), all metrics (whether single/vector or error-based/signature) have limitations and deficiencies (Pushpalatha et al., 2012; Santos et al., 2018; Westerberg & McMillan, 2015; Westerberg et al., 2016). The problem of metric equifinality will not be eliminated by developing more sophisticated metrics. There is no ultimate (set of) objective function(s), as all metrics are

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"*underdetermined*" (i.e. "*do not describe unique error characteristics, even when many of them are used collectively*" (Tian et al., 2016)). Tian et al. (2016) demonstrated how identical values of conventional metrics and their derivatives—e.g. bias, correlation coefficient, and mean square error—can be achieved from vastly different time series.

### 2.4 Equifinality of model initial/boundary conditions

Given the unknowability of historical/future initial and boundary conditions in almost all cases (epistemic uncertainty), they are a source of model-equifinality. That is, different initial/boundary conditions can lead to similar results. Ebel and Loague (2006) simulated five scenarios of different initial/boundary conditions (e.g. soil-water content and permeability characteristic functions) for a distributed model of an experimental catchment, with NSE (Nash–Sutcliffe model Efficiency (Nash & Sutcliffe, 1970)) values between 0.66 to 0.82 for the discharge. That is, different initial/boundary conditions could lead to reasonably acceptable model performance for the discharge. To see through this "*fog of equifinality*" of models' discharge performances, they further compared the simulated and observed pressure-head at three locations, and found that the associated NSE values were all negative except for the scenario with discharge NSE of 0.76. They attempted to constrain the model-equifinality and improve the model realism by looking at variables other than discharge, i.e. introducing additional information. There can be many other realistic scenarios with different initial/boundary conditions (Pappenberger et al., 2006), and these scenarios may fail to simulate other catchment processes if new data are introduced.

### 2.5 Equifinality of model inputs

Different input variables with varying degrees of information content (i.e. different types, quantities and qualities of inputs) could lead to similar model outcome, e.g. equifinality of model predictions from different stochastic realisations of the input data (Zin, 2002) such as rainfall input (Ehlers et al., 2018). Newman et al. (2015) developed an ensemble of gridded observation-based daily precipitation and temperature for 1980-2012 for the contiguous United States, which could be used to account for uncertainty of gridded product and model forcing, as well as exploring the equifinality of model inputs. As another example, Oudin et al. (2005) investigated the use of different potential evapotranspiration (PET) inputs to four different rainfall-runoff models, and found no systematic improvements in the calibrated model performance when using daily temporally varying PET instead of seasonal mean PET. This instance of model input equifinality may also be related to the insensitivity of the model (process-representation) to input information content.

### 2.6 Equifinality of model internal fluxes

Various combinations of model internal fluxes can lead to similar model output. Interception, evapotranspiration, and runoff fluxes are examples of internal fluxes in the case of a conceptual rainfall-runoff model. These fluxes are essentially representations of real-world

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processes, e.g. model runoff fluxes mimic catchment runoff generation mechanisms. Also, under a given model conditioning, i.e. available data and model performance metrics, different routines for calculating internal fluxes (e.g. interception) can be equifinal. Grayson et al. (1992) demonstrated that a given observed hydrograph could be equally reproduced through Hortonian overland flow or saturated area runoff with very different distributed flow characteristics. Physical significance is a distinct characteristic of flux equifinality, over other facets of model-equifinality like parameter equifinality, which is desirable for generating/testing hypotheses.

It should be noted that these six facets of model-equifinality are not mutually exclusive, as different model components are intertwined as discussed above. That said, each facet accentuates a particular aspect (sub-space) of the overall model space. That is, each facet (or their combinations) could be utilised as a way of generating model simulations or to investigate an ensemble of model runs in terms of MWH. In the next section, we demonstrate how replacing the emphasis from the equifinality of model parameters to model internal fluxes gives new insights into model behaviour and to generate MWH, even if only model parameters are perturbed.

## 3 Flux Mapping: an approach to evaluate model internal dynamics

In this section we develop a method called *Flux Mapping* for evaluating model behaviour, based on the concept of model internal flux equifinality. We demonstrate that the new tool of *Flux Maps* can give new insights into model behaviour that are not inferable from conventional model evaluation tools of dotty plots (i.e. projection of points on a model response or likelihood surface onto a single parameter axis (Beven, 2006)) or statistical parameter distributions.

### 3.1 Hydrological model

For this study, we chose SIMHYD, a lumped conceptual daily rainfall-runoff model (Chiew et al., 2002; Peel et al., 2000). It has seven parameters, takes precipitation and areal potential evapotranspiration as inputs, and generates streamflow as the output. SIMHYD incorporates runoff generating mechanisms; namely infiltration excess (INFexc), interflow and saturation excess overland flows (INT & SATexc) and baseflow (BAS) (Figure 5A). With three runoff generating mechanisms it is a suitable choice to examine the equifinality of internal (runoff) fluxes.

### 3.2 Study area and data set

The Australian Network of Hydrologic Reference Stations (HRS) is a set of 222 catchments (http://www.bom.gov.au/water/hrs/) with minimal land use disturbances and water resource development, and relatively high-quality data (Turner, 2012, p. 6) composed of daily time series of observed streamflow (Q). Fowler et al. (2016) calculated areal average precipitation (P) from AWAP (www.bom.gov.au/jsp/awap/) daily 5km grids (Jones et al., 2009),

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and also estimated areal potential evapotranspiration (APET) at the catchment centroid using Morton's Wet Environment method (Morton, 1983) using gridded estimates of Jeffrey et al. (2001) (see Fowler et al. (2016) for further details of data set preparation).

The modelling experiment (flux mapping) is conducted on a subset of HRS catchments with a high level of SIMHYD performance, here defined as NSE $\geq$ 0.75. To select them, SIMHYD was first calibrated to all HRS sites over their total streamflow record, using the global optimisation algorithm of Shuffled Complex Evolution (SCE-UA) (Duan et al., 1992). For each case, the SCE-UA routine was repeated 20 times to ensure consistency in the calibration results. The highest NSE value from the 20 repeats for each catchment-model pair was selected as the upper bound of possible model performance (hereinafter SCE-NSE). A subset of the top 53 catchments, $0.75 \leq NSE \leq 0.88$, were selected. It should be stressed that this pre-calibration step is not a part of the modelling experiment and only serves to find the upper bound of model performance as a rough measure of sampling sufficiency (explained in the following section).

### 3.3 Flux Mapping

Figure 1-A presents a conceptual example indicating that a model (here SIMHYD) can simulate an observed hydrograph through different combinations of model internal fluxes (here, proportions of model runoff fluxes), leading to similar NSE values ($0.803 \leq NSE \leq 0.825$) at a given catchment. It clearly shows the value of the objective function is not a reliable measure of model internal behaviour. For a large ensemble of model runs, equifinal fluxes can be summarised and visualised based on the percentage of their (volumetric) contribution to the total simulated Q on a plot we name a *Flux Map*. Figure 1-B is a conceptual example of flux map, and is used to inspect the runoff flux space, a subset of the model flux space, of SIMHYD model by mapping the three runoff fluxes (i.e. INFexc, INT & SATexc, and BAS) for three equifinal model runs demonstrated on Figure 1-A.

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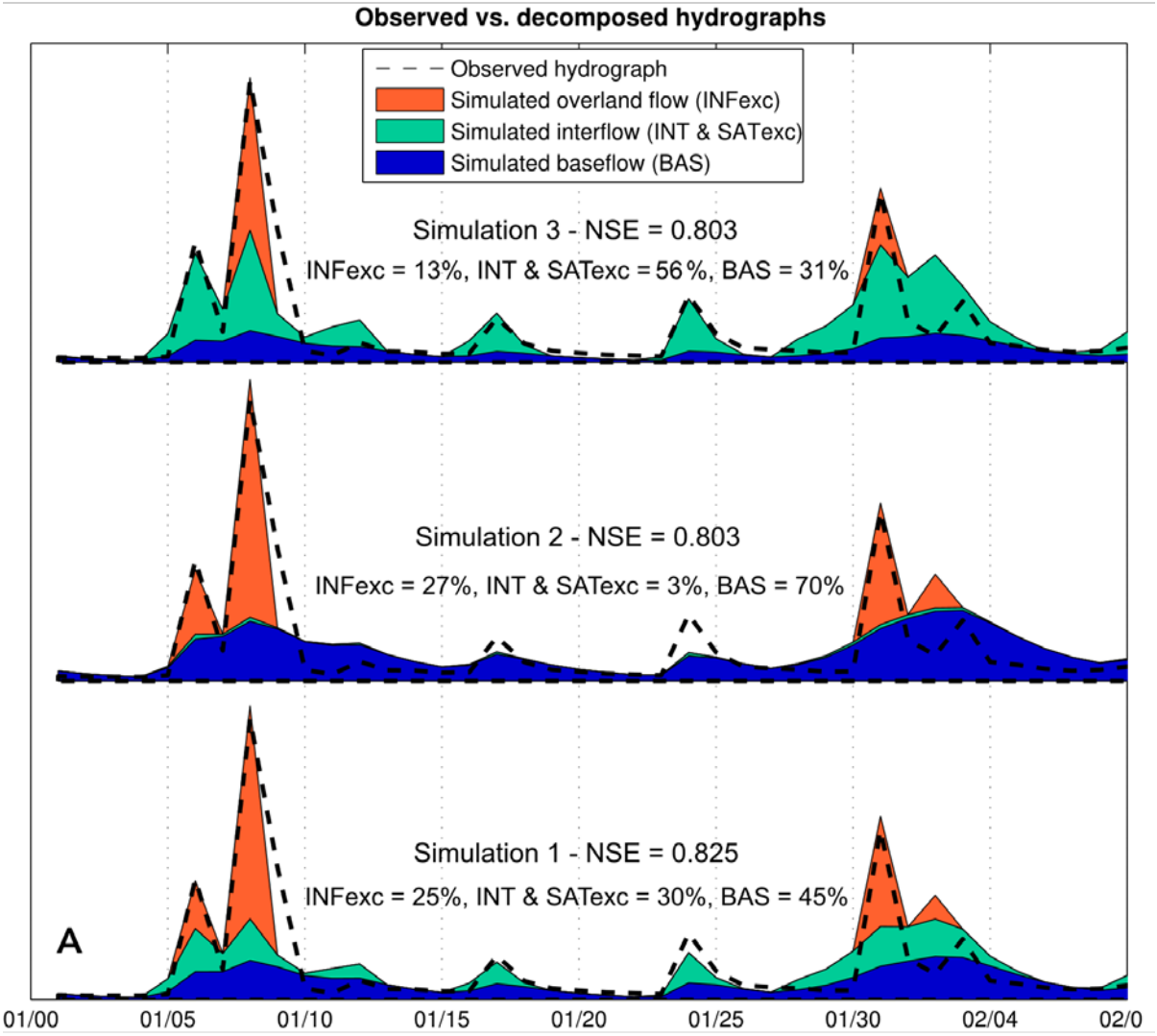


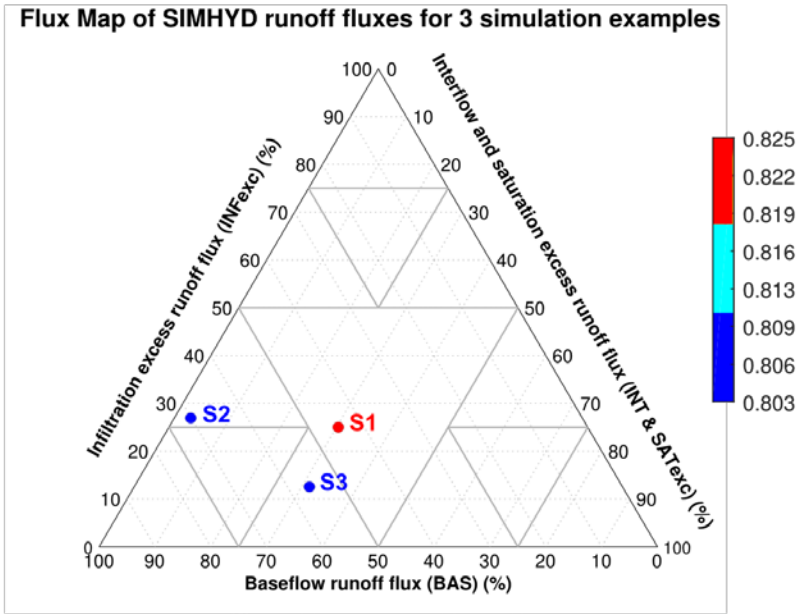


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**Figure 1**. (A) Three simulations (S1-S3) of an observed hydrograph through different combinations of runoff generating mechanisms (volumetric contribution to the total simulated runoff) summarised on a flux map (B), colour-coded based on the simulation performance (NSE value). The triangle (B) represents the plausible flux space for a model with three runoff fluxes.

A flux map is a ternary plot where each dimension represents a model runoff flux, and each model run is projected as a single point based on the proportions of its equifinal runoff fluxes to the total simulated Q. The cloud pattern can vary from very constrained (Figures 3A, one flux is dominating the simulation of total Q), through intermediated cases (Figures 3B and 3C, two fluxes are co-dominating the simulation of total Q with possibly small contribution of the third flux), up to filling the entire plausible flux space (i.e. the entire triangle, Figures 3D and 4). Thus, the point cloud on the flux maps is an expression of the model flux equifinality; filling a larger space on the flux map indicates higher degrees of model flux equifinality. In the case of two fluxes, the plausible flux space would shrink to a line showing the interplay between the contribution of either flux. In case of more than three fluxes, the flux map can be simply presented as a series of 2-by-2 scatterplots.

### 3.4 Experiment design

The flux space of each catchment model is explored using simulations of $10^6$ parameter sets sampled from a uniform parameter (prior) distribution using Latin Hypercube Sampling (LHS). The sample size was determined by comparing the difference between SCE-NSE (the best NSE value from 20 repeats of pre-calibration) and the highest NSE value from the LHS ensemble (hereinafter Ensemble-NSE) at a few trial catchments. Selecting $10^6$ samples generally led to the Ensemble-NSE being within 3% of the SCE-NSE, suggesting that $10^6$ samples was sufficient to adequately explore the parameter space and the consequent flux space. It should be mentioned that for higher dimensional parameter spaces, LHS or random sampling are very inefficient and often insufficient; efficient searching/sampling strategies should be used instead such as dynamically dimensioned search (Tolson & Shoemaker, 2008).

To track the emerging pattern of the point cloud of the flux maps, model runs are evaluated against a set of thresholds of equifinality/acceptability, defined as SCE-NSE × {0.99, 0.98, 0.97, 0.96, 0.95, 0.90, 0.85, 0.80}. That is, gradually relaxing the threshold—hereinafter referred to as *thresholding*. Equifinal model runs above a given threshold are considered as acceptable and the rest as unacceptable.

## 4 Results

The overall model performance in the example catchments is $0.75 \leq$ SCE-NSE $\leq 0.80$, and for the extreme case is SCE-NSE = 0.82. Yet, as shown in Figures 3 and 4 the flux maps are vastly different. We chose four classes of general flux map behaviour (Class I to IV), within the 53 catchments studied, for further discussion. For each class, we present flux maps of an

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example catchment for the *strict* (0.95×SCE-NSE) and *relaxed* (0.85×SCE-NSE) thresholds (Figures 3 and 4), colour-coded based on the corresponding Ensemble-NSE values. For Class IV, an additional example of an extreme case is also presented (Figure 4). Flux maps of other thresholds are presented in the supporting information (Table S1) to demonstrate the emerging pattern of the flux maps. Also, the corresponding 2-by-2 flux maps of Figures 3 and 4 are available (see Khatami et al., 2017). To the extent possible, the four examples have similar hydrological characteristics; namely catchment area of 125-170 $km^2$, mean annual P = 950-1353 mm, mean annual Q = 162-335 mm, mean annual APET = 1222-1532 mm, and annual runoff coefficient 0.17-0.25. The extreme case of Class IV flux maps is quite similar to the other four examples except for a smaller catchment area, 83 $km^2$, and a higher runoff coefficient of 0.44. Figure 2 presents the location of example catchments based on the Köppen-Geiger climate classification (Peel et al., 2007), and catchment summaries are presented in Table 1. Specific simulation characteristics of each example are mentioned in the corresponding figure caption.

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**Figure 2.** Map of the Australian example catchments for the modelling experiment of flux mapping. The colour scheme is based on the Köppen-Geiger climate classification by Peel et al. (2007).

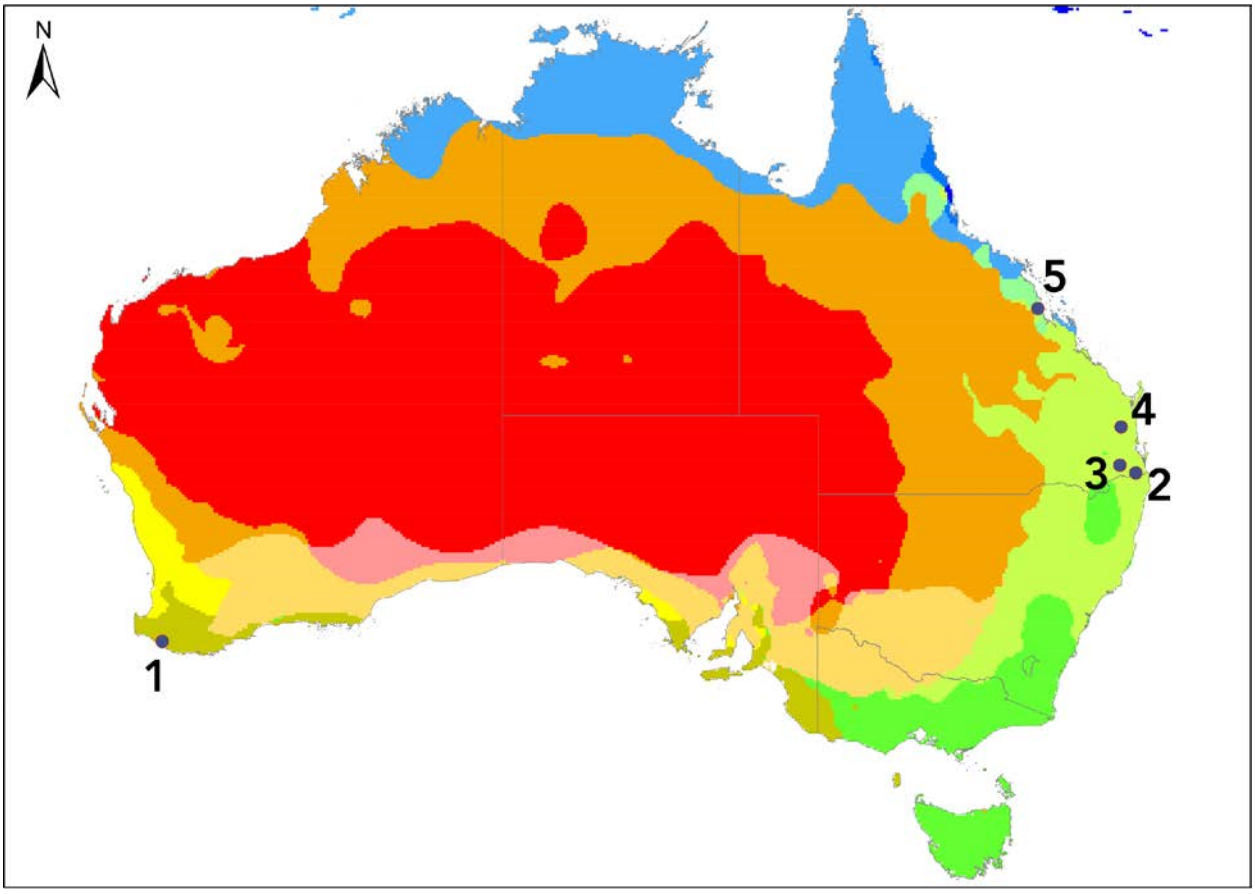


**Table 1.** Catchments summaries of the examples presented in modelling experiments

| Catchment No. | Corresponding figures (Class) | Catchment | | | | | | |
|---|---|---|---|---|---|---|---|---|
| | | Name | Location | Area ($km^2$) | Mean annual total P (mm) | Mean annual total Q (mm) | Mean annual APET (mm) | Annual runoff ratio |
| 1 | Figs 3-A1 & 3-A2 (Class I) | Dombakup Brook at Malimup Track | Western Australia (115.98° E 34.58° S) | 125.09 | 1130.99 | 232.63 | 1222.41 | 0.21 |

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| **2** | **Figs 3-B1 & 3-B2 (Class II)** | Albert River at Lumeah | Queensland (153.05° E 28.05° S) | 167.39 | 1353.61 | 335.14 | 1451.17 | 0.25 |
| **3** | **Figs 3-C1 & 3-C2 (Class III)** | Bremer River at Adams Bridge | Queensland (152.51° E 27.83° S) | 126.09 | 951.07 | 162.19 | 1506.55 | 0.17 |
| **4** | **Fig 3-D1 & 3-D2 (Class IV)** | Kandanga Creek at Hygait | Queensland (152.65° E 26.39° S) | 170.78 | 1135.18 | 277.98 | 1532.49 | 0.24 |
| **5** | **Fig 4-A, 4-B, & 4-C (Class IV)** | Carmila Creek at Carmila | Queensland (149.399° E 21.915° S) | 83.8 | 1275 | 538 | 1736 | 0.42 |

4.1 Class I

The point cloud on the flux map in Figures 3A is very constrained indicating a very low degree of flux equifinality; a baseflow-dominant runoff simulation, having zero infiltration excess runoff and a low saturation excess runoff in the simulations. For the strict threshold (Figure 3-A1) there are 252 equifinal model runs, which all exhibit a very narrow range of possible flux contributions to total simulated Q. As the equifinality threshold lowers to the relaxed threshold (Figure 3-A2) the number of equifinal runs increases, yet the general pattern of the flux map remains; i.e. predominantly baseflow oriented, with the possibility of up to 20% contribution from INT & SATexc.

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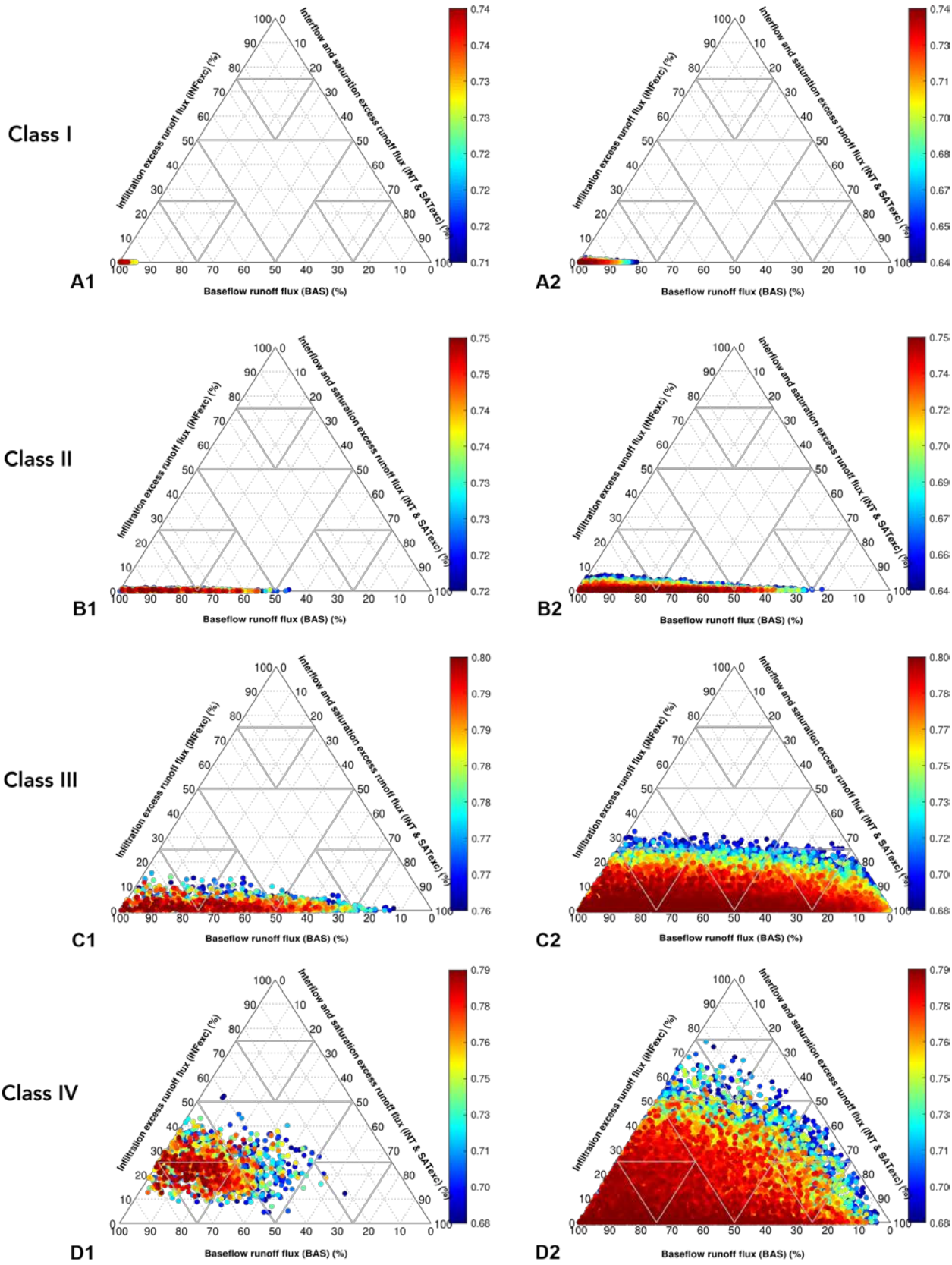


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**Figure 3**. This figure represents how different model internal behaviour, represented on flux maps, can emerge within a certain range of model performance. Flux maps for 4 different Australian catchments (catchments 1-4 on Table 1) for two different thresholding; each row presents a different catchment with strict threshold on the first column and relaxed threshold on the second column. Colour bar represent the model performance in terms of NSE value. (A) Class I flux maps for strict threshold (0.95×SCE-NSE=0.71 ≤ Ensemble-NSE=0.75 ≤ SCE-NSE=0.75) with 252 equifinal simulations (A1), and relaxed threshold (0.85×SCE-NSE=0.64 ≤ Ensemble-NSE ≤ SCE-NSE) with 3036 equifinal simulations (A2). (B) Class II flux maps for strict threshold (0.95×SCE-NSE=0.71 ≤ Ensemble-NSE=0.75 ≤ SCE-NSE=0.75) with 592 equifinal simulations (B1), and relaxed threshold (0.85×SCE-NSE=0.64 ≤ Ensemble-NSE ≤ SCE-NSE) with 8476 equifinal simulations (B2). (C) Class III flux maps for strict threshold (0.95×SCE-NSE=0.74 ≤ Ensemble-NSE=0.78 ≤ SCE-NSE=0.78) with 3644 equifinal simulations (C1), and relaxed threshold (0.85×SCE-NSE=0.66 ≤ Ensemble-NSE ≤ SCE-NSE) with 47702 equifinal simulations (C2). (D) Class IV flux maps for strict threshold (0.95×SCE-NSE=0.71 ≤ Ensemble-NSE=0.75 ≤ SCE-NSE=0.75) with 1270 equifinal simulations (D1), and relaxed threshold (0.85×SCE-NSE=0.64 ≤ Ensemble-NSE ≤ SCE-NSE) with 65126 equifinal simulations (D2). Catchment summaries are presented in Table 1.

Model runs with similar flux contributions but distinct flux dynamics (e.g. magnitude, shape and sequencing of events), would be mapped as identical points on the flux map. Therefore, even a very constrained flux map might be unfolded to a number of model runs with distinct dynamics yet similar volumetric contribution of the fluxes. In other words, flux maps are in fact under-estimating the flux equifinality.

### 4.2 Class II

The flux map for this class (Figures 3B) is mainly constrained around a line which corresponds to the complementary possible contributions of the BAS and INT & SATexc runoff fluxes. The range of the line varies depending on the thresholding. For the strict threshold (Figure 3-B1), the baseflow contribution to total runoff volume is around 45-90%; and as the threshold relaxes (Figure 3-B2), baseflow contributes 15-100% to the total simulated flow. SIMHYD exhibits less than 5% contribution from INFexc at the relaxed threshold.

It should be noted that in producing flux maps, model runs with different performance but similar flux contributions are plotted on top of each other, with higher performing points (towards red) plotted on top. So, the marginal distributions of flux maps are also provided (supporting information Table S1). Regardless of the threshold, even the highest performing points (i.e. red ones in the cloud) are moderately spread across the two contributing fluxes. Colour-coding and marginal distributions of flux maps are not suggested as a way for identifying *optimal* or *high likelihood* regions on the flux maps. One cannot infer that model runs with higher performance values (red points on the flux maps) are more realistic. Model

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performance—particularly assessed in a scalar sense—is a weak, unreliable, and unrealistic measure for model evaluation, as model process-representation cannot be *measured* with a single (or few) value(s) of performance metrics (for further details also see the discussion on hydrological signatures (Addor et al., 2018; Euser et al., 2013; Gupta et al., 2008; Kelleher et al., 2017; Schaefli, 2016; Yilmaz et al., 2008)). As demonstrated by Ebel and Loague (2006) and Seibert and McDonnell (2002) in detail, strict interpretation of objective functions is misleading, as model runs with slightly lower values of NSE might have better process-representation than the higher ones. Model performance does not imply realism, and may be a numerical artefact given various sources of uncertainty. Insufficient knowledge of catchment processes (e.g. runoff generating mechanisms and the details of the sequencing of different storm and runoff events) make it difficult to assign likelihood to model runs. Marginal distributions (Table S1) and colour-coding of the flux maps, only serve a demonstrative purpose (the spread of equifinal fluxes on the flux map) and not a prescriptive one (necessarily indicating the realism of model runs). All the cloud points are equifinal by definition; i.e. *possible* flux contributions given the modelling setup and equifinality threshold, unless/until additional data are used to reject or constrain them, which argues against a probability- or likelihood-based interpretation of the flux maps.

### 4.3 Class III

This class (Figures 3C) is an extension of Class II to three active fluxes, i.e. all three runoff fluxes can make noticeable contributions to simulating the observed flow, albeit with INFexc being smaller than the other two. For the strict case of acceptability (Figure 3-C1), $0.74 \leq$ Ensemble-NSE $\leq 0.78$, there exists an extreme model run with almost 95% contribution form INT & SATexc and another with almost 80% contribution from BAS. INFexc contributes up to around 15%. For the relaxed threshold (Figure 3-C2), the range of all fluxes increases, most notably INFexc, which is the least constrained (being <15% at the strict threshold). For both cases of thresholding, particularly for the relaxed one, the flux contribution of high-performing model runs (red points) are widely spread on the flux map, indicating a high degree of flux equifinality even for the highest performing model runs.

### 4.4 Class IV

This class (Figures 3D) is an extension of Class III, i.e. all three fluxes can vary widely. Even for the strict threshold, there are 1270 acceptable model runs with a moderately wide range ($\geq$ 50% variation) of possible flux contributions as shown in Figure 3-D1 (compare this case with Figure 3-B1). A key difference to the other classes is that INFexc is as variable as the other fluxes. In the case of the relaxed threshold, the cloud fills almost the entire space of the flux map (lower triangle), signifying a very high degree of flux equifinality. All three runoff fluxes vary around at least 90% of flux contributions. In other words, almost *any* combination of runoff flux (volumetric) contribution could lead to a similar model performance—all flux combinations are plausible/feasible.

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To further illustrate Class IV, Figure 4 presents an extreme case. Even for a threshold as strict as 0.99 × SCE-NSE and as few as 287 equifinal runs (which is close to the number of equifinal runs in the case of strict thresholding in Class I with a constrained flux map, Figure 3-A1), acceptable fluxes are remarkably scattered—occupying about 25% of the flux map plane, shown in Figure 4-A. Even within 1% of SCE-NSE significant differences in the dynamics of model runoff fluxes emerge. The flux map is almost space-filled even for the strict threshold, with more than 69,000 equifinal model runs (Figure 4-B). This shows an extraordinary degree of flux equifinality compared with previous cases. For such a degree of flux equifinality, even $10^5$ thousand model runs were enough to achieve a space-filling flux map at the relaxed threshold (Figure 4-C). Given that the SCE-NSE for this catchment is higher than the previous cases (0.81), one cannot simply associate the flux equifinality with the model performance.

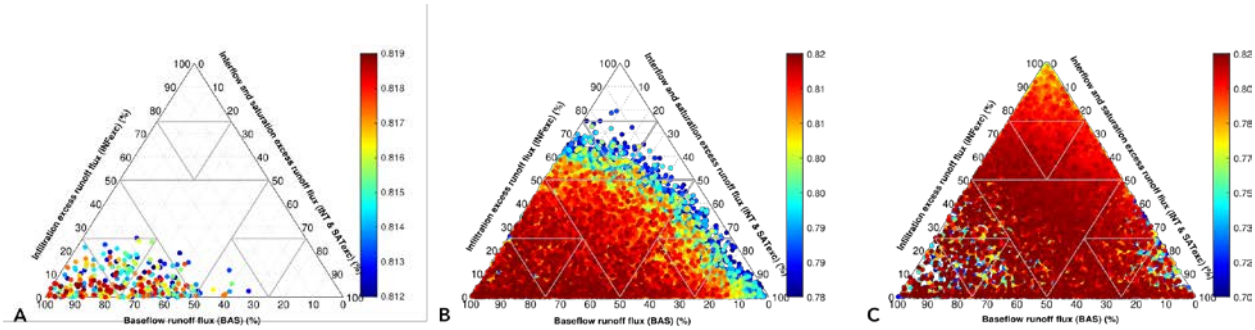


**Figure 4**. Class IV flux maps for very strict threshold (0.99×SCE-NSE=0.80 ≤ Ensemble-NSE=0.80 ≤ SCE-NSE) with 287 equifinal simulations (A), strict threshold (0.95×SCE-NSE=0.77 ≤ Ensemble-NSE ≤ SCE-NSE) with 69,090 equifinal simulations (B), and relaxed threshold (0.85×SCE-NSE=0.69 ≤ Ensemble-NSE ≤ SCE-NSE) with 49,591 equifinal simulations only from $10^5$ simulations (C). Catchment summaries are presented in Table 1.

## 5 Discussion

### 5.1 Flux mapping and model evaluation: flux space vs. parameter space

A striking dimension of the results is the wide range of model internal dynamics that emerges from a similar level of model performance for catchments with a reasonably constrained range of physiographic characteristics, regardless of the thresholding and number of equifinal model runs. The different patterns/degrees of flux equifinality range from very constrained to almost space-filling flux maps. Such new insights into model behaviour that flux mapping provides, cannot (easily) be characterised by common model evaluation tools, like dotty plots and parameter distributions. The dotty plot is a tool to visualise model parameter equifinality and (in)sensitivity, and the statistical distribution of parameter values (commonly presented as marginal distributions) is a probability-based tool for expressing model parameter uncertainty.

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While dotty plots and parameter distributions are useful tools, they do not sufficiently characterise the model behaviour, particularly its internal dynamics and process-representation; hence the flux map is a valuable complement to these tools. For instance, the differences in model behaviours for the aforementioned Cases I-IV are not discernible from the marginal distribution of model parameters (Figure 5) nor the dotty plots (supporting information Table S1).

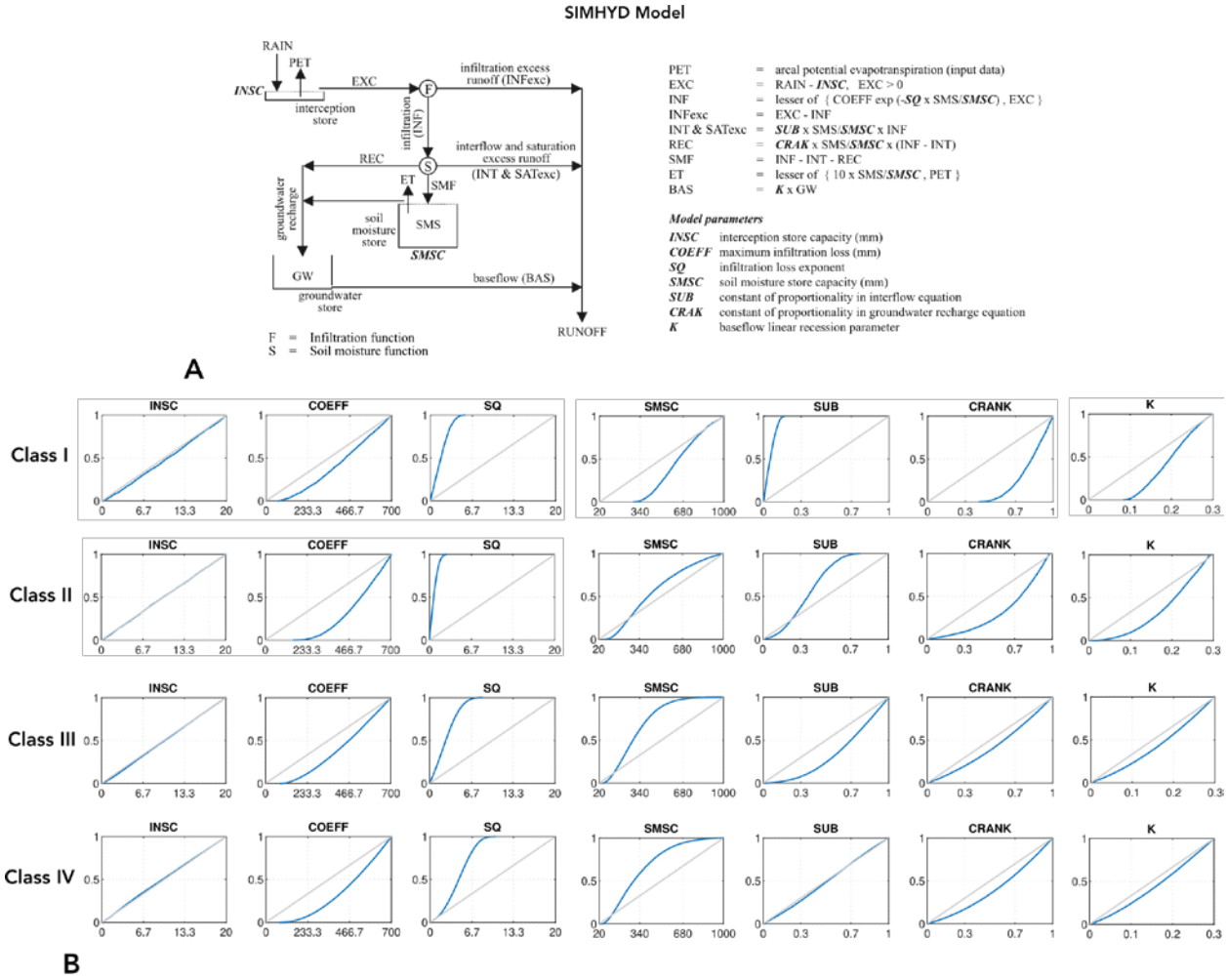


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**Figure 5**. (A) Schematic illustration of the SIMHYD model structure together with the description of the model's internal fluxes and parameters (derived from Peel et al., 2000). (B) Marginal (cumulative) distribution of model parameters (grey is the prior and blue is the posterior distributions) corresponding to the Classes I-IV flux maps (excluding the extreme case of Class IV) in the Results section, for the relaxed threshold (0.85 × SCE-NSE).

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Figure 5 presents the marginal distributions of model parameters corresponding to the example catchments in Figure 3. Comparing Figures 3 and 5 shows that despite vastly different flux maps, the marginal distributions of the influencing parameters can be similar, and therefore it would be difficult to translate the changes in distribution into flux dynamics. For instance, parameter distributions of both Classes III and IV (Figure 5-B) are almost identical except for parameter SUB, which controls the INT & SATexc flux; while Figure 3 clearly shows there are profound differences between the flux maps of these Classes.

To explore more complex interactions of model parameters and their implication on model fluxes, we discuss further a few more cases. While given the model structure some parameters are not influencing the partitioning of runoff fluxes (e.g. K only determines the timing of the baseflow reservoir), other parameters are strongly related to flux partitioning. For instance, both INSC and COEFF influence infiltration excess runoff; but INSC is almost identical across all cases hence not informative, and COEFF is very similar between Classes I, III, and IV. When parameter SUB, as a control of INT & SATexc flux, is highly constrained (Class I) the BAS flux is also constrained; and as the SUB marginal distribution becomes more uniform (towards Class IV) the BAS flux becomes less constrained. That said, while BAS flux is (almost) equally variable for both Classes III and IV (varying between 0 to 100%), the corresponding marginal distributions of SUB parameter are different. This is due to the strong interaction of influencing parameters, as model fluxes are usually controlled by more than one parameter. The bottom line is, given the often complex and nonlinear interaction between model parameters, even in the case of influencing parameters, it is still very difficult to evaluate the impact of parameter distributions or their changes from one case (e.g. catchment, model structure, etc.) to another on flux dynamics (partitioning/contributions) in particular, and model process-representation in general. Hence, it is difficult—if not impossible—to infer model internal dynamics from parameter marginal distributions and/or their changes. It is instead much easier to map the model behaviour into the flux space, i.e. flux mapping. In technical terms, flux mapping is a nonlinear transformation of the model response surface from the parameter space into the flux space. Within parameter uncertainty estimation methods, *modelling uncertainties*—the interplay between data information content, modelling framework and model structure, performance metrics, and modeller's decisions/understanding—are lumped into and evaluated within the parameter space. Flux mapping can illustrate the impact of *modelling uncertainties*, regardless of the source and nature, on model internal behaviour and process-representation.

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In this study, flux maps could be interpreted as a new visualisation of parameter equifinality within the model flux space. Although in this study we only perturbed model parameters to explore the dynamics of internal fluxes, other model components could be taken into account (e.g. using an ensemble of model inputs or various scenarios of boundary conditions, as discussed in section 2) to generate an ensemble of model runs. No matter how the ensemble of model runs is produced, we could use flux maps (i.e. the particular facet of model internal fluxes of model-equifinality) to explore, summarise, and visualise model internal behaviour. It should also be mentioned that the overall pattern of the point cloud of flux maps is independent of the thresholding, the number of acceptable model runs, and/or how constrained the parameter distributions are. Flux maps of each modelling example, for different thresholdings are presented in Table S1. The bottom line is that equifinal model fluxes, compared to equifinal model parameters, provide a more insightful basis to generate and explore multiple working hypotheses based on model process-representation.

Furthermore, runoff flux space has lower dimensions than parameter space. For instance, in the case of SIMHYD, visualising and investigating a 3-D runoff flux space instead of a 7-D parameter space is more convenient. Moreover, flux mapping is extendable to any combination of model fluxes. It is particularly of interest for fluxes of physical significance such as actual evaporation. Although in this work model realisations are the product of perturbing model parameters, other components of the model could also be used for generating flux maps, e.g. model inputs and/or input/boundary conditions.

### 5.2 Flux mapping, process representation, and multiple working hypotheses

Flux space also has the advantage over parameter space of being (more) physically meaningful/relatable. *Modelling uncertainties* in general, and parameter uncertainty in particular, are the result of various types/sources of uncertainties. However, placing the emphasis only on parameter distributions, i.e. uncertainty estimation *as if* all uncertainties are aleatory (due to variability and randomness) (Beven, 2016), neglects the crucial role of epistemic uncertainties. But, within the flux mapping approach, we deal with and can pose questions of an epistemic nature. For instance, the flux map of Class I (Figures 3A) indicates a baseflow-dominant system, a hypothesis to be further tested across multiple model structures and/or performance metrics (error/efficiency metrics and hydrological signatures). To see whether different modelling setups (given modeller's judgements/decisions) are in (dis)agreement with each other and to what extent; and eventually pose an essential question of conceptual modelling, i.e. how well model output (and internal behaviour) corresponds to catchment response (and its internal processes). In other words, changing the emphasis of model-equifinality from model parameters to fluxes enables us to develop MWH that are process-based and testable both across different model-based hypotheses as well as our understanding of real-world catchment processes. It should be noted that defining the flux space—i.e. selecting a subset of the model's entire flux space for flux mapping—is closely related to the model structure and nature of the hypotheses of interest; i.e., what processes are represented in the model or meant to be examined.

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The importance of independent estimates of *catchment* internal fluxes/storages and their exploitation as diagnostic tools has been discussed in the literature (for further details see Clark et al., 2011). However, evaluating model behaviour in terms of their internal fluxes—model flux equifinality—has received little attention compared with parameter equifinality, although it can be a valuable source of insight. For instance, Guo et al. (2017) presented an example of evaluating the relative realism of evapotranspiration (ET) process representation within three conceptual rainfall-runoff models, by comparing the simulated actual ET (AET) with measurements. They observed some unrealistic behaviour in the simulated AET. Given that ET process representation can have significant impacts on the sensitivity of runoff projections under climatic changes, assessing the realism of model AET flux is essential. Li et al. (2015) also demonstrated that while a conceptual model can generally simulate the total observed streamflow well for various catchments with different characteristics, it may fail to match the observed baseflow and quickflow fluxes. Such unrealistic internal model behaviour/dynamics are not easily discernible from model performance solely or parameter distributions (if at all), but are crucial for rejecting unfit model runs, improving the model realism, and reducing model structural and prediction uncertainties.

Furthermore, if additional measurements are available, such as flow path information (baseflow measurements/estimates), the conflicting modelling scenarios (as MWH) could then be evaluated in terms of their process-representation. That is, which of the so-called equifinal fluxes should be rejected as not physically plausible/significant (less realistic), and which of them could be seen as plausible working hypotheses. Therefore, the curious follow up question would be to investigate the relationship between catchment characteristics and flux map patterns; Which catchment characteristics are controlling/determining flux maps. For instance, other hydrologic variables such as filed data on surface runoff measurement and soil moisture (Western & Grayson, 1998), water quality, e.g. salt load (Nathan & Mudgway, 1997), isotopes (Beria et al., 2018; Kendall & McDonnell, 1998) may provide diagnostic information about the sources of dominant flow processes that could be used to further evaluate/constrain model fluxes. Also, integrating hard and soft data (Winsemius et al., 2009) and diagnostic approaches (e.g. hydrological signatures) could provide valuable sources of information to understand the interplay between flux maps and catchment dynamics particularly dominant processes. While knowledge about dominant processes within the catchment system is a major control for developing/improving models (Seibert & McDonnell, 2002), the modeller's personal judgment and experience is crucial in deciding the dominant processes (Holländer et al., 2009). So, combining hydrologic signatures with expert knowledge of mechanisms and processes of real-world catchment systems, i.e. expert elicitation, we can improve model realism and process-representation by imposing relative model parameter/flux constraints (Euser et al., 2013; Fenicia et al., 2014; Gharari et al., 2014; Hrachowitz et al., 2014).

We can also further assess how modifying different model components (e.g. interception, evaporation, and soil water routines) can influence and hopefully improve the flux map pattern. Therefore, flux mapping has an *exploratory* power to evaluate the impact of *modelling*

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*uncertainties* on model behaviour; to explore model *capacity* for process representation, at least partly and in a lumped way. This can pave the way to go beyond only evaluating model performance (i.e. model *capability* for yielding a high value of some error metrics), possibly together with some estimation of parameter uncertainties, based on only the model *output*. We emphasise that flux mapping alone cannot improve model realism, and additional information is required for refining models. Also, flux mapping provides *explanatory* opportunities to postulate hypotheses of possible explanations of real-world processes (e.g. catchment processes and their changes) based on the (internal) behaviour of their corresponding conceptual models under all *modelling uncertainties*. The relationship between different modes of model process-representation (i.e. model-equifinality) and catchment internal processes is a crucial question and remains an open one, which can only be addressed by bridging the gap between modelling and experimental hydrology (Seibert & McDonnell, 2002). That said, various catchment internal processes are unknown or unknowable (knowledge uncertainty). There are myriad (ever-evolving and dynamic) flow paths in any real catchment that we cannot expect conceptual models to represent them. Such epistemic uncertainties and hence modelling limitations may be *a* contributing factor to model-equifinality. It is unclear to what extent a projected flux equifinality resembles the plausible hypotheses of internal processes of a given catchment, and to what extent it is a modelling artefact due to *modelling uncertainties*. For instance, to what extent a constrained or space-filling flux map is due to catchment characteristics or due to modelling setup. What occurred in reality in a particular period would be mapped to a single unknown *true point* on the flux map. Model-equifinality, e.g. flux equifinality, results in a point cloud which does not necessarily encompass the *true point* (i.e. reality). What we can hope for is to refine our hypotheses while encompassing the *truth* by improving model realism—by improving model structures, evaluation schemes, data quality and accounting for their uncertainties—and hence reducing knowledge uncertainty.

### 5.3 Equifinality, hydrological systems, and beyond

The theoretical framework presented, and its implications for model evaluation (going beyond model *output* and accounting for model *behaviour* under *modelling uncertainties*) and hypothesis generating, could be further extended to other domains. It could also be used to improve understanding/modelling in data-poor catchments/regions (Davtalab et al., 2017) and in regional generalization (also known as regionalisation or prediction in ungauged basins) (Peel et al., 2000; Reichl et al., 2006). Moreover, although the proposed theoretical framework and flux mapping method are mainly discussed within the context of hydrological systems, it can be further extended to any field of scientific modelling concerned with understanding/modelling open complex systems in the face of uncertainties. Real-world processes, their perceptual, and conceptual models are all open systems and hence give rise to equifinality. Therefore, it is important to go beyond evaluating *only* the (equifinality of) model output and account for model fluxes (or other facets of model-equifinality) as well; particularly physically meaningful fluxes of conceptual models that may be used in e.g. data assimilation(Alvarez-Garreton et al., 2014;

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Teweldebrhan et al., 2018a) and flood forecasting (Alvarez-Garreton et al., 2015), catchment classification (Kelleher et al., 2015; Knoben et al., 2018; Sawicz et al., 2014), socio-hydrological systems (Di Baldassarre et al., 2015; Khazaei et al., 2019; van Emmerik et al., 2014; Westerberg et al., 2017), environmental (Chowdhury et al., 2016) and ecological systems (Luo et al., 2009), natural hazard and risk assessment (Beven et al., 2017), decision making under uncertainty (Madani & Lund, 2011; Maier et al., 2016), agent-based modelling (Billari et al., 2006; Madani et al., 2014), sustainability transitions (de Haan et al., 2016; Moallemi & Köhler, 2019) and exploratory modelling (Kwakkel & Pruyt, 2013; Moallemi et al., 2017; Moallemi & Malekpour, 2017) under deep uncertainty (Haasnoot et al., 2013; Maier et al., 2016; Moallemi et al., 2018), demand modelling/forecasting in energy (van Ruijven et al., 2010), and traffic (Flyvbjerg et al., 2006; Saberi et al., 2018) and network design (Chen et al., 2011).

## 6 Conclusion

We outlined different facets of model-equifinality in the context of hydrological modelling. We developed a novel model evaluation scheme, *Flux Mapping*, based on a particular facet of model-equifinality namely model internal fluxes. We demonstrated how flux mapping can give new insights into model behaviour that cannot be inferred from conventional evaluation methods. That is, even within a very narrow margin of model error/performance, different modes of model response, i.e. internal runoff generating fluxes of the model, can be equally active. In other words, different dynamics of model internal fluxes can equally reproduce a given observed hydrograph within a narrow margin of model error. Flux Mapping can be extended to any field of scientific modelling dealing with conceptual modelling of open complex systems under uncertainty. We argued that equifinality plays a central role in scientific modelling, particularly within the paradigm of multiple working hypotheses.

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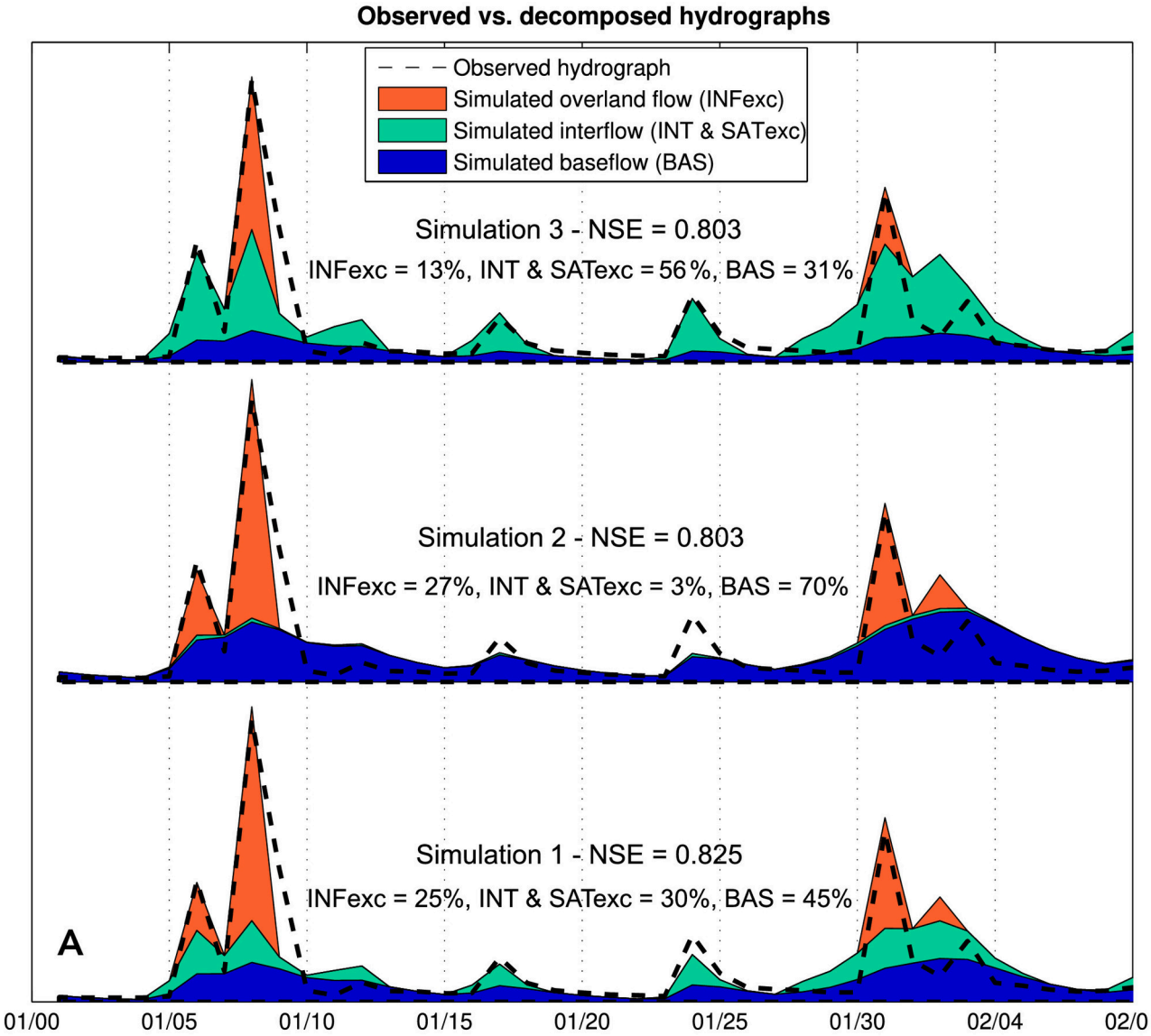


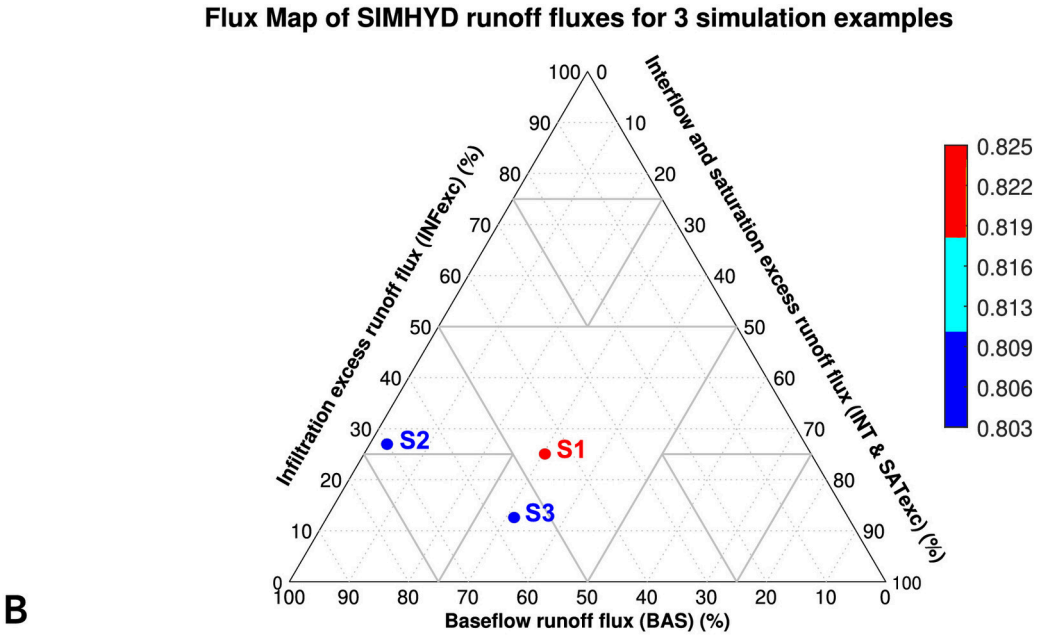


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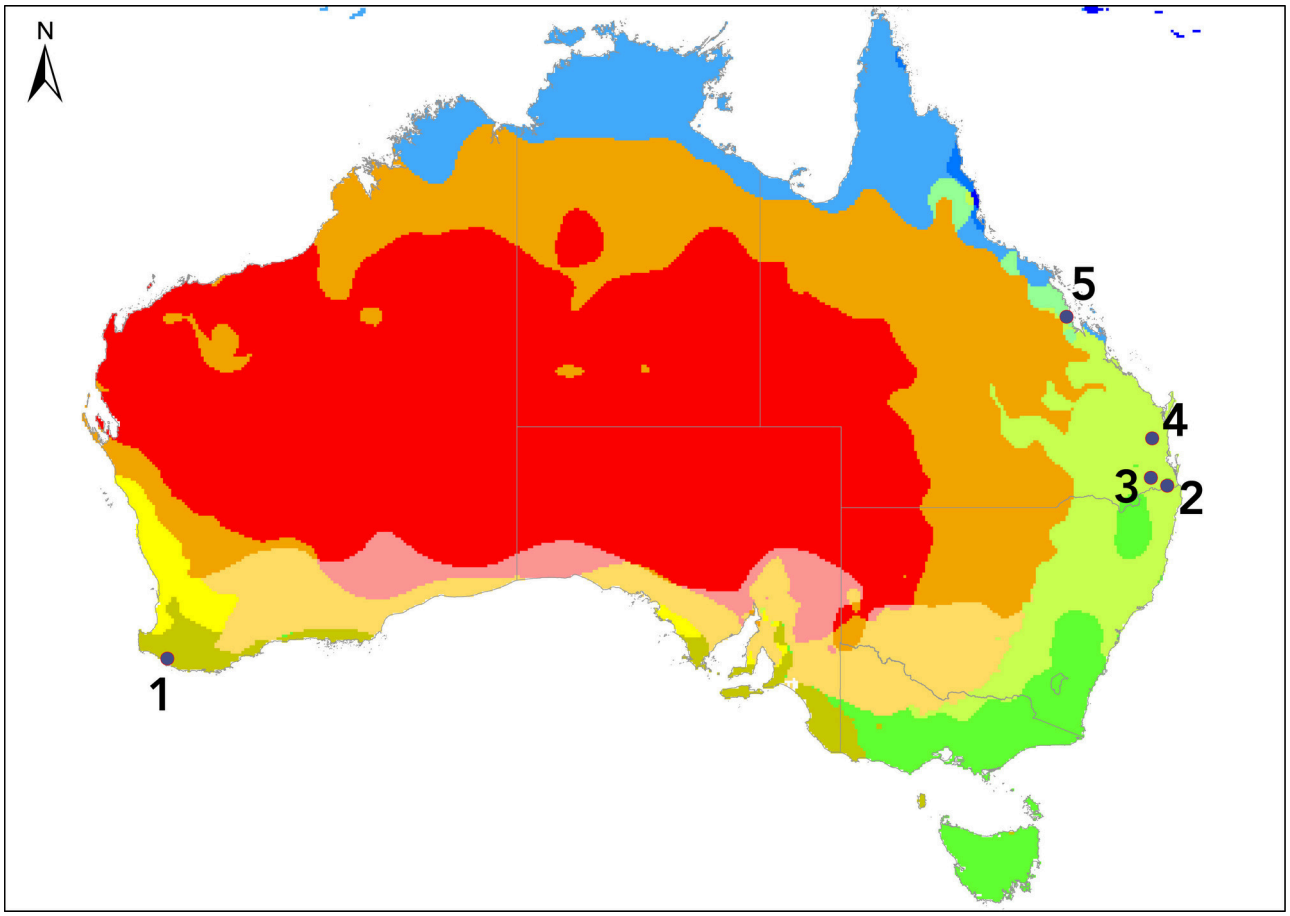


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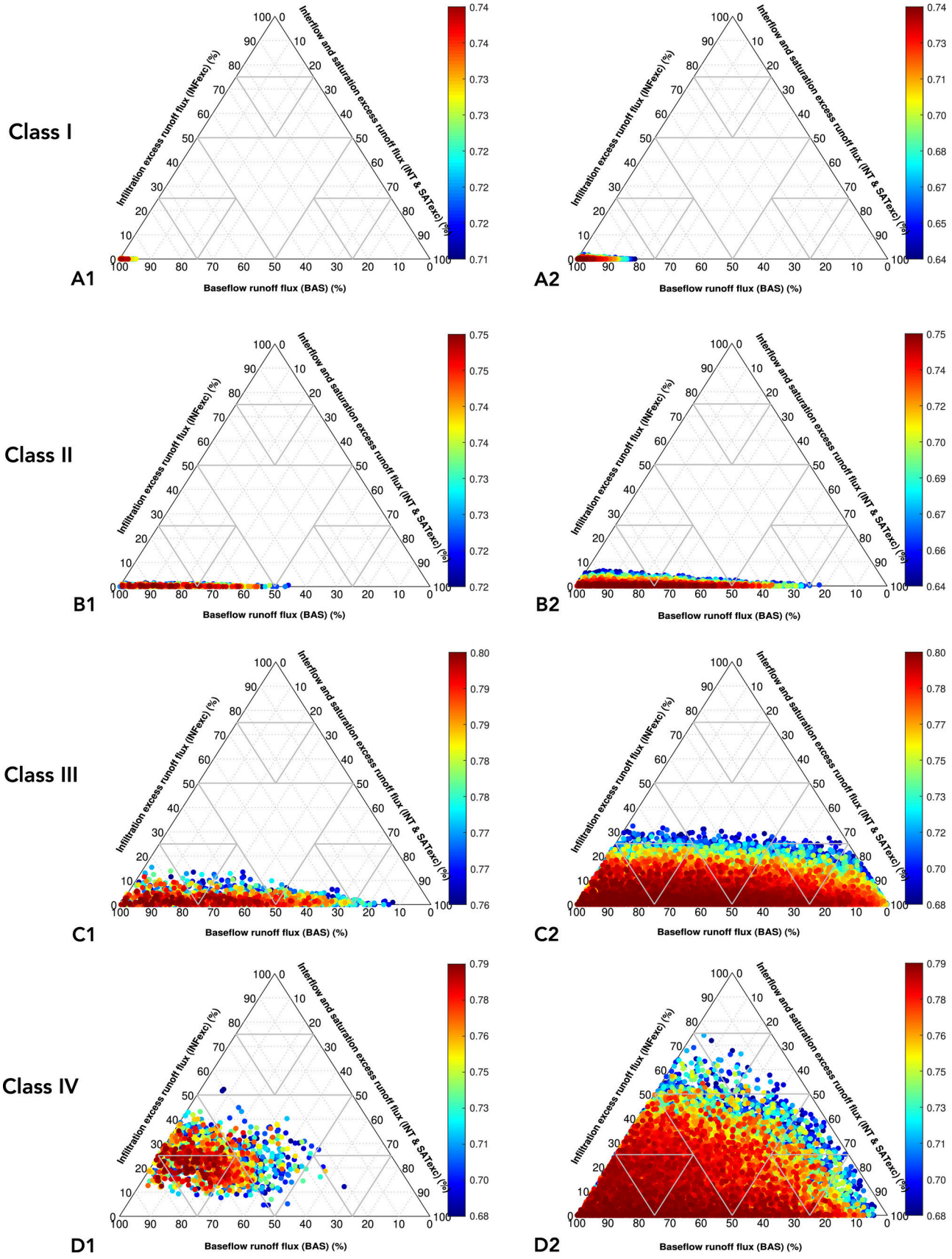


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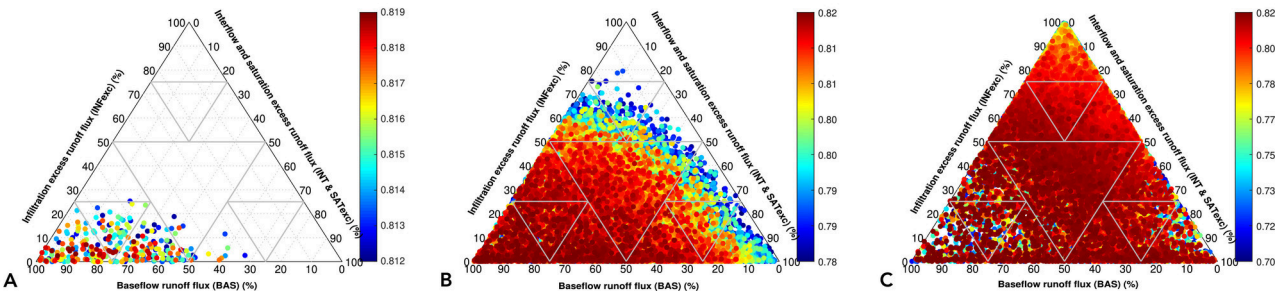


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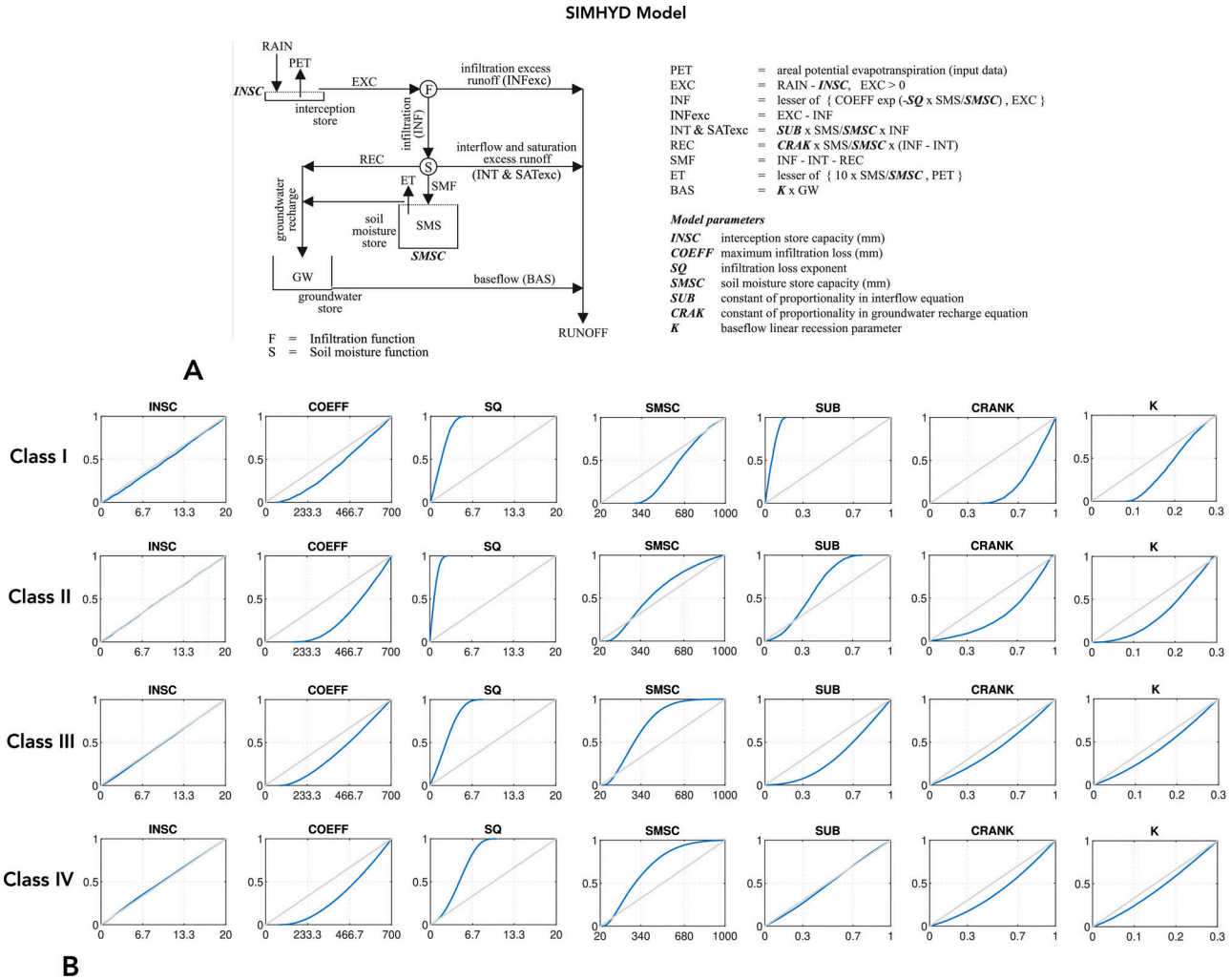


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