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Semi-analytic modelling of Pop. III star formation and metallicity evolution – I. Impact on the UV luminosity functions at $z = 9–16$

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ABSTRACT

We implemented Population III (Pop. III) star formation in mini-haloes within the MERAXES semi-analytic galaxy formation and reionization model, run on top of a N -body simulation with $L = 10 h^{-1}$ cMpc with 2048^3 particles resolving all dark matter haloes down to the mini-haloes ($\sim 10^5 M_\odot$). Our modelling includes the chemical evolution of the IGM, with metals released through supernova-driven bubbles that expand according to the Sedov–Taylor model. We found that SN-driven metal bubbles are generally small, with radii typically of 150 ckpc at $z = 6$. Hence, the majority of the first galaxies are likely enriched by their own star formation. However, as reionization progresses, the feedback effects from the UV background become more pronounced, leading to a halt in star formation in low-mass galaxies, after which external chemical enrichment becomes more relevant. We explore the sensitivity of the star formation rate density and stellar mass functions to the unknown values of free parameters. We also discuss the observability of Pop. III dominated systems with *JWST*, finding that the inclusion of Pop. III galaxies can have a significant effect on the total UV luminosity function at $z = 12–16$. Our results support the idea that the excess of bright galaxies detected with *JWST* might be explained by the presence of bright top-heavy Pop. III dominated galaxies without requiring an increased star formation efficiency.

Key words: stars: Population III – galaxies: formation – galaxies: high-redshift.

1 INTRODUCTION

The first episodes of star formation likely occurred at redshift 30–40 inside low-mass ($10^{5–7} M_\odot$) haloes with a pristine chemical composition (metal-free or extremely metal-poor). These environments were responsible for the chemical enrichment of the intergalactic medium (IGM) leading to the Pop. III/Pop II transition at redshift 15–10. However, due to the low mass and the high- z , the study of Pop. III star formation in mini-haloes is challenging both in terms of observations and simulations (see Klessen & Glover 2023 for a recent and comprehensive review).

Even with the launch of *JWST*, we do not have confirmed observations of Pop III stars and only a few potential candidates (Welch et al. 2022; Maiolino et al. 2023). As pointed out by Trussler et al. (2023), a direct detection of a Pop. III galaxies will be extremely challenging, as in the best-case scenario, hundreds of hours of integration time are needed in order to detect an unlensed Pop. III system with 5σ confidence. There are a number of Pop. III star formation simulations at different scales. Hydrodynamical simulations that follow the cooling of gas in a single pristine or very metal-poor cloud suggest that the inefficient cooling due to the lack of metals might favour an initial mass function (IMF) that is shifted to larger masses (e.g. Bromm, Coppi & Larson 1999; Hirano

et al. 2014; Stacy, Bromm & Lee 2016; Chon, Omukai & Schneider 2021); however, there is no general consensus (e.g. Wollenberg et al. 2020; Jaura et al. 2022; Prole et al. 2022 predict IMF shifted to lower masses). Simulations at larger scales (≥ 1 cMpc) are instead used to follow the global evolution of Pop. III stars with redshift and their impact on the cosmic metal enrichment and reionization. In the last decade, many of these simulations have been performed both with hydrodynamical (Pallottini et al. 2014; Xu et al. 2016; Jaacks et al. 2018; Sarmiento, Scannapieco & Cohen 2018; Skinner & Wise 2020; Schauer et al. 2021; Correa Magnus et al. 2023; Venditti et al. 2023; Yajima et al. 2023) and semi-analytical codes (Trenti, Stiavelli & Shull 2009; Crosby et al. 2013; Mebane, Mirocha & Furlanetto 2018; Visbal, Haiman & Bryan 2018; Visbal, Bryan & Haiman 2020; Magg et al. 2022; Trinca et al. 2022; Feathers et al. 2024; Hegde & Furlanetto 2023). In this work, we chose to use the semi-analytical model of galaxy formation MERAXES (Mutch et al. 2016, M16 hereafter) within a simulation that allows us to resolve all the mini-haloes down to a few $10^5 M_\odot$ in a simulation of $L = 10 \text{ Mpc } h^{-1}$. The size of this simulation is not large enough to be representative of the Universe (we will miss the most massive galaxies). However, the scales are large enough to investigate the impact of the main physical processes on the Pop. III star formation. We incorporated a number of new physical processes that are relevant to Pop. III star formation in mini-haloes including: (i) molecular hydrogen cooling functions for mini-haloes, (ii) baryon-dark matter streaming velocities, (iii) photodissociation of H_2 molecules from

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the Lyman–Werner background, and (iv) the chemical evolution of the intergalactic medium. This latter effect has been implemented assuming that metals are released through supernova explosions and within a bubble that expands accordingly to the Sedov–Taylor model (the approach is very similar to the analytical calculation shown in Furlanetto & Loeb 2003). We found that these bubbles are generally small and that they roughly agree with the previous estimate by Trenti et al. (2009), with typical radii of 150 kpc at $z = 6$. The implementation of both internal and external metal enrichment allows us to understand whether a galaxy will form Pop. III or Pop. II stars and thus quantify the impact of Pop. III galaxies on the total luminosity function at $z \geq 5$. This paper is structured as follows:

In Section 2, we present the new physics implemented in MERAXES. In Section 3, we show the main global properties of the Pop. III star formation across cosmic history discussing which parameters have a stronger impact on the global star formation history and on the metallicity of the IGM. In Section 4, we discuss the SED evolution of Pop. III galaxies and the UV luminosity functions at $z = 9$ –16 for different Pop. III IMFs. Finally, we discuss our main results and conclusions in Section 5.

2 POP. III STAR FORMATION IN MERAXES

The semi-analytical model MERAXES was first developed by M16, Qin et al. (2017), and Qiu et al. (2019) in order to study galaxy formation and growth through the Epoch of Reionization. MERAXES assumes that all the galaxies form in a previously chemically enriched Universe and inside atomic cooling haloes. Such an approximation does not allow us to study the first episodes of star formation that mostly occurred in mini-haloes when the Universe did not have any metals. The version of MERAXES presented in this work allows us to compute the physics of the first episodes of star formation from the initial molecular cooling of the gas to the external metal enrichment from the supernova feedback. As in the previous work, MERAXES is coupled to the reionization so that all the radiative backgrounds are computed in a self-consistent way from the galaxy properties. This has been done by implementing a modified version of 21cmFAST (Mesinger, Furlanetto & Cen 2011) that includes the local ionizing UV background from Sobacchi & Mesinger (2014) and the X-ray heating (Balu et al. 2023). In this version, we also included the Lyman–Werner background.

2.1 High-resolution N -body simulation

The updates to MERAXES for Pop. III necessitate high mass and spatial resolution. For this purpose, we introduce L10_N2048 (hereafter L10) from the *Genesis* suite of dark matter only N -body simulations. L10 is a periodic cubical simulation of side $10 h^{-1}$ Mpc and consists of 2048^3 dark matter particles of mass $m_p = 9.935 \times 10^3 h^{-1} M_\odot$ resulting in a halo mass resolution of $\sim 3.18 \times 10^5 h^{-1} M_\odot$ (based on a minimum of 32 particles per halo). The simulation, run using the SWIFT (Schaller et al. 2018) cosmological code, evolves these dark matter particles from $z = 99$ down to $z = 5$. The haloes were identified using the friends-of-friends phase space halo-finder VELOCIRAPTOR (Elahi et al. 2019a) and the merger trees were constructed using TREEFROG (Elahi et al. 2019b). We note that the mass resolution achieved in this simulation allows us to resolve all the mini-haloes below $z \sim 30$ and is the highest resolution on which MERAXES has been run. The output trees of the N -body simulation used in this work are available on Zenodo at Balu et al. (2024).

2.2 Molecular cooling

The first process in order to enable star formation is the cooling of the gas. For dark matter haloes with $T_{\text{vir}} \geq 10^4$ K, the main coolant is the atomic hydrogen, while in mini-haloes ($10^3 \text{ K} \leq T_{\text{vir}} < 10^4 \text{ K}$), the cooling occurs via roto-vibrational transitions of molecular hydrogen (e.g. Tegmark et al. 1997). For the details on how the cooling of the gas is implemented in MERAXES, we refer the reader to M16; in this section, we only highlight the main differences between the atomic and the molecular cooling.

As in M16, we compute the ratio of the specific thermal energy to the cooling rate per unit volume:

$$t_{\text{cool}}(r) = \frac{1.5 \bar{\mu} m_p k T}{\rho_{\text{hot}}(r) \Lambda(T, f_{\text{H}_2})}, \quad (1)$$

where $\rho_{\text{hot}}(r)$ is the gas density profile (we assume a singular isothermal sphere), k is the Boltzmann constant, and T is the temperature of the gas (which we set to be the virial temperature of the halo). M16 included only atomic cooling haloes. Thus, they set the mean molecular weight $\bar{\mu} = 0.59$ assuming a fully ionized gas and the cooling function $\Lambda(T)$ in units of $\text{erg cm}^{-3} \text{ s}^{-1}$ from Sutherland & Dopita (1993). For mini-haloes, we instead set $\bar{\mu} = 1.22$ (fully neutral gas) and implement the molecular hydrogen cooling functions $\Lambda(n_{\text{H}}, T)$ from Galli & Palla (1998). This choice is valid as long as we assume that the cooling inside mini-haloes occurs only due to H_2 . This may not be valid as, if a mini-halo is chemically enriched with metals by a nearby halo, metals are much more effective in the cooling of the gas (e.g. Nebrin, Giri & Mellema 2023). However, as we will show in Section 3, this enrichment is almost ineffective at $z > 10$. The molecular cooling function Λ depends on the gas density of the halo (which can be directly computed for each galaxy assuming an isothermal sphere) and on the molecular hydrogen fraction f_{H_2} . For the latter we assumed a fixed value of 0.1 per cent, which is consistent with results from Nebrin et al. (2023) for haloes of $T_{\text{vir}} \simeq 5 \times 10^3$ K at $z = 15$ –20.¹ As in M16, the cooling time is used to find a cooling radius that determines the amount of gas that is cooled down.

2.3 Streaming velocities

As a first approximation, gas in a mini-halo can start to cool down the gas once it reaches the virial temperature of $\simeq 10^3$ K. From Barkana & Loeb (2001), adopting $\mu = 1.22$ for a fully neutral gas, this requirement would correspond to a minimum virial mass of (Visbal, Haiman & Bryan 2015):

$$M_{\text{min}, \text{H}_2} = 2.5 \times 10^5 \left(\frac{26}{1+z} \right) M_\odot. \quad (2)$$

However, there are a number of effects that can decrease the amount of molecular hydrogen present in the halo, reducing the cooling efficiency and ultimately increasing the minimum virial mass of a halo capable of cooling (see Nebrin et al. 2023 for an extensive discussion and comparison between results found in different simulations).

A non-radiative process that can delay the gas cooling in very low-mass haloes is the streaming velocity between baryons and dark matter (Tselikhovich & Hirata 2010). This effect is a consequence

¹The exact value of f_{H_2} depends on the virial mass of the halo, redshift and the time available for H_2 formation in the minihalo (which is likely to be a multiple of the free fall time). To compute the exact value of f_{H_2} is beyond the aim of this work, hence we chose an average value.

of the different decoupling of baryons and dark matter particles from photons that results in a velocity difference between the two species of v_{bc} that can be expressed as a constant multiple of the root-mean-square (rms) streaming velocity $\sigma_{bc} = 30 \times (1 + z)/1000 \text{ km s}^{-1}$. The presence of a relative motion between baryons and dark matter particles will make it harder for baryons to fall into the potential wells of dark matter haloes, delaying the accretion and, hence, the cooling of the gas in mini-haloes. The main outcome of this physical process is to delay the very first episodes of star formation around $z \sim 40$. Throughout this work, we implemented the effect of the streaming velocities as per other semi-analytical models based on a fitting function found by Fialkov et al. (2012), which is calibrated to reproduce the results of the hydrodynamical simulations of Greif et al. (2011) and Stacy, Bromm & Loeb (2011):

$$V_{\text{cool,H}_2} = (a^2 + (bv_{bc})^2)^{0.5}, \quad (3)$$

where $a = 3.714 \text{ km s}^{-1}$ and $b = 4.015 \text{ km s}^{-1}$. Equation (3) provides the minimum circular velocity that a halo needs to have in order to have enough H_2 to cool down the gas. $V_{\text{cool,H}_2}$ can be easily converted into a virial mass $M_{\text{cool,H}_2}$ using the formula in Barkana & Loeb (2001). In this work, we fixed $v_{bc}(z) = \sigma_{bc}(z)$ and we assumed this value for the entire box.²

2.4 LW background

A self-consistent model of star formation in mini-haloes must consider the photodissociation of H_2 from UV photons in the Lyman–Werner (LW) band ([11.2–13.6] eV). LW photons destroy H_2 and thus prevent mini-haloes gas from cooling (Haiman & Bryan 2006). We implement this effect by changing the minimum mass for molecular cooling using the fitting from Visbal et al. (2015):

$$M_{\text{crit,MC}} = M_{\text{cool,H}_2} [1 + 22.87 \times J_{\text{LW}}^{0.47}]. \quad (4)$$

This critical mass only applies to minihaloes, which are below the atomic cooling halo mass threshold. In the absence of an LW background, this equation simply gives $M_{\text{crit,MC}}$ as defined in Section 2.3. J_{LW} is the LW flux in units of $10^{-21} \text{ erg s}^{-1} \text{ cm}^{-2} \text{ Hz}^{-1} \text{ sr}^{-2}$ that reaches the minihalo. LW photons have a mean free path of $\sim 100 \text{ Mpc}$, so each minihalo will be affected even by distant galaxies that formed at higher redshift. Thus, we modelled the LW background by integrating contributions across the cosmic history (see a similar approach in Qin et al. 2020 which is briefly summarized below).

As for all the radiative backgrounds in MERAXES, we follow an excursion-set formalism (Furlanetto, Zaldarriaga & Hernquist 2004), which counts the number of photons in a certain band in spheres of radius R centred at location and redshift (x, z) . We decrease the radius down to the size of the cell R_{cell} . At each of these locations, we compute the LW emissivity $\epsilon_{\text{LW}}(\mathbf{x}, z')$ using the spectral energy distributions from Barkana & Loeb (2005). These give $\frac{dn^i}{dv}$: the number of photons per solar mass per unit frequency for both Pop III and Pop II stars. We assume that LW photons are absorbed only at resonant frequencies (thus we are neglecting any absorption from H_2 in the IGM), where $\nu_n = \nu_{\text{LL}}(1 - n^{-2})$ and $\nu_{\text{LL}} = 3.29 \times 10^6 \text{ GHz}$ is the Lyman limit frequency. Under these approximations, we can compute the LW emissivity smoothed over R at redshift z and

location x for sources emitted at redshift z' as:

$$\epsilon_{\text{LW}}(\mathbf{x}, z' | z, R) = \sum_{i=\text{III,II}} \text{SFRD}^i \sum_{n=2}^{n_{\text{max}}(z)} \int_{\nu_{\text{max}}(\nu_n', \nu_{\text{LW}})}^{\nu_{n+1}} \frac{dn^i}{dv''} h dv''. \quad (5)$$

In the equation above, we directly link the star formation rate density (SFRD) for both Pop. III and Pop. II stars (which we can compute from MERAXES) to the LW emissivity summed over the Lyman series. This sum accounts for the resonances in the Lyman series (Lyman- n photons will be absorbed and re-emitted as a Lyman- α photon). Given the large mean free path of LW photons, we must also account for distant galaxies at higher redshift $z' > z$ with the redshifted spectrum $\nu' = \nu \frac{1+z}{1+z'}$. The sum of these two effects causes the peculiar shape of the LW spectrum (see fig. 2 in Qin et al. 2020). Following Barkana & Loeb (2005), we account for all the Lyman resonances with $n \leq 23$. Under these approximations, we can find the maximum redshift z_{max} from which a LW photon can reach z :

$$z_{\text{max}} + 1 = (z + 1) \frac{1 - (n + 1)^{-2}}{1 - n^{-2}}. \quad (6)$$

Finally, we need to convert the emissivity into a flux following (Qin et al. 2020):

$$J_{\text{LW}}(\mathbf{x}, z | R) = \frac{(z + 1)^3}{4\pi} \int_z^\infty dz' \frac{c}{dz'} \epsilon_{\text{LW}}. \quad (7)$$

The approach described above differs from the one in 21cmFAST only for the computation of the SFRD. In Qin et al. (2020), the SFRD is estimated from the density field and the collapsed fraction, while in this work, it is computed directly from MERAXES, which tracks the formation of each galaxy and its entire star formation history.³

Together with the LW background, the main radiative feedback that suppresses star formation is the UV photo-ionization (the ionizing UV background inhibits gas accretion in low-mass haloes Sobacchi & Mesinger 2013). We used the same prescriptions as in M16, which consists of reducing the baryon content through a baryon fraction modifier f_{mod} (that depends on the local ionizing rate and the time when the nearby IGM becomes ionized) that stops the gas infall. In difference from the LW feedback, the UV photo-ionization is relevant only during reionization ($z \leq 10$), and it also affects atomic cooling haloes as massive as $\sim 10^{9.5} M_\odot$.

2.5 Metal evolution

Once stars start to form in the Universe, they also explode as supernovae, releasing metals. Most of these will stay inside the same galaxy, contributing to the chemical enrichment of the galaxy itself. This process is commonly known as ‘genetic’ enrichment and is likely to be the main mechanism of chemical enrichment of the Universe. However, some of the metals escape their parent galaxy. In this case, they will pollute the nearby IGM, and if later a galaxy forms in a region where the IGM was enriched, the new galaxy will be pre-enriched with metals. This latter mechanism is referred to as ‘external’ metal enrichment (e.g. Pallottini et al. 2014; Smith

²This assumption is not entirely accurate as the streaming velocities are roughly constant up to a scale of a few Mpc while our box is larger than 10 Mpc. However, the effect of streaming velocities is dominant only at $z \geq 30$ before the first stars form, and the Lyman–Werner background is built up.

³In this work, we are not accounting for the self-shielding of H_2 , which acts against the H_2 photodissociation and thus might enhance the molecular cooling in mini-haloes (Hartwig et al. 2015; Schauer et al. 2021; Chiaki & Wise 2023) increasing the Pop. III SFRD (Feathers et al. 2024). Kulkarni, Visbal & Bryan (2021) provided a fitting formula for $M_{\text{crit,MC}}$ accounting for the H_2 self-shielding. Since this affects only the LW feedback, the combined effect of the LW background and the streaming velocities in Kulkarni et al. (2021) is not multiplicative as assumed in equation (4).

et al. 2015; Hartwig et al. 2018; Visbal et al. 2020; Yamaguchi, Furlanetto & Trapp 2023). Keeping track of the metallicity evolution of the Universe is crucial in order to put constraints on when the Pop. III/II transition occurred.

We account for both processes, and we are able to follow the metallicity evolution of the IGM. First, we choose a critical metallicity $Z_{\text{crit}} = 10^{-4} Z_{\odot}$ as the threshold value below which a galaxy will form Pop. III stars. All new galaxies, unless externally polluted, will accrete pristine gas (without any metals) onto the hot gas reservoir. This gas, once it cools, will provide the reservoir for the star formation. Hence, a galaxy that is not externally polluted will always form Pop. III stars for the first time. At each snapshot, we compute the metallicity of the cold gas reservoir from the amount of metals released by earlier supernovae and if this is higher than Z_{crit} , the galaxy will form Pop. II stars, otherwise it will form Pop. III.

While internal enrichment is the main mechanism that drives the Pop.III/II transition, some galaxies can be externally enriched through supernova winds originating in a nearby galaxy. Once several supernovae in a galaxy go off, they will form a ‘superbubble’ that will expand outside the galaxy escaping the binding energy of the dark matter halo. We followed the expansion in time of this ‘metal bubble’ using the analytic approximation in Dijkstra, Ferrara & Mesinger (2014):

$$r_{\text{bubble}}(t) = \left(\frac{\Delta E_{\text{SN}}}{m_p n_{\text{gas}}} \right)^{0.2} t^{0.4}. \quad (8)$$

All quantities that appear in this equation are computed in MERAXES. ΔE_{SN} is the total supernova energy released at a certain snapshot, and it is computed using the stellar mass that goes supernova in that snapshot multiplied by the supernova explosion energy (see equation 11 in M16). n_{gas} is the number density of the gas to which the bubble has expanded (while the bubble is smaller than the virial radius, this is the gas density of the galaxy; otherwise, the density of the IGM), and t is the time since the explosion occurred. We assume that all the supernova events will occur in the middle of the snapshot.⁴ Note that since MERAXES accounts for both contemporaneous and delayed supernova feedback (see more in M16), each galaxy has several bubbles associated with the same star formation episode. However, we consider only the largest of these bubbles so that each galaxy has only one associated bubble. Having calculated the bubble size, we can predict if a nearby galaxy will accrete pristine or enriched gas. In order to reduce the computational cost, we avoid computing the distance between all the pairs of galaxies and instead use the grid-based approach outlined below:

(i) Build a high-resolution grid with N_{grid}^3 cells smoothing the matter density grid from the N -body simulation. The size of the cell is chosen so that the volume of the cell is similar to the volume of the typical bubble at the end of the simulation ($R_{\text{ave, bubble}} \simeq 100$ ckpc, see Fig. 2). For our box, this requirement is satisfied when $N_{\text{grid}} = 128$. This ensures that the metal bubble will not overflow outside the pixel where it originates.

(ii) For each cell i , we compute the average metallicity $Z_{\text{IGM}, i}$ as the ratio between the sum of the metals ejected by all galaxies inside the cell and the total gas in the cell:

$$Z_{\text{IGM}, i} = \frac{\sum_j M_{\text{MetalsEj}, j}}{M_{\text{IGM}, i} + M_{\text{EjGas}, j} - M_{\text{gas}, j}}. \quad (9)$$

⁴This assumption is not self-consistent with the luminosity computation of Pop. III galaxies, which assumes stochastic Pop. III star formation (see Section 2.7).

Here, $M_{\text{IGM}, i} = \rho_{\text{crit}} \Omega_m (1 + \delta_i) f_b d^3$ is the total baryonic mass inside each cell, which depends on the average matter overdensity of the cell δ_i and the cell size d . M_{EjGas} and M_{gas} are, respectively, the total mass of the ejected gas and the bounded gas of each galaxy. We only let the galaxies with $r_{\text{bubble}} \geq 3 \times R_{\text{vir}}$ contribute to $M_{\text{MetalsEj}, j}$ and $M_{\text{EjGas}, j}$. For the computation of the metals ejected from Pop. II galaxies, we refer the reader to M16 and Qiu et al. (2019) and for Pop. III galaxies to Section 2.6.

(iii) For each cell i , we compute the volume fraction filled with metals (the metal filling fraction), summing the volume of the largest bubble surrounding each galaxy within the pixel and dividing by the cell volume. As above, we account only for those galaxies with $r_{\text{bubble}} \geq 3 \times R_{\text{vir}}$. This choice reflects the fact that a central galaxy needs to be surrounded by a bubble at least as large as its virial radius in order to pollute a nearby galaxy. The factor of 3 has been chosen given that the distance between two central galaxies in our simulation is always larger than three times the virial radius of the biggest galaxy.

Hence, the metal filling factor for the cell i is $Q_{\text{metal}, i} = \frac{\sum_j V_{\text{bubble}, j}}{V_i}$.

(iv) At the beginning of each snapshot, we assign the probability p for external metal enrichment to each galaxy inside the cell i . This probability will be given by the metal filling factor Q_i . This choice assumes that the galaxies are randomly distributed within each pixel. This assumption holds only if we use a high-resolution grid, where the pixel size is small enough such that clustering effects are negligible.

(v) We assign a random number m between 0 and 1 to each newly formed galaxy, and at each snapshot, we compare this random number to p . When the condition $m \leq p$ is satisfied, we label that galaxy as externally enriched, and it accretes enriched gas with a metallicity equal to the average metallicity of the cell that belongs to $(Z_{\text{IGM}, i})$. Furthermore, when a galaxy experiences a star formation episode, we enforce $p = 1$ (in this latter case, we know that this galaxy will be inside its own metal bubble and thus cannot accrete pristine gas). With this latter condition and internal enrichment, we effectively stop Pop. III star formation inside a galaxy after the first supernova episode.

We illustrate an example in Fig. 1, where we selected a 2D slice of our L10 box at $z = 10$ with a thickness of $0.078 h^{-1}$ cMpc. The red (blue) dots are the galaxies with $M_{\text{vir}} \geq 10^6 M_{\odot}$ (not) externally metal-enriched, while the green dots are previously formed galaxies with $r_{\text{bubble}} \geq 0.05 h^{-1}$ cMpc. For a better visualization, we zoomed into a slice with $0.24 h^{-1}$ cMpc on a side showing the actual size of the metal bubble (right plot). Inside this region, all the seven galaxies that formed inside the bubble are actually marked as externally enriched. At the same time, the five galaxies that are marked as not enriched lie outside the bubble, showing that the adopted approximation works quite well (see Appendix A for a more detailed discussion). This demonstrates that this method can reproduce the statistical properties of inhomogeneous metal enrichment. The main limitation of this technique is that we are not accounting for the overlap of the bubbles and thus are overestimating the metal-filling factor and underestimating the metallicity of those galaxies that are polluted from more than one galaxy. However, given the small size of the bubbles (see discussion in Section 3 and Fig. 2), this is not a major factor, especially prior to reionization. We note that the methodology shown here is similar to Sassano et al. (2021) with the main differences being that we divided the volume of our simulation in cells allowing a more precise computation of the metallicity of the enriched regions.

Fig. 2 shows the bubble size distribution function (r_{bubble} in ckpc) at redshift 20, 15, 10, and 5. From this plot, we see the bubble growth

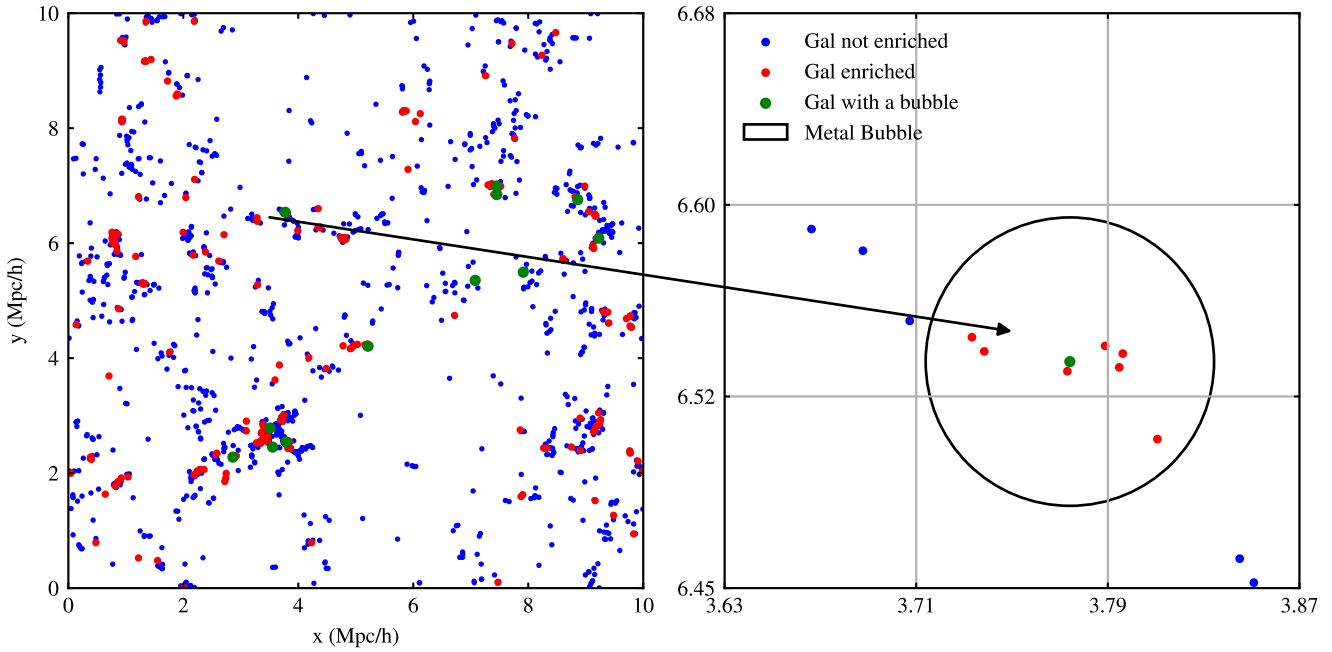


Figure 1. *left:* 2D slice of the L10 box at $z = 10$ with the position of all the galaxies with $M_{\text{vir}} \geq 10^6 M_{\odot}$ (blue dots) highlighting the ones that are externally metal enriched (red dots). The green dots are galaxies with an associated metal bubble larger than $0.05 h^{-1} \text{ cMpc}$. The slice is $10 h^{-1} \text{ Mpc}$ on a side and $\sim 0.078 h^{-1} \text{ Mpc}$ thick. *right:* zoom-in of a single pixel ($0.24 h^{-1} \text{ Mpc}$ on a side). The circle represents the actual size of the bubble around the green dot.

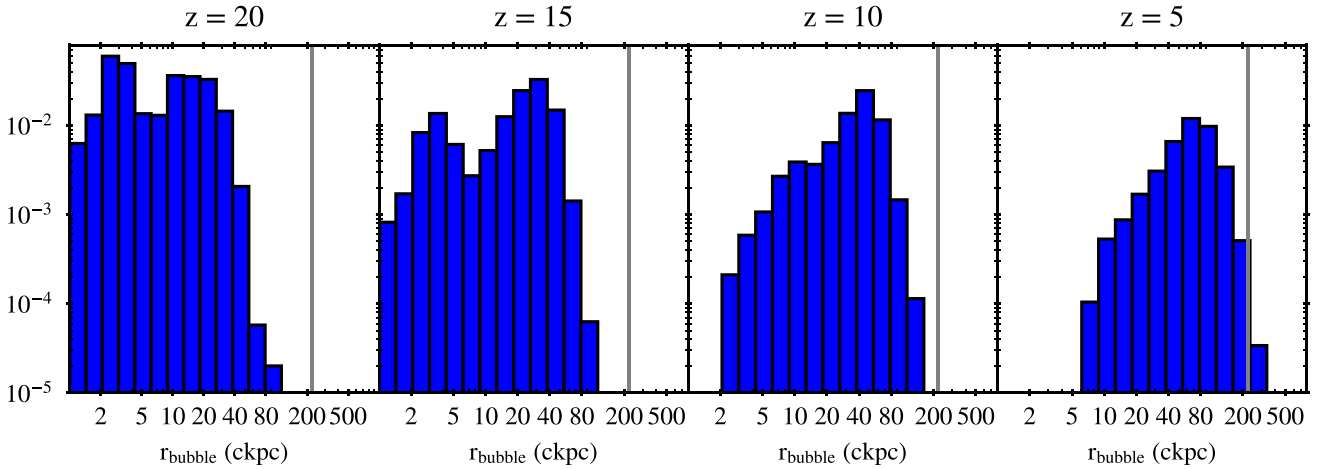


Figure 2. Distribution function of the metal bubble size computed according to equation (8) at four different redshifts. The grey column indicates the predicted value for the maximum bubble size at $z = 6$ from Trenti et al. (2009).

over time from a typical radius of $\sim 30 \text{ ckpc}$ at $z = 20$ to $\sim 150 \text{ ckpc}$ at $z = 5$. These values are consistent with the results shown in Trenti et al. (2009) ($r_{\text{bubble}} \leq 150 h^{-1} \text{ ckpc}$ at $z = 6$) with only a few bubbles at $z = 5$ larger than this value.

Fig. 3 shows the IGM metallicity (top row), metal filling factor (middle row), and density (bottom row) maps at four different snapshots. The red (blue) cells in the top row have $Z_{\text{IGM}} \geq (<) Z_{\text{crit}}$ indicating that galaxies that will be externally polluted in those cells will accrete enriched (pristine) gas and will form Pop. II (III) stars. Comparing the maps at the same snapshot, we see that the more overdense regions have a larger filling factor and a higher metallicity as these hosts more galaxies, hence more metal bubbles. Fig. 3 also shows the progressive enrichment of the IGM over the cosmic history since, as we move to lower redshift (from left to right-hand panels), we have more enriched cells and with larger filling factors.

2.6 Pop. III star formation

In this work, we modify Pop. II description in M16 to allow star formation in Pop. III galaxies (see Section 2.4 in M16). In particular, once a galaxy reaches a mass of cold gas larger than a critical value m_{crit} , this galaxy will convert the cold gas into stars according to the star formation efficiency α_{SF} . The value of m_{crit} is computed as in M16 and is determined by a critical surface density Σ_{norm} of the gas in the cold disc. Since we are now considering two different stellar populations, we adopted two different free parameters, both for the star formation efficiency $\alpha_{\text{SF, III}}$ and for the critical surface density $\Sigma_{\text{crit, III}}$. Recent full hydrodynamical simulations that follow the collapse of a pristine gas cloud until a Pop. III star is formed (e.g. Hirano et al. 2014; Stacy et al. 2016; Chon et al. 2021), suggest that the Pop. III IMF is shifted to larger masses as a result

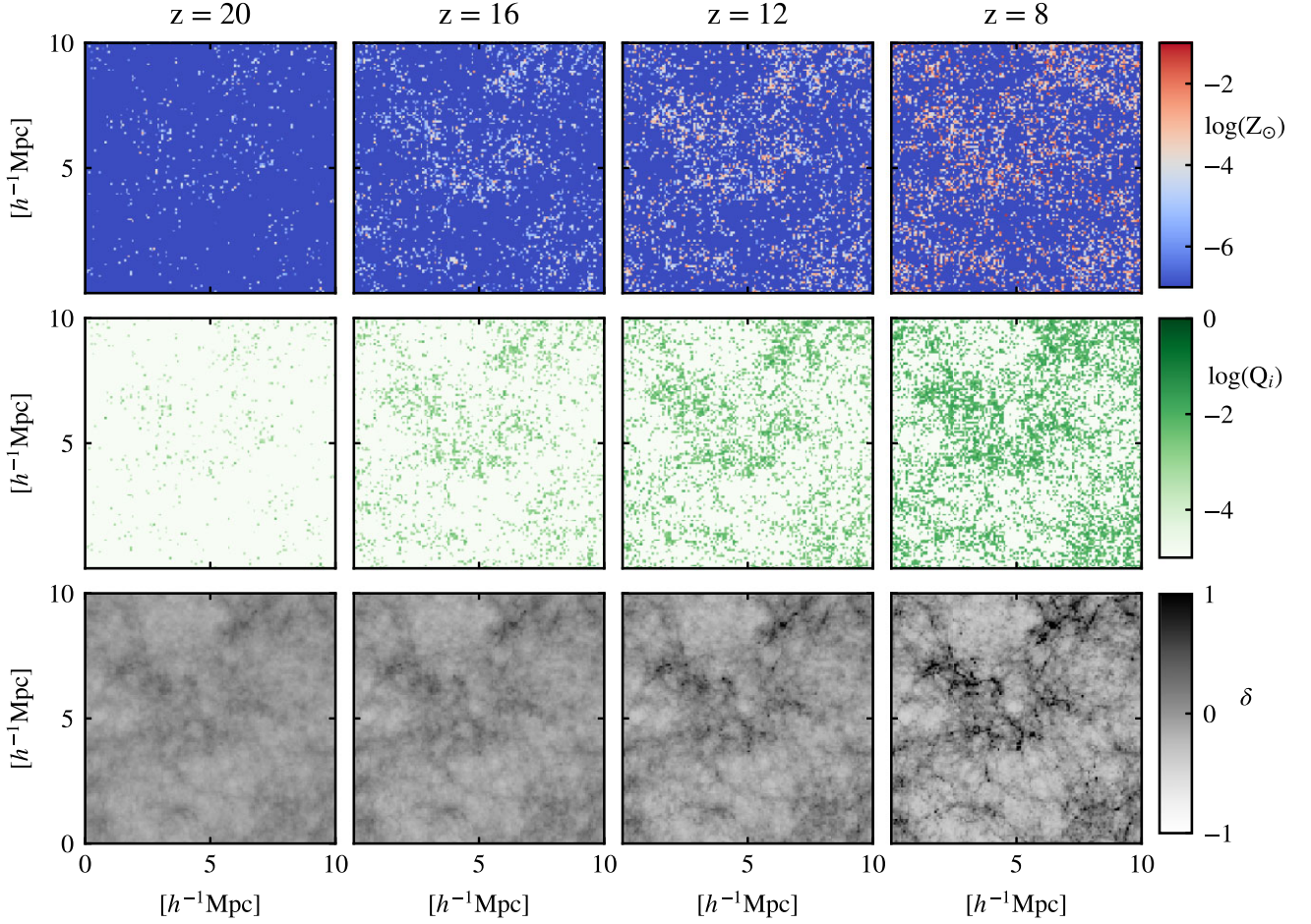


Figure 3. 2D projections of the IGM metallicity $\log(Z_{\text{IGM}})$ in solar units (top row), the metal filling factor $\log(Q)$ (middle row), and the overdensity δ (bottom row). From left to right, the columns correspond to the same redshift: $z = 20, 16, 12, 8$. Each slice is $10 h^{-1} \text{ Mpc}$ on a side and considers the average contribution over the entire thickness of the box. In the top row, red (blue) represents enriched (pristine) pixels: $Z_{\text{IGM}} \geq (<) Z_{\text{crit}}$. Green pixels have a larger filling factor Q , indicating a larger probability of a galaxy accreting enriched gas. Dark cells in the bottom row have larger mean overdensity δ .

of less fragmentation due to inefficient cooling. Within this work, we adopted the IMFs from Raiter, Schaerer & Fosbury (2010) (see Table 2), while for Pop. II stars, we assumed a Kroupa (2001) IMF. For the fiducial model, we chose a Salpeter IMF with a mass between 1 and $500 M_{\odot}$. The choice of the IMF is crucial as it determines many properties of the stellar population, including what fraction of stars will explode as supernovae and, hence, the amount of energy and metals injected into the IGM. In this work, we explore the impact of the four free parameters discussed above (see also Table 1) since these have the strongest impact on the Pop. III star formation history. MERAXES includes more free parameters describing the energy coupling efficiency of the supernova explosion (see M16 and Qiu et al. 2019) that will not be explored in this work (we will take the same fiducial values as for Pop. II). Since the focus of this work is on the first galaxies formed during the Cosmic Dawn, we do not explore parameters describing the UV ionizing and X-ray radiation (e.g. escape fraction), and we will take the same fiducial values as in the previous works (see Balu et al. 2023). Those will be discussed in a future work focused on the EoR using a larger box.

The fate of a zero-metallicity star is quite uncertain due to the many poorly constrained physical mechanisms. Here, we adopt a simplified picture of the final fate of a Pop. III star depends only on its initial mass (Heger & Woosley 2002). For masses below $8 M_{\odot}$, there will be no SN event. If $M_{\star} \in [8, 40] M_{\odot}$, it will explode as a core-collapse

SN (CCSN) leaving a remnant; if $M_{\star} \in [140, 260] M_{\odot}$, there will be a pair-instability SN (PISN) leaving no remnant; and if $M_{\star} \in [40, 140] M_{\odot}$ or $M_{\star} > 260 M_{\odot}$, stars collapse directly into a black hole (BH) with negligible feedback. Given the different endings of a Pop. III star life, the choice of the IMF is crucial to compute the timing of delayed supernova feedback. While we use the technique of Qiu et al. (2019) for Pop. II stars with precomputed tables assuming a Kroupa IMF (Kroupa 2001), for Pop. III supernova feedback we estimated the amount of SN energy and metal yields with an analytic calculation as in M16. The total energy provided by Pop. III supernovae explosions at the snapshot j is:

$$\begin{aligned} \Delta E_{\text{total,III},j} &= \sum_{i=j-17}^{i=j} (\Delta E_{\text{CCSN,III},j} + \Delta E_{\text{PISN,III},j}) \\ &= \epsilon_{\text{energy}} \left(\sum_{i=j-17}^{i=j} (\Delta m_{\star,\text{III}}^i \eta_{\text{III,CCSN},j}^i E_{\text{CC}}) \right. \\ &\quad \left. + \Delta m_{\star,\text{III}}^j \eta_{\text{III,PISN}} E_{\text{PISN}} \right), \end{aligned} \quad (10)$$

where Δm_{\star}^i is the new stellar mass formed at an earlier snapshot i , ϵ_{energy} is the energy coupling efficiency (Qiu et al. 2019), $E_{\text{CC}} = 10^{51} \text{ erg}$, and $E_{\text{PISN}} = 10^{53} \text{ erg}$ are the typical energy for a core collapse and a pair-instability supernova respectively and

Table 1. Free parameters of Pop. III star formation.

Parameter	Description	Fiducial value (Pop II)
α_{SF}	Star formation efficiency	0.008 (0.08)
Z_{crit}	Critical metallicity for Pop III star formation	$10^{-4} Z_{\odot}$
Σ_{norm}	Critical surface density of cold gas for Pop III star formation	$0.37 (0.37) M_{\odot} \text{ pc}^{-2}$
IMF type*	Shape of the Initial Mass Function	Sal (Kroupa)

Note. *see Table 2.

$$\eta_{\text{III,CCSN},j}^i = \int_{m_{\text{min},j}^i}^{m_{\text{max},j}^i} \phi(M) dM \quad (11)$$

$$\eta_{\text{III,PISN}} = \int_{140 M_{\odot}}^{260 M_{\odot}} \phi(M) dM \quad (12)$$

are, respectively, the fraction of stars formed during snapshot i that go core collapse and pair-instability supernova in snapshot j . These are computed by integrating the chosen IMF over the correct mass limits. Assuming that all-star formation occurred in the middle of the snapshot, $m_{\text{min},j}^i$ and $m_{\text{max},j}^i$ for CCSN are computed from the lifetimes for Pop. III stars using Schaerer (2002) assuming no mass loss and zero metallicity. We highlight that a zero metallicity star with $M \in [140, 260]$ has a lifetime smaller than the time separation between two consecutive snapshots in MERAXES; hence, it will explode as a PISN in the same snapshot in which it forms. For this reason, in equation (12), the mass limit for η_{PISN} is the entire mass range of the PISN, and when computing the total energy from PISN injected at snapshot j in equation (10), we consider only the stars that are formed at snapshot j . For CCSN, instead, we keep track of the star formation history over the last 17 snapshots, which correspond to $\gtrsim 40$ Myr, after which all stars with $M \geq 8 M_{\odot}$ will already have exploded. To compute the amount of gas that is reheated and ejected from the halo, we adopted the same prescription as Qiu et al. (2019).

We also update the amount of ejected gas and metals from Pop. III stars. These are taken from Heger & Woosley (2010) assuming non-mixing (no rotation) and a supernova explosion of 1.2×10^{51} erg. As in M16, when a star goes core-collapse supernova at snapshot j , it will release an amount $\Delta m_{\text{CCSN},z,j}$ of metals and $\Delta m_{\text{CCSN},x,j}$ of gas into the interstellar medium:

$$\Delta m_{\text{CCSN},z,j} = \sum_{i=j-17}^{i=j} \frac{\Delta m_{\text{CCSN},z,j}^i}{m_{\text{CCSN}}} \Delta m_{\star}, \quad (13)$$

where m_{CCSN} is the total fraction of stars that ends as a CCSN:

$$m_{\text{CCSN}} = \int_{8 M_{\odot}}^{40 M_{\odot}} M \phi(M) dM \quad (14)$$

and $\Delta m_{\text{CCSN},z,i,j}$ is the amount of metals released by a star formed at snapshot i and going supernova at snapshot j :

$$\Delta m_{\text{CCSN},z,j}^i = \int_{m_{\text{min},j}^i}^{m_{\text{max},j}^i} M \phi(M) Z dM. \quad (15)$$

In the above equation, Z is the metal mass fraction released into the ISM from supernovae, and it is incorporated inside the integral because it is not fixed over the mass range (i.e. in stars with $M_{\star} \geq 25 M_{\odot}$ most of the metals will fall onto the remnant due to the massive fallback). With an entirely analogous calculation, it is possible to find $\Delta m_{\text{CCSN},x,j}$ (we just need to replace Z with the gas mass fraction X). Once again, we are doing delayed SN recycling only for CCSN because, in the case of pair instability, all the feedback is contemporaneous. For PISN, we considered the gas and metal yields from Heger & Woosley (2002).

Table 2. IMF model parameters.

Label	Type	M_{low}	M_{up}	α	M_c	σ
Sal	Salpeter	1	500	-2.35	-	-
log A	log-Normal	1	500	-	10	1.0
log E	log-Normal	1	500	-	60	1.0

In all the previous MERAXES works, all the stellar mass locked up in remnants (neutron stars and BHs) was neglected as it was recycled into the gas mass budget of the galaxy. We decided to drop this approximation for Pop III stars as they are likely to leave more massive remnants (some might be massive enough to be the first ‘light’ seeds of supermassive BHs). First, we need to consider the BHs that formed after a ‘failed SN scenario’ typical of a star with an initial mass $M_{\star} \in [40, 140] M_{\odot}$ and $M_{\star} > 260 M_{\odot}$. The BH mass arising from this scenario will be:

$$m_{\text{BH}} = \Delta m_{\star} \left(\int_{40 M_{\odot}}^{140 M_{\odot}} M \phi(M) dM + \int_{260 M_{\odot}}^{M_{\text{max}}} M \phi(M) dM \right). \quad (16)$$

Finally, we need to account for the BH remnants that are left after a CCSN. In this case, we use equations (13) and (15) substituting the metal mass fraction with the BH mass fraction $B = (1 - X - Z)$ (since all the remaining material that has not been ejected is locked onto the stellar remnant). MERAXES does not evolve the remnants (via accretion), as the main focus of this work is Pop. III stars. However, the impact of the first accreting BHs on the formation of the supermassive black holes and radiative backgrounds might be important even at high-redshift (Ventura et al. 2023).

2.7 Pop. III luminosity

In order to investigate the observability of the first Pop. III galaxies, we implement spectral energy distributions (SED) for Pop. III stars. We use SEDs from Raiter et al. (2010) that have been computed for the IMFs listed in Table 2 assuming that star formation occurs in an instantaneous burst (see *instantaneous burst* in Raiter et al. 2010). These SEDs also include the nebular continuum emission and the UV ionizing properties. We used the latter to compute the number of UV ionizing photons per baryon n_b^{γ} for each IMF provided. To compute the luminosity of galaxies at a specific wavelength λ , we used the model introduced by Qiu et al. (2019) (see also Mutch et al. 2024), and we extended it to Pop. III galaxies. Having the Pop. III SEDs, we can compute the luminosity of a Pop. III galaxy at time t as:

$$L_{\lambda}(t) = \int_0^t \psi(t - \tau) S_{\lambda}(\tau) T_{\lambda}(\tau) d\tau. \quad (17)$$

Here, τ is the stellar age, $\psi(t - \tau)$ the stellar mass formed at $t - \tau$ with age between τ and $\tau + d\tau$, $S_{\lambda}(\tau)$ is the luminosity of a stellar population per unit mass, and $T_{\lambda}(\tau)$ is the transmission function of the interstellar medium. For the latter term, we refer the reader to

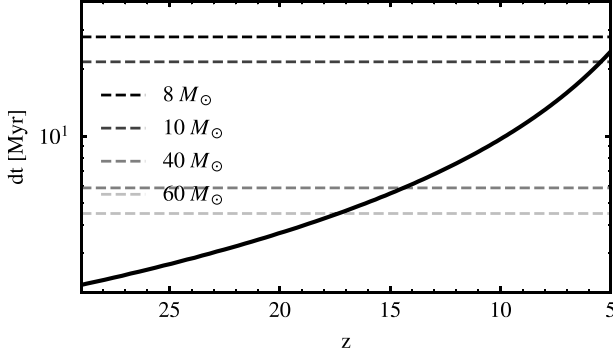


Figure 4. Duration of the snapshot dt in Myr as a function of redshift. Dashed lines correspond to the lifetime of a zero metallicity star of 8, 10, 40, and $60 M_{\odot}$.

Qiu et al. (2019) while S_{λ} for each Pop. III IMF has been taken from Raiter et al. (2010) as discussed above. This calculation is nearly identical to Qiu et al. (2019), with the difference being that we do not have the metallicity dependence because Pop. III stars SEDs are defined with a zero metallicity. In this framework, we assume that the star formation occurs continuously throughout the snapshot. To compute $\psi(t - \tau)$, we take the stellar mass formed in that snapshot and average it over the entire duration of the snapshot. While this is a good approximation for Pop. II stars, Pop. III star formation is expected to occur in a single burst because of the feedback from Pop. III stars is likely to prevent continuous star formation. For this reason, we expanded the calculation of the luminosity of Pop. III galaxies assuming that new stars Δm_{\star} form instantaneously at the time $t - \tau = t_0$. Hence, we can write $\psi(t - \tau) = \Delta m_{\star} \delta(t_0)$ and equation (17) simplifies to:

$$\begin{aligned} L_{\lambda}(t) &= \Delta m_{\star} \int_0^t d\tau \delta(t - t_0) S_{\lambda}(\tau) T_{\lambda}(\tau) \\ &= \Delta m_{\star} S_{\lambda}(t - t_0) T_{\lambda}(t - t_0). \end{aligned} \quad (18)$$

As we will discuss in Section 4, instantaneous (instead of continuous) Pop. III star formation has an impact on the estimated luminosity function of galaxies hosting Pop. III stars. This is because Pop. III stars have lifetimes that can be shorter than the duration of the snapshot (at $z = 10$ the snapshot will last 10 Myr, see Fig. 4). Hence, when we consider continuous star formation, we average the star formation over the entire snapshot, leading to lower luminosity with a higher duty cycle.

In order to account for instantaneous star formation, we assumed that a Pop. III star formation episode in a galaxy can occur at random $\Delta t \in [0, t_{\text{snap}}]$ prior to the end of the snapshot. For the detailed evaluation of the UV luminosity function accounting for the stochasticity in the time at which the burst of star formation occurs in different galaxies, we refer the reader to Appendix B.

3 GLOBAL EVOLUTION OF POP. III STARS

To explore the Pop. III contributions to the cosmic star formation history, we ran two simulations on the L10 box, one with all the updates described in Section 2 adopting the fiducial parameters (see Table 1 and one without the new physics that we labelled as ‘NoMini’). Given that there are no observational constraints on Pop. III, the choice of a fiducial model is arbitrary. The one adopted in this work has both a low star formation efficiency and a Salpeter-like IMF, which will result in a relatively small global impact of Pop. III star formation compared to Pop. II.

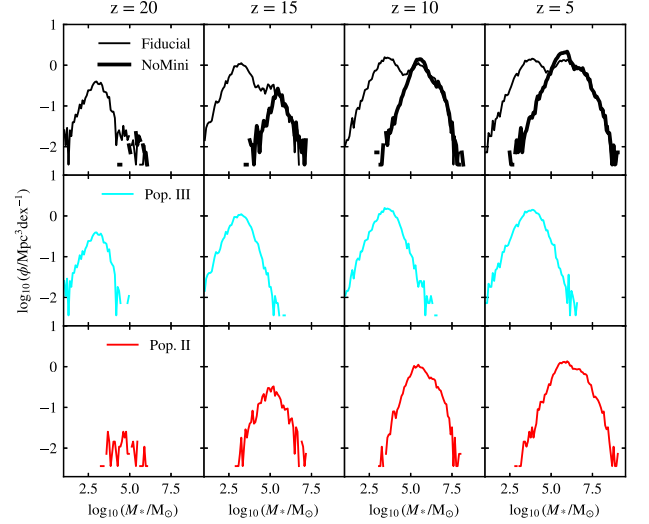


Figure 5. SMF at $z = 20, 15, 10,$ and 5 for all stars (upper row), Pop. III stars (middle row), and Pop. II (lower row) using the fiducial model (Table 1) and the NoMini model (thick line).

In Fig. 5, we show the stellar mass function (SMF) at different redshifts, accounting for all (black), only Pop. III dominated (cyan), and only Pop. II dominated (red) galaxies. We classified a galaxy as Pop. III or Pop. II dominated based on which population is brighter in the UV band. Thin (thick) lines are computed from the fiducial (NoMini) model. The total SMF has two components, separated by their stellar types. In this fiducial model, as Pop. III SFE is 10 times lower than Pop. II, we see a resulting bimodality (which we will further expand discussion in Section 3.2.1). As shown in the upper panels, the new updates on MERAXES mostly affect the lower end of the SMF, with a larger impact at high- z . This reflects the star formation in mini-haloes (we are now considering molecular cooling), which is dominant at $z \geq 15$ before the LW background becomes strong enough to photodissociate all the molecular hydrogen.

The low mass of Pop. III systems is mainly a consequence of both the shorter lifetimes of Pop. III stars (given their larger mass) and the lower SF efficiency, but it also suggests that most of the Pop. III star formation must occur in mini-haloes. In order to investigate this, we checked which haloes form Pop. III and Pop. II stars. In Fig. 6, we show the halo mass function for Pop. III (cyan line) and Pop. II (red line) star-forming haloes at $z = 20, 15, 10,$ and 5 . The dashed line corresponds to the limit of atomic cooling ($T_{\text{vir}} = 10^4$ K). Given the small size of the box, we have only a few atomic cooling haloes at $z \sim 20$, so all star-forming systems are mini-haloes (and are mostly Pop. III). At lower redshift, the peak of the distribution shifts to higher masses (by $z = 10$ most of the stars form in atomic cooling haloes except for some low-mass haloes that are undergoing a merger event), and the impact of Pop. II increases. Finally, Fig. 6 shows that Pop. III stars mostly form in mini-haloes (except at $z = 5$ when the radiative feedback has suppressed both the gas infall and cooling in mini-haloes). This is because the more massive haloes are more likely to have already experienced star formation and so will be internally chemically enriched.

In Fig. 7, we show the total star formation rate density (SFRD) as a function of redshift for both the fiducial and the NoMini model. In the case of the fiducial model, we also show the Pop. III (Pop. II) contribution in the upper (lower) panel. Mini-haloes have an

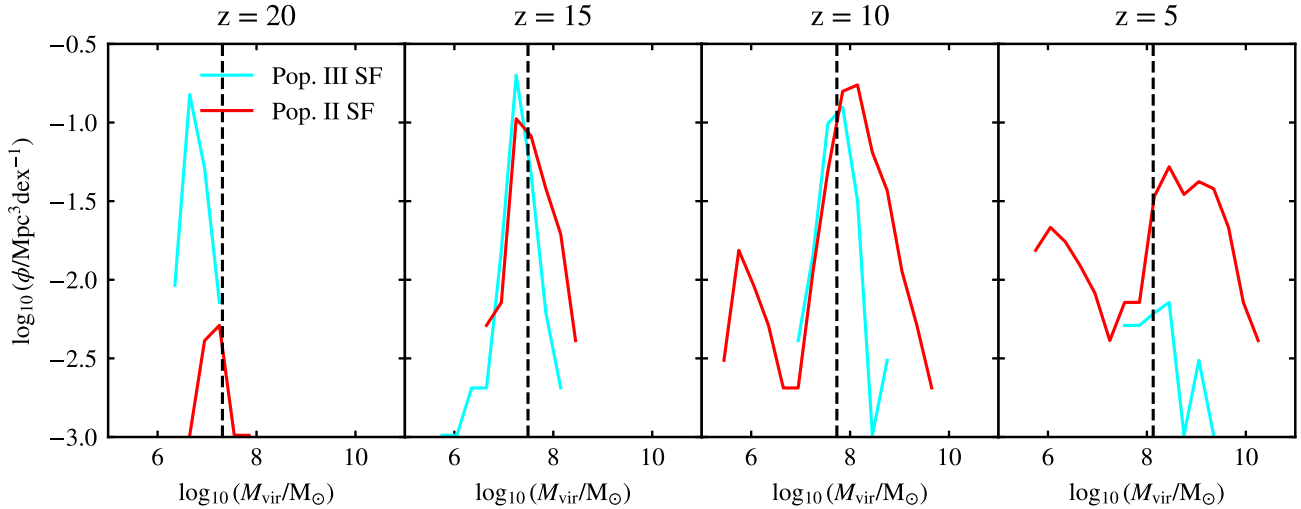


Figure 6. Halo mass function at $z = 20, 15, 10,$ and 5 of Pop. III and Pop. II hosting systems. The dashed line corresponds to the $T_{\text{vir}} = 10^4$ K that defines the atomic cooling limit.

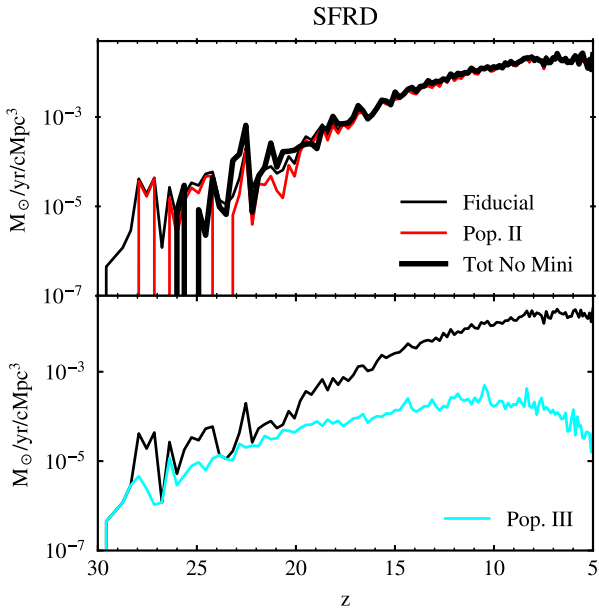


Figure 7. SFRD versus redshift for all stars (black line), Pop. III (cyan) and Pop. II (red) using the fiducial model (thin line) and the NoMini model (thick line).

appreciable impact on the SFRD only up to $z \geq 20$, while at lower redshift, most star formation occurs in atomic cooling haloes (at $z < 15$, the total SFRD in the fiducial and NoMini model are superimposed). We see that accounting for Pop. III star formation in mini-haloes is crucial during the Cosmic Dawn because Pop. III stars dominate the global star formation history at $z \geq 20$ and are still relevant up to $z = 18$. As we can see in the lower panel, the Pop. III SFRD flattens at $z \sim 18$ and starts to decrease at $z \sim 10$. The early flattening occurs due to the build-up of the LW background that affects Pop. III star formation in minihaloes. The sharp drop at $z \leq 10$ is mostly caused by the photoionizing feedback from reionization that also affects the atomic cooling haloes. The feedback from reionization also mildly affects Pop. II as can be

seen from the flattening of the red line at $z \sim 8$ in the upper panel.⁵

3.1 Chemical enrichment of the IGM

Compared to reionization, the chemical enrichment of the IGM is a much slower process due to the lower velocity of the expansion of the metal bubbles. As already found in previous works (e.g. Visbal et al. 2020; Yamaguchi et al. 2023), the impact of external metal enrichment is subdominant compared to internal metal enrichment. However, external enrichment might still be important for low-mass haloes that do not form stars until $z \sim 10$.

The top left-hand panel of Fig. 8 shows the redshift evolution of the average metallicity of the box (in solar units) computed using equation (9) and averaging through all 128^3 pixels. As expected, the average metallicity increases monotonically. It crosses the critical value at $z \sim 11$ and at the end of the simulation is $\sim 5 \times 10^{-3} Z_{\odot}$. The redshift evolution of Z_{IGM} is in very good agreement with Yamaguchi et al. (2023), especially for their ‘bursty’ models, which is the one that most closely resembles the star formation in MERAXES. However, the average metallicity of the IGM does not completely inform us of the average metallicity of the galaxies since, when averaging through the entire box, we are considering voids that have no galaxies and hence zero IGM metallicity. For this reason, in the top right-hand panel, we computed the black solid line, averaging only through cells that have at least one metal bubble (meaning that there must be at least one galaxy that formed stars). The shaded region shows the scatter in the metallicity of these cells from the highest to the lowest metallicity. The average metallicity, in this case, is much higher, and it is always above the critical value. This suggests that once the first galaxies form, the ejection of metals from Pop. III is quite effective in the nearby regions, allowing a fast Pop. III/II transition in those cells where star formation has already occurred (and the galaxies

⁵Given the small size of the box, the feedback from reionization is slightly overestimated, as we (i) are missing the most massive systems that would not be affected by the photo-ionizing feedback, and (ii) the box gets completely ionized at $z \sim 6.9$, which is much earlier than what is suggested by the latest Lyman- α forest measurements (e.g. Qin et al. 2021; Bosman et al. 2022).

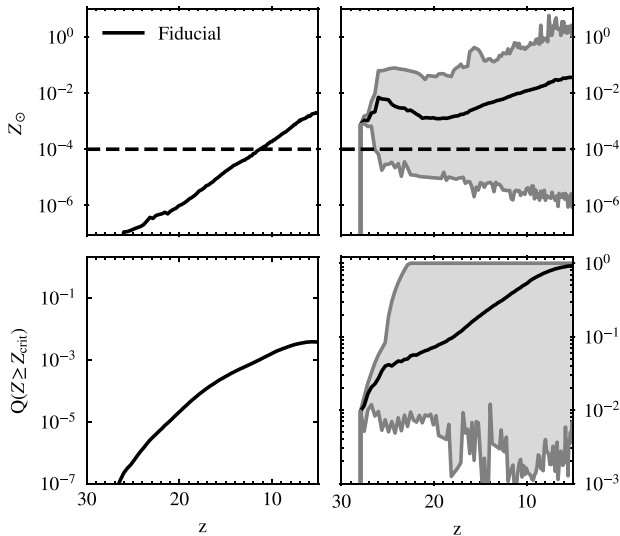


Figure 8. *Top:* Average metallicity of the IGM (in solar units) versus redshift highlighting Z_{crit} for the Pop. III/II transition. *Bottom:* fraction of the volume with a metallicity $Z \geq Z_{\text{crit}}$ versus redshift. The left-hand panels show these quantities averaged through the entire box, while the right-hand panels consider only those cells with at least one metal bubble in them. Shaded regions in the right-hand panels highlight the minimum and the maximum value (see text).

are internally enriched). The lower panels instead show the fraction of the IGM that reached the critical metallicity (or equivalently the metal filling factor $Q(Z \geq Z_{\text{crit}})$). Considering the entire box (left-hand panel), less than 1 per cent of the volume gets enriched above Z_{crit} by $z \sim 5$. This result is fairly consistent with Visbal et al. (2020) and Yamaguchi et al. (2023) (~ 1 per cent by $z = 6$). These small differences are likely due to differences in the star formation models and in the choice of parameters, such as the star formation efficiency. If we focus only on the regions with at least one galaxy that formed stars, we find larger filling factors, and by the end of the simulation, those pixels are all completely enriched. This final result reflects our choice of pixel size that is designed to be similar to the average volume of the metal bubble at $z \sim 5$.

Finally, in Fig. 9, we show the halo mass function for the externally (black line) and internally (grey line) metal enriched haloes at $z = 20, 15, 10$, and 5 .⁶ While most haloes get internally enriched by their own star formation, at $z = 5$ haloes with virial masses $M_{\text{vir}} \leq 10^{7.5} M_{\odot}$ get their metals mostly from a nearby supernova bubble. This picture reflects the fact that low-mass haloes during reionization are not able to form stars because of the LW and photo-ionizing feedback. Hence, those objects can be chemically enriched only from an external source.

In conclusion, when looking at the global evolution of star formation, the effect of the external metal enrichment is quite negligible, as it is important only for low-mass haloes at low redshift that will hardly form stars due to the radiative feedback effects. We verified this by running a simulation without external metal enrichment (a halo can only get enriched by its own star formation). We plot in Fig. 10 the total, Pop. III and Pop. II SFRD (dashed lines) compared to the fiducial model (solid lines). There are no appreciable differences

⁶While physically a halo could be both internally and externally enriched, here we are simplifying assuming that a halo is either internally or externally enriched.

between the two models except at $z \leq 8$ when the dashed line is slightly larger (about 0.1 dex difference).

3.2 Pop. III star formation parameters

The results in previous sections were obtained adopting quite conservative assumptions for Pop. III stars given the very low SF efficiency and the Salpeter-like IMF (although with $M_{\text{min}} = 1 M_{\odot}$). In the following sections, we explore the four main free parameters that regulate Pop. III star formation in MERAXES listed in Table 1: the Pop. III star formation efficient $\alpha_{\text{SF, III}}$, the critical metallicity for Pop. III/II transition Z_{crit} , the critical surface density of cold gas for Pop. III star formation to occur $\Sigma_{\text{norm, III}}$ and the IMF.

3.2.1 Pop. III SF efficiency

The star formation efficiency determines the conversion of the cold gas into stars and is the free parameter with the largest impact on the Pop. III global SFRD and SMF. This parameter is largely unconstrained, with some simulations supporting very low values (10^{-4} – 10^{-3} Skinner & Wise 2020) and others suggesting higher values (Fukushima et al. 2020). We ran two simulations keeping all the Pop. III free parameters unchanged except for $\alpha_{\text{SF, III}}$, which we boosted by one order of magnitude (to the same value we use for Pop. II $\alpha_{\text{SF}} = 0.08$) and to a very high value ($\alpha_{\text{SF}} = 0.5$).

As shown in Fig. 11, Pop. III galaxies become more massive as α_{SF} increases, erasing the ‘double peak’ feature in the total SMF. For the model with $\alpha_{\text{SF, III}} = \alpha_{\text{SF, II}}$, the peak of the Pop. III SMF is still shifted to the left by half dex compared to the Pop. II. This is because, despite having the same star formation efficiency, Pop. III galaxies mostly form in mini-haloes. For $\alpha_{\text{SF, III}} = 0.5$, the peak of the Pop. III and Pop. II SMF is at the same mass value (10^5 – $10^6 M_{\odot}$ at $z \sim 15$ – 5) with the only difference being the larger variance for Pop. II galaxies. Increasing the Pop. III SF efficiency does not affect the Pop. II SMF (except for small variations at $z = 5$) meaning that the mechanical feedback does not change significantly.

The star formation efficiency also regulates the Pop. III/II transition as it directly correlates with the SFRD. Looking at the SFRD in the three different models (Fig. 12), we see that for $\alpha_{\text{SF, III}} = 0.5$, the SFRD is dominated by Pop. III up to $z \sim 15$ compared to the fiducial model, where Pop. II SF becomes larger than Pop. III at $z > 20$. The Pop. II SFRD does not significantly change between the three models, and so the change in the Pop. III SFRD also affects the total SFRD (the dashed line is almost one order of magnitude higher than the solid one). All the models converge at $z \sim 13$ when even with the highest $\alpha_{\text{SF, III}}$, the total SFRD is entirely dominated by the Pop. II contributions.

3.2.2 Critical metallicity

The critical metallicity defines the metallicity at which there is a change in the IMF (metal-free gas clouds have inefficient cooling that leads to less fragmentation and higher masses Chiaki & Yoshida 2022). There is currently no consensus on the value of Z_{crit} , with two competing models that assume the fragmentation driven by either the carbon and oxygen line (e.g. Chon et al. 2021) or the dust cooling (e.g. Schneider et al. 2012; Chiaki & Yoshida 2022). The first class of models determine a $Z_{\text{crit}} \sim 10^{-2}$ – $10^{-3} Z_{\odot}$, while the seconds give a lower value ($\sim 10^{-6} Z_{\odot}$). Some studies also argue that the value of Z_{crit} evolves with redshift due to the effect of the CMB (Chon et al. 2022). Following simulations in the literature (Schneider et al. 2006;

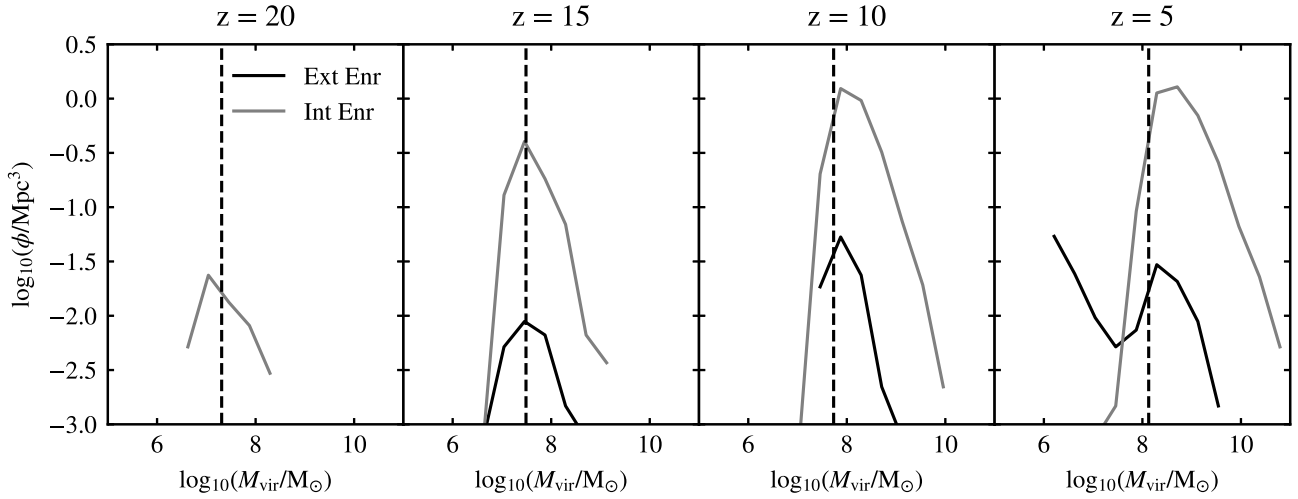


Figure 9. Halo mass function at $z = 20, 15, 10,$ and 5 of Pop external (black) and internal (grey) metal enriched haloes. The dashed line corresponds to the $T_{\text{vir}} = 10^4$ K that defines the atomic cooling limit.

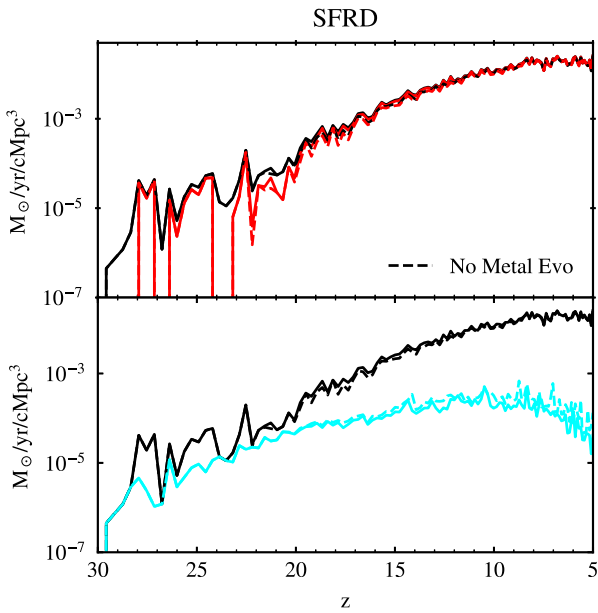


Figure 10. As Fig. 7 for the fiducial model (solid lines) and turning off the external metal enrichment (dashed lines).

Visbal et al. 2020), in this work we adopted an intermediate value $Z_{\text{crit}} = 10^{-4} Z_{\odot}$ as the fiducial value, hereafter we will also show results for the two extreme values of 10^{-2} and $10^{-6} Z_{\odot}$.

The SMF between the fiducial model and $Z_{\text{crit}} = 10^{-6} Z_{\odot}$ does not change. This is because, as we saw in the top right-hand panel of Fig. 8, in the overdense regions where there is star formation, the metallicity becomes larger than $10^{-4} Z_{\odot}$ very quickly so that changing Z_{crit} to $10^{-6} Z_{\odot}$ does not further accelerate the Pop. III/II transition. However, considering a higher value changes the total SMF, as we end up with many more Pop. III stars. As shown in Fig. 13, in the Pop. III SMF in this case, many of the previously identified as Pop. II galaxies are now Pop. III galaxies across the entire mass range. The high-mass tail of Pop. III SMF extends up to $10^{7.5} M_{\odot}$ at $z = 5$ when $Z_{\text{crit}} = 10^{-2} Z_{\odot}$, while the Pop. II systems are less massive as they start to form later and so have less time to build up their mass. The combined effect of Pop. III and Pop. II makes the

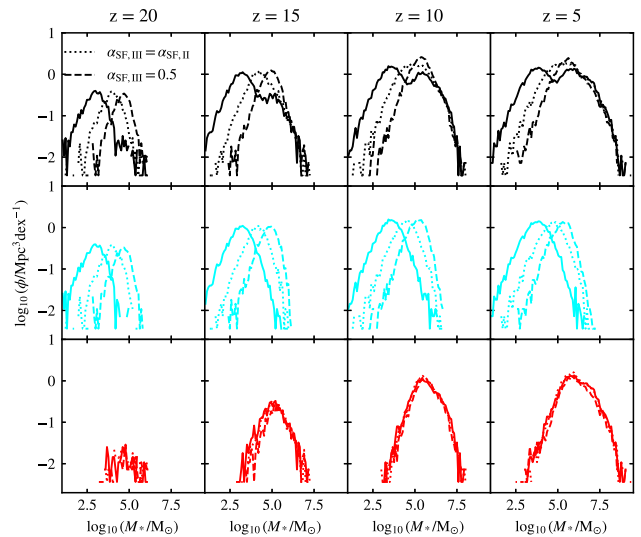


Figure 11. As Fig. 5 using the fiducial model (solid), $\alpha_{\text{SF, III}} = \alpha_{\text{SF, II}}$ (dotted) and $\alpha_{\text{SF, III}} = 0.5$ (dashed).

total SMF computed from the simulation with $Z_{\text{crit}} = 10^{-2} Z_{\odot}$ single peaked as the high-mass peak coming from Pop. II stars are washed out even at $z = 5$ so that the total SMF peaks at $M_{*} \sim 10^4 M_{\odot}$ at $z = 10-5$ with a high-mass tail that extends up to $10^9 M_{\odot}$.

The critical metallicity also has a strong impact on the evolution of the SFRD (see Fig. 14), as it affects both the internal and external enrichment. While decreasing the value of Z_{crit} from the fiducial value only mildly decreases the Pop. III SFRD without altering the total result, choosing $Z_{\text{crit}} = 10^{-2} Z_{\odot}$ strongly changes the SFRD history at $z \leq 18$. The Pop. III SFRD increases by 1–2 orders of magnitude while the Pop. II decreases by the same amount. It also starts to increase steadily only from $z \sim 18$. Increasing the Pop. III star formation and simultaneously decreasing the Pop. II impacts on the total SFRD. Since Pop. III stars form less efficiently ($\alpha_{\text{SF, III}} = 0.1 \times \alpha_{\text{SF, II}}$), we predict a lower total SFRD compared to the fiducial model (and in this case, the two models do not converge until the very end of the simulation). Overall the critical metallicity heavily impacts both the SFRD and SMF during the Cosmic Dawn and the Epoch of

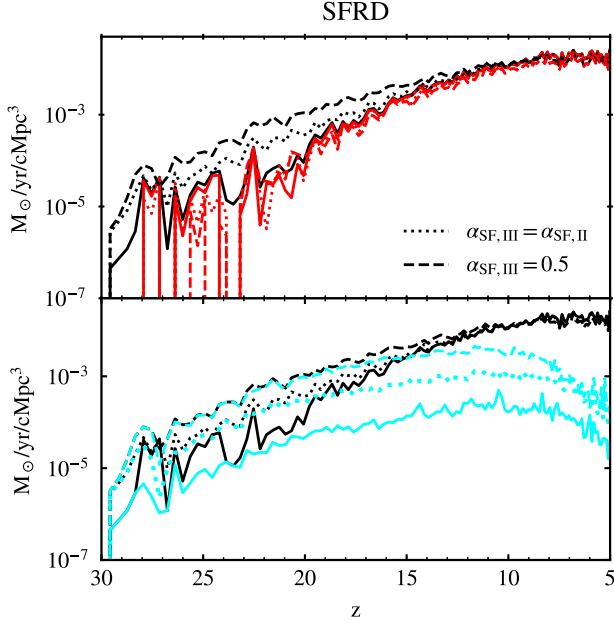


Figure 12. As Fig. 7 using the fiducial model (solid), $\alpha_{\text{SF, III}} = \alpha_{\text{SF, II}}$ (dotted) and $\alpha_{\text{SF, III}} = 0.5$ (dashed).

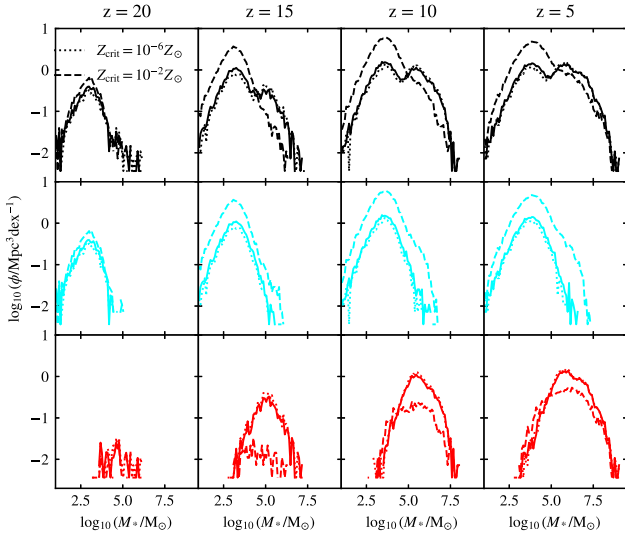


Figure 13. As Fig. 5 using the fiducial model (solid), $Z_{\text{crit}} = 10^{-6}$ (dotted) and $10^{-2} Z_{\odot}$ (dashed).

Reionization and affects when the Universe transitions from being Pop. III dominated Pop. II.

3.2.3 Critical surface density

In order to trigger the star formation in a galaxy, our model requires the gas density in the disc to be above a certain threshold. This result has been obtained in the observational results of Kennicutt (1998); Kennicutt & De Los Reyes (2021) and theoretically motivated by Kauffmann (1996); however, the value of this parameter is highly uncertain, especially at high- z , as it depends on the structure of the disc (e.g. thickness, turbulence etc.). We decided to duplicate this free parameter so that we have one for Pop. III and one for Pop. II. While keeping the Pop. II parameter fixed, we explore the extreme

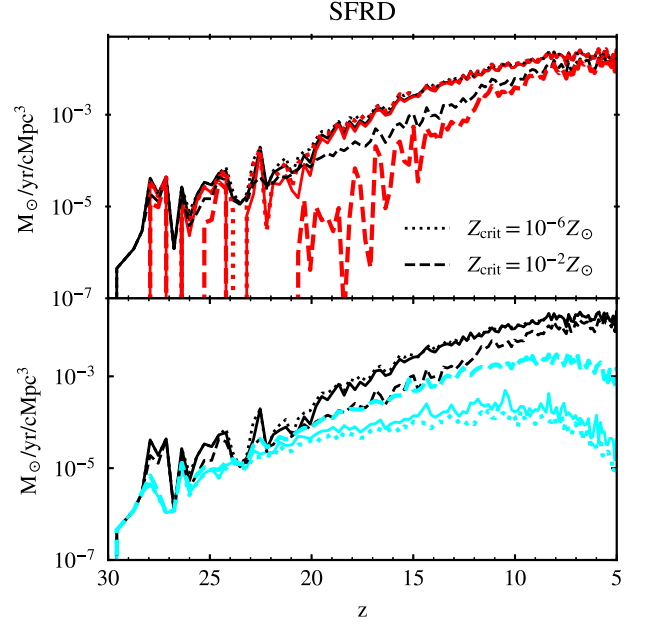


Figure 14. As Fig. 7 using the fiducial model (solid), $Z_{\text{crit}} = 10^{-6}$ (dotted) and $10^{-2} Z_{\odot}$ (dashed).

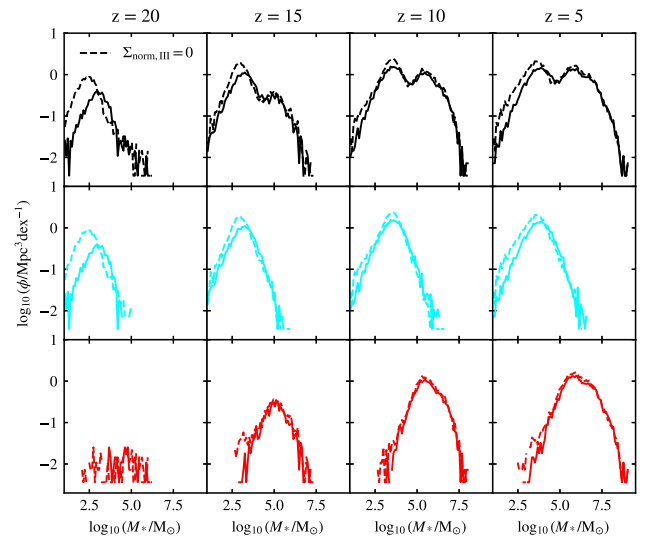


Figure 15. As Fig. 5 using the fiducial model (solid) and $\Sigma_{\text{norm, III}} = 0$ (dashed).

case of $\Sigma_{\text{norm, III}} = 0$, which is equivalent to assuming that Pop. III stars start to form as soon as the cooling of the gas begins, and all cold gas is available to form Pop. III stars (in proportion to the star formation efficiency). This choice results in a larger abundance of low-mass Pop. III systems at high- z (the largest difference between the cyan dashed and solid line in Fig. 15 are at $z = 20$ and 15).

However, since the main changes in the Pop. III SF are in low-mass haloes, setting $\Sigma_{\text{norm, III}} = 0$ does not significantly change the SFRD history (see Fig. 16 where the cyan dashed line is only slightly lower than the fiducial model).

Overall, this free parameter is the one with the smallest impact on the star formation history, as it only impacts the low-end of the stellar mass function at high- z for which there are no observational constraints.

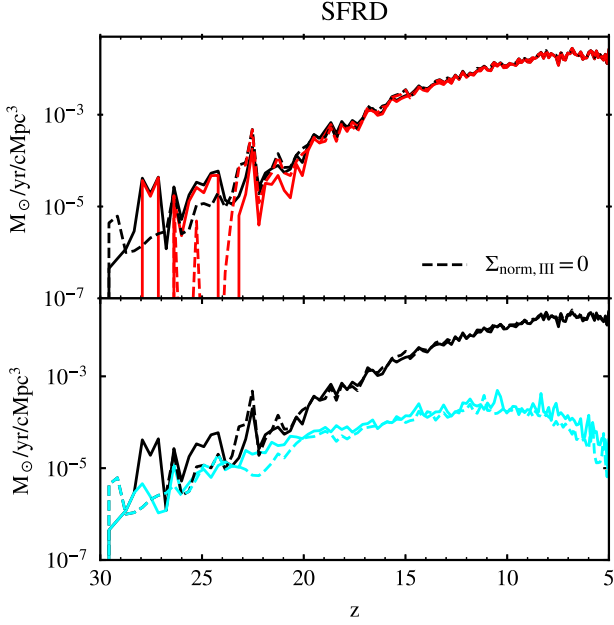


Figure 16. As Fig. 7 using the fiducial model (solid) and $\Sigma_{\text{norm, III}} = 0$ (dashed).

3.2.4 IMF

The last parameter we explore is the IMF of Pop. III stars. Our fiducial model is quite similar to the Pop. II IMF as we assume a Salpeter IMF that favours the formation of low-mass stars. The only difference is that we take larger lower and upper limits (1 and $500 M_{\odot}$). We consider two log-normal IMFs labelled log A and log E as in Tumlinson (2006) with the parameters summarized in Table 2. For these IMFs, we have spectral energy distributions (from Raiter et al. 2010), which will be used in Section 4. The IMF logA is centred at $M = 10 M_{\odot}$, which enhances the probability of a Pop. III stars ending its life as a core-collapse SN. log E is centred at even a higher mass ($M = 60 M_{\odot}$), so we expect most of the stars with very short lifetimes to end their lives by collapsing into a black hole without any supernova explosion. Compared to the Salpeter IMF, both log-normal IMFs do not have many low mass stars ($M < 8 M_{\odot}$).

Decreasing the lifetime of Pop. III stars makes the Pop. III SMF in Fig. 17 shift to lower masses, increasing the separation between the two peaks of the total SMF (the effect of changing the IMF towards higher masses is the opposite of increasing the SF efficiency). The difference between the fiducial model and one adopting the logA IMF is less than one dex. However, in the logE IMF model, most of the stars die in the same snapshot in which they form (the lifetime of a $60 M_{\odot}$ star is ~ 4.5 Myr, which at $z < 15$ is less than the time separation between two consecutive snapshots in MERAXES, see also Fig. 4). This effect strongly prevents the build-up of Pop. III systems, and in Fig. 17, we can see that the most massive Pop. III galaxies at $z = 5$ have $M \sim 10^5 M_{\odot}$. There are no differences in the Pop. II SMF with different IMFs.

In difference from the SF efficiency, the IMF mostly affects the stellar mass function. This is because the main change is with respect to the lifetime of Pop. III stars. In Fig. 18, we see that there are no significant differences in the SFRD from adopting different IMFs, except for the first few snapshots of our simulation, where the star formation is mildly reduced in the logE model. This result comes from the stronger feedback typical of the more top-heavy IMF (a larger number of massive stars implies more supernovae), and it

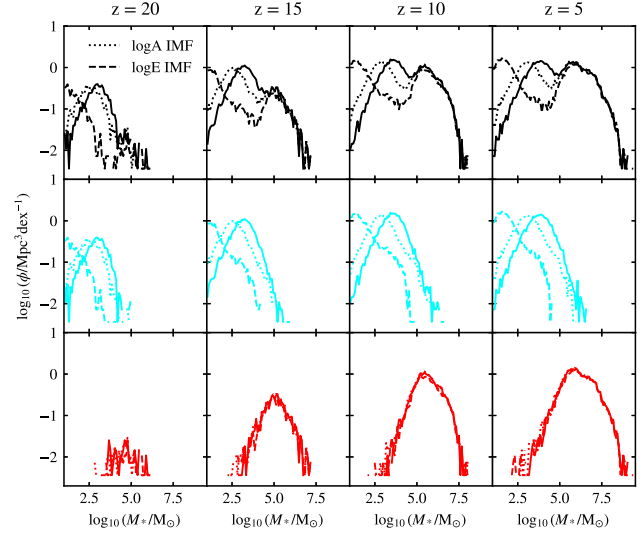


Figure 17. As Fig. 5 using the fiducial model (solid), the log A IMF (dotted) and the log E IMF (dashed).

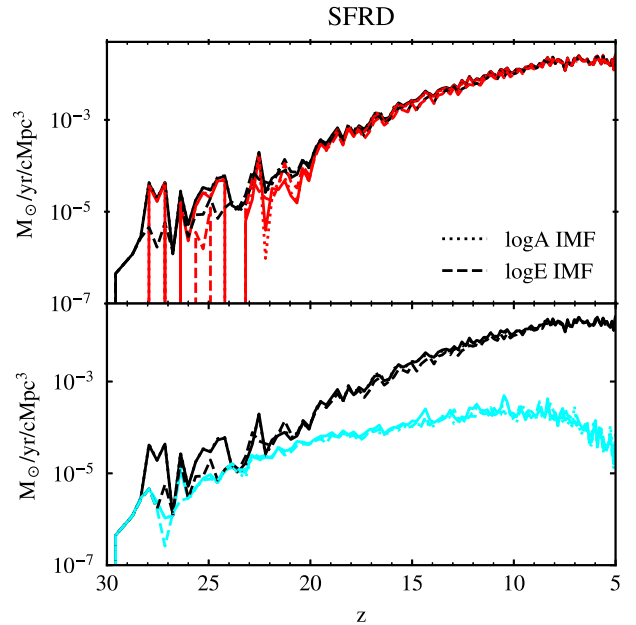


Figure 18. As Fig. 7 using the fiducial model (solid), the log A IMF (dotted) and the log E IMF (dashed).

has a stronger impact at $z \geq 24$ when Pop. III star formation is dominating.

In conclusion, the global evolution of Pop. III stars is strongly dependent on the star formation efficiency because high $\epsilon_{\text{SF, III}}$ increases both the SMF and the SFRD. The evolution is also dependent on the IMF adopted (although the IMF affects only the SMF). The critical metallicity has an impact only if we consider a high value, and it mostly affects the self-enrichment as most of the galaxies in our simulation get their metals from their own star formation rather than from an external metal bubble. The critical surface density instead has only a small impact on the Pop. III star formation history, and it is restricted to small mass haloes and high- z .

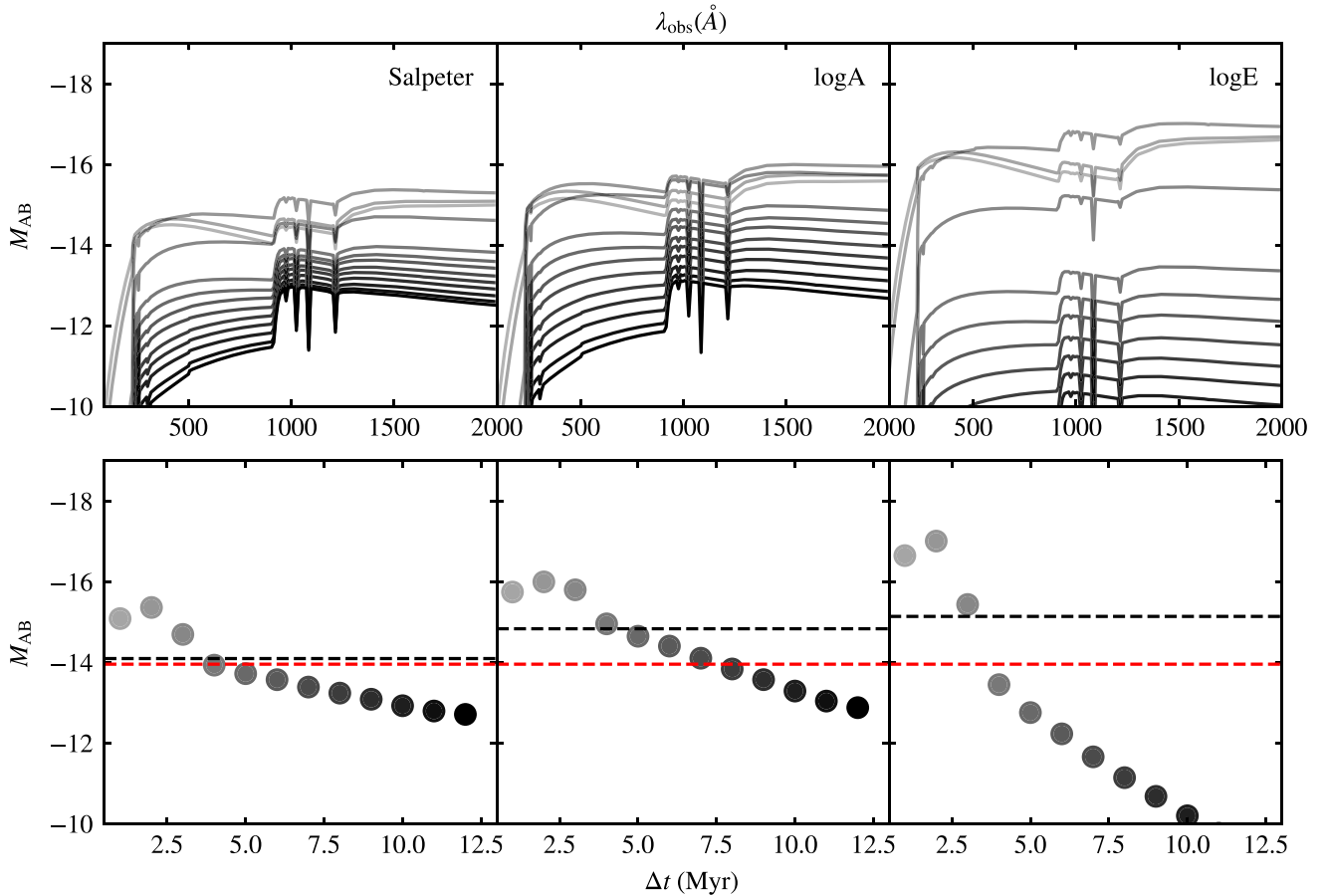


Figure 19. *Top:* time evolution of the SED of the brightest Pop. III galaxy at $z = 8$, assuming a Salpeter (left), log A (mid), log E (right) IMF. Lighter lines assume a smaller Δt since the star formation burst. *Bottom:* Absolute UV magnitude of the same galaxy as a function of Δt in Myr. The black (red) horizontal line shows the magnitude value of the galaxy assuming a Pop. III (Pop. II) continuous star formation.

4 POP. III OBSERVABILITY WITH JWST

Unconstrained Pop. III free parameters in our model have an impact on the redshift evolution of the SMF and SFRD. However, our model predicts a consistent number density of Pop. III dominated systems with stellar masses between 10^3 – $10^5 M_{\odot}$. Here, we will explore the UV luminosity of these systems using the model described in Section 2.7 focusing on the luminosity functions at very high- z .

Given the same total stellar mass, Pop. III systems have larger luminosities compared to Pop. II galaxies, but shine for shorter times. This is demonstrated in Fig. 19, where we show the evolution in the first 10 Myr of the SED of a Pop. III galaxy that forms $10^5 M_{\odot}$ Pop. III stars at $z = 8$ (top panels) and the absolute UV magnitude (bottom panels) at different times Δt since the star formation burst. Left-hand, mid, and right-hand panels assume a Pop. III Salpeter, log A and log E IMF, respectively. The black horizontal line corresponds to the magnitude computed, assuming a continuous star formation throughout the snapshot. For reference, we also show the magnitude of a Pop. II galaxy forming the same amount of Pop. II stars (red dashed line). First, we notice that Pop. III galaxies with continuous star formation and a log-normal IMF are one magnitude brighter than Pop. II galaxies with the same SFR (while there is no significant difference if Pop. III stars follow a Salpeter IMF). Once we focus on the instantaneous star formation model for Pop. III stars, the brightness of the galaxy can be boosted (or reduced) by several magnitudes depending on the time Δt following the burst at which

we are observing the system (see also Trussler et al. 2023). Even when we consider a Salpeter IMF, the brightness of a Pop. III galaxy changes ~ 2 mags in ~ 10 Myr. This change is more dramatic for the log-normal IMFs (especially for the log E IMF where in 10 Myr $\Delta M_{AB} \simeq 7$ mags). The large difference between the instantaneous and continuous star formation models shown in Fig. 19 for a single Pop. III galaxy will reflect on the entire population and potentially lead to a higher number density of extremely bright Pop. III galaxies.

Fig. 20 shows the luminosity function (computed as described in the Appendix B). As a result of instantaneous Pop. III star formation, there are chances to observe these galaxies at a time when their luminosities are higher than what is given by the continuous scenario. This is reflected in Fig. 20 where we see the bright end of the solid cyan line shifting to higher luminosities. When looking at the total luminosity function, we see a much significant Pop. III contribution to the number density of galaxies around $M_{AB} \sim -16$ when assuming a Log E IMF for their SF.

Given their larger brightness, a population of Pop. III galaxies with a top-heavy IMF has been suggested as a possible explanation for the abundance of bright galaxies at $z > 10$ (see e.g. Trinca et al. 2023; Harikane et al. 2023 and Yung et al. 2024). Without invoking any exotic physics or a revision of the standard Λ CDM model of cosmology, other possible explanations are a combination of increased star formation efficiencies at high- z and reduced feedback (Qin, Balu & Wyithe 2023), bursty star formation (Sun et al. 2023), cosmic variance (Shen et al. 2023), and a modified Λ CDM power

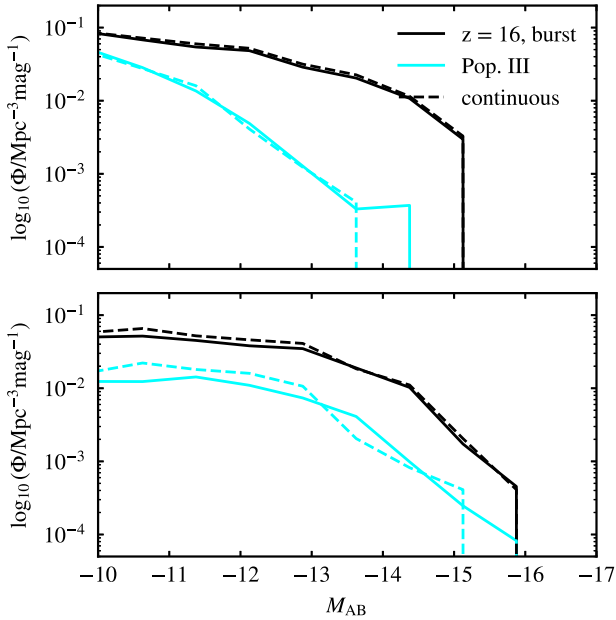


Figure 20. Total (black) and Pop. III (cyan) UV luminosity function at $z = 16$ assuming the Salpeter (top) and the logE (bottom) IMF. Solid lines are computed assuming that Pop. III stars form in a single burst, dashed lines take a continuous star formation model.

spectrum (Padmanabhan & Loeb 2023; Parashari & Laha 2023). Here, we show the predicted UV luminosity functions at $z = 16, 12, 11, 10, 9$ (we chose these values as the ones for which there are more *JWST* observations available). Results for different IMFs and different star formation efficiencies are summarized in Fig. 21, where all the other Pop. III parameters are taken as in the fiducial model. For all the models considered below, our total luminosity function agrees with early *JWST* observations at $z \leq 12$ (except for the points at $M_{\text{AB}} < -19$, where we do not have galaxies in MERAXES).

With our fiducial parameters (dashed lines), both with the Salpeter and with the log A IMF (upper and middle row), we find that Pop. III systems are not the brightest galaxies at the redshift considered ($M_{\text{AB}} \geq -14$). However, when we consider a log-normal IMF with a characteristic mass of $60 M_{\odot}$ (lower row), Pop. III galaxies become significantly brighter (the cyan line approaches the black line) and at $z = 12$ and 16 when some of the brightest systems ($M_{\text{AB}} \sim -16$) are Pop. III dominated. Even though most of the Pop. III galaxies are still very faint (well below the sensitivity of *JWST*). This result may indicate that Pop. III dominated galaxies are present at $z > 12$.

This result becomes more robust when considering $\alpha_{\text{SF, III}} = \alpha_{\text{SF, II}}$ (solid lines). The bright end of the total and Pop. III dominated galaxy UVLF shifts of 1–2 mag (depending on the IMF) at $z = 16$ and 12 . At $z \leq 11$, there is no or little difference in the total UVLF with different star formation efficiency even though Pop. III dominated galaxies are still ~ 1 mag brighter. Models with a Salpeter or a log-normal IMF centred at $10 M_{\odot}$ predict that the bright end of the UVLF at $z = 16$ is impacted by Pop. III dominated systems while at $z \leq 12$, none or very few of the brightest galaxies are Pop. III dominated. Overall, the abundance of bright galaxies at $z \geq 12$ is better explained by the model with the log E Pop. III IMF and $\alpha_{\text{SF, III}} = \alpha_{\text{SF, II}} = 0.08$. For this model at $z \geq 12$, we find Pop. III dominated galaxies with $M_{\text{AB}} \simeq -18$ and at $z = 16$ all the brightest galaxies ($M_{\text{AB}} \leq -16$) are Pop. III dominated.

The results discussed above considered a star formation efficiency $\alpha_{\text{SF, III}} \geq 0.008$, which allows the formation of Pop. III stellar systems in MERAXES with masses up to $\sim 10^5 M_{\odot}$. These values are substantially higher than what predicted by some hydro-dynamical simulations (e.g. Xu et al. 2016; Sarmiento & Scannapieco 2022). This may suggest lower star formation efficiencies than what considered in this work making Pop. III galaxies much fainter and very unlikely to be observed. We compared our results with Trinca et al. (2023) (black pentagons in Fig. 21), and found a good agreement at $z \leq 12$ and $M_{\text{AB}} \lesssim -16.5$ for all the models considered. The main differences are that at $z = 9$, we do not have any galaxy with $M_{\text{AB}} \sim -20$, and their model has a steeper evolution predicting many more faint galaxies. At $z = 16$ only models with $\alpha_{\text{SF, III}} = 0.08$ and a log-normal IMF reproduce their results at $-14 \leq M_{\text{AB}} \leq -18$. Even though the total UVLF is similar, their Pop. III contribution is significantly lower, especially when compared to the models with $\alpha_{\text{SF, III}} = 0.08$ (their results predict that less than 10 per cent of bright galaxies at $z = 15$ – 16 host an active Pop. III stellar population). Given that the choice of Pop. III free parameters is similar (they also take $\alpha_{\text{SF, III}} \sim 0.1$ and account for a critical surface density of the cold gas before forming Pop. III stars). The main differences in the model that can explain the different results are (i) the homogeneous feedback and (ii) the Pop. III luminosity calculation. In their model, both the radiative feedback and the chemical enrichment are homogeneous; this might overestimate the suppression of Pop. III systems at $z \sim 10$ – 20 (when the LW background is effective). Regarding the second point, our model accounts for the fact that a Pop. III galaxies might be observed immediately after they formed stars. As shown in Fig. 20, this enables us to boost the luminosity of some Pop. III dominated galaxies by several magnitudes. Without accounting for this effect, our Pop. III galaxies would have a similar luminosity to those predicted by Trinca et al. (2023).

The main limitation of our results is that, given the small size of the simulation, we intrinsically miss the brightest galaxies (at $z \geq 9$, we do not get galaxies brighter than $M_{\text{AB}} \simeq -19$). Larger simulation volumes will allow us to be conclusive, but this result suggests that if Pop. III stars are still forming at $z \geq 10$ – 12 , and they have a top-heavy IMF, they do not require increased star formation efficiencies to outshine the Pop. II systems. As Pop. III dominated galaxies become much more rare at $z \lesssim 10$, this scenario allows us to increase the abundance of bright galaxies only at $z > 10$ without boosting the bright end of the UV luminosity function at lower redshift hence we achieve a good agreement with early *JWST* observations from Donnan et al. (2023), Harikane et al. (2023), and Pérez-González et al. (2023).

5 CONCLUSIONS

In this paper, we studied Pop. III star formation in mini-haloes with an updated version of the MERAXES semi-analytic model of galaxy formation that includes LW background and the streaming velocities. We also implemented external metal enrichment following the growth of the supernova bubbles according to the Sedov–Taylor model. We computed the bubble size distribution function and found that our results agree with Trenti et al. (2009) (most bubbles are smaller than $150 h^{-1} \text{ ckpc}$ at $z = 6$ and have a typical size of 100 – 200 ckpc at $z = 5$), hence most haloes get self-enriched rather than externally polluted. Only low-mass haloes ($M_{\text{vir}} \leq 10^{7.5} M_{\odot}$) at $z < 10$ are more likely to get their metals from the IGM. This is a consequence of the small size of the supernova bubbles that results in a small filling factor (0.1 per cent at $z = 12$ and less than 1 per cent at $z = 5$).

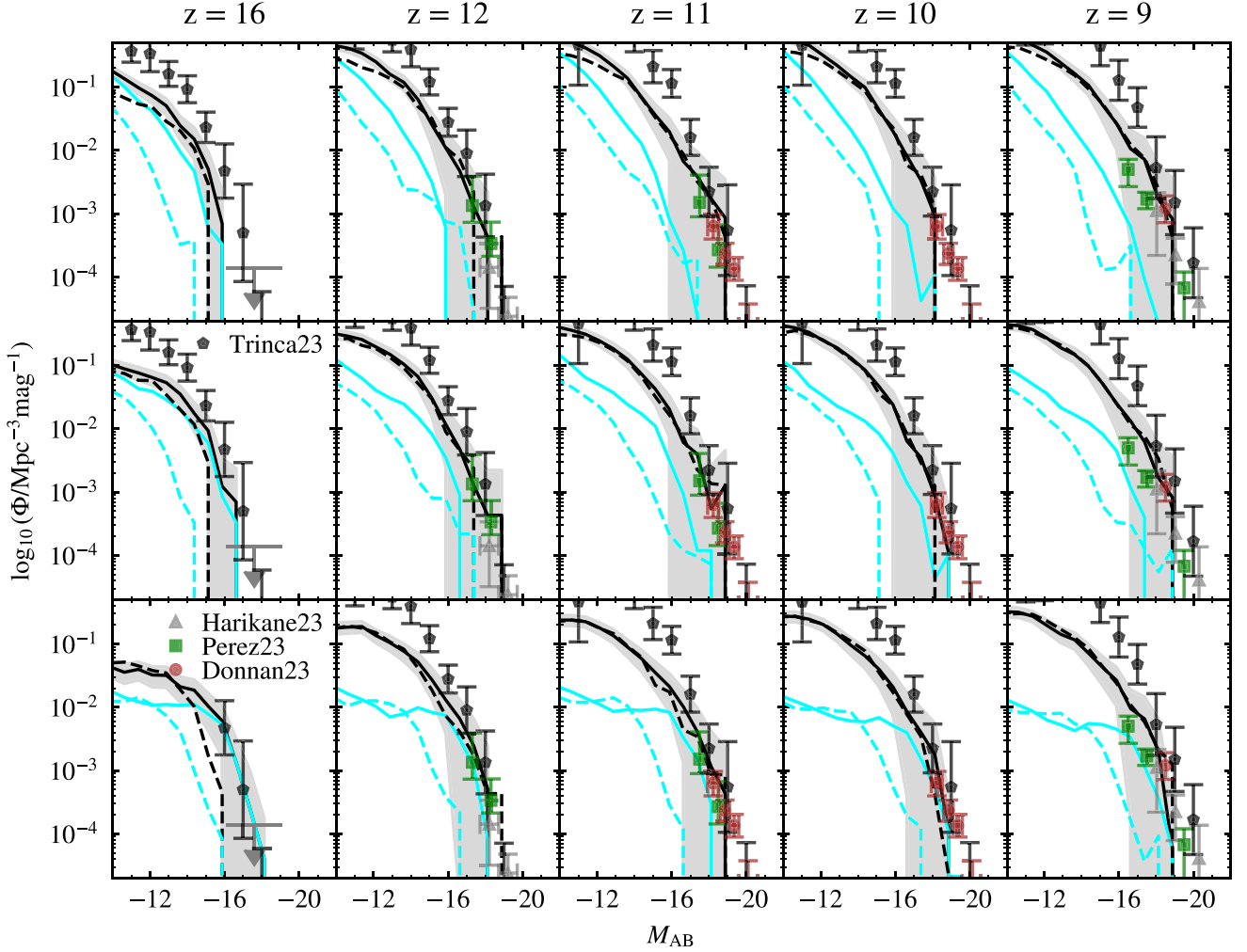


Figure 21. Total (black) and Pop. III dominated galaxies (cyan) UV LF at $z = 16, 12, 11, 10, 9$ (from left to right) for the Salpeter, log A, and log E IMF (from top to bottom) and $\alpha_{\text{SF, III}} = 0.08$ (solid), 0.008 (dashed). Uncertainties for the black solid line are shown with shaded regions (computed using the Poisson error). Data points highlight recent *JWST* results from Donnan et al. (2023); Harikane et al. (2023); Pérez-González et al. (2023), and the results from the simulation of Trinca et al. (2023).

The free parameters allow us to explore the global properties of Pop. III dominated galaxies. We ran this model on top of a dark matter-only N -body simulation able to resolve all the mini-haloes down to $\sim 3 \times 10^5 M_{\odot}$ at $z \leq 30$. We explored the impact on the SMF and SFRD of the main free parameters of our model. All models converge at $z \lesssim 10$. However, Pop. III star formation efficiency and IMF lead to differences at high- z .

Finally, we investigated the SED evolution of a Pop. III dominated galaxy for different IMFs. The shorter lifetime of a Pop. III galaxy motivated us to use an instantaneous star formation model when computing the luminosity function. We computed the total and the Pop. III galaxy UV luminosity functions and compared these to the early *JWST* results in order to study whether the excess of bright galaxies at high- z could be explained by a population of Pop. III dominated galaxies. Having explored different IMFs and star formation efficiencies, our model predicts, for a log-normal IMF with a characteristic mass of $60 M_{\odot}$ and a Pop. III star formation efficiency comparable to the Pop. II, most of the brightest galaxies at $z \geq 12$ and all at $z = 16$ ($M_{\text{AB}} = -18$) are Pop. III dominated. Even with a smaller mass or a Salpeter IMF, Pop. III dominated systems still have an impact on the bright end of the

UVLF at $z = 16$. In conclusion, this work supports the scenario for which top-heavy Pop. III dominated galaxies might explain the abundance of bright *JWST* galaxies at $z \geq 12$ without requiring very high star formation efficiencies or extremely weak feedback at high- z .

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DATA AVAILABILITY

The main data presented in this work have been analysed with the DRAGONS⁷ and SECTOR⁸ PYTHON packages publicly available. The latest version of MERAXES is now publicly available on GitHub here.⁹ The output of the high-resolution *N*-body simulation used in this work can be downloaded from Zenodo at Balu et al. (2024). Further data and codes will be shared on reasonable request to the corresponding author.

REFERENCES

- Balu S., Greig B., Qiu Y., Power C., Qin Y., Mutch S., Wyithe J. S. B., 2023, *MNRAS*, 520, 3368
- Balu S., Power C., Mutch S., Qin Y., Ventura E. M., 2024, Dark Matter Halo Merger Trees. Zenodo. Available at: <https://doi.org/10.5281/zenodo.10608236>
- Barkana R., Loeb A., 2001, *Phys. Rep.*, 349, 125
- Barkana R., Loeb A., 2005, *ApJ*, 626, 1
- Bosman S. E. I. et al., 2022, *MNRAS*, 514, 55
- Bromm V., Coppi P. S., Larson R. B., 1999, *ApJ*, 527, L5
- Chiaki G., Wise J. H., 2023, *MNRAS*, 520, 5077
- Chiaki G., Yoshida N., 2022, *MNRAS*, 510, 5199
- Chon S., Omukai K., Schneider R., 2021, *MNRAS*, 508, 4175
- Chon S., Ono H., Omukai K., Schneider R., 2022, *MNRAS*, 514, 4639
- Correa Magnus L., Smith B. D., Khochfar S., O’Shea B. W., Wise J. H., Norman M. L., Turk M. J., 2023, *MNRAS*, 527, 307
- Crosby B. D., O’Shea B. W., Smith B. D., Turk M. J., Hahn O., 2013, *ApJ*, 773, 108
- Dijkstra M., Ferrara A., Mesinger A., 2014, *MNRAS*, 442, 2036
- Donnan C. T. et al., 2023, *MNRAS*, 518, 6011
- Elahi P. J., Cañas R., Poulton R. J. J., Tobar R. J., Willis J. S., Lagos C. d. P., Power C., Robotham A. S. G., 2019a, *PASA*, 36, e021
- Elahi P. J., Poulton R. J. J., Tobar R. J., Cañas R., Lagos C. d. P., Power C., Robotham A. S. G., 2019b, *PASA*, 36, e028
- Feathers C. R., Visbal E., Kulkarni M., Hazlett R., 2024, *ApJ*, 962, 62
- Fialkov A., Barkana R., Tselikhovich D., Hirata C. M., 2012, *MNRAS*, 424, 1335
- Fukushima H., Yajima H., Sugimura K., Hosokawa T., Omukai K., Matsumoto T., 2020, *MNRAS*, 497, 3830
- Furlanetto S. R., Loeb A., 2003, *ApJ*, 588, 18
- Furlanetto S. R., Zaldarriaga M., Hernquist L., 2004, *ApJ*, 613, 1
- Galli D., Palla F., 1998, *A&A*, 335, 403
- Greif T. H., White S. D. M., Klessen R. S., Springel V., 2011, *ApJ*, 736, 147
- Haiman Z., Bryan G. L., 2006, *ApJ*, 650, 7
- Harikane Y. et al., 2023, *ApJS*, 265, 5
- Hartwig T., Glover S. C. O., Klessen R. S., Latif M. A., Volonteri M., 2015, *MNRAS*, 452, 1233
- Hartwig T. et al., 2018, *MNRAS*, 478, 1795
- Hegde S., Furlanetto S. R., 2023, *MNRAS*, 525, 428
- Heger A., Woosley S. E., 2002, *ApJ*, 567, 532
- Heger A., Woosley S. E., 2010, *ApJ*, 724, 341
- Hirano S., Hosokawa T., Yoshida N., Umeda H., Omukai K., Chiaki G., Yorke H. W., 2014, *ApJ*, 781, 60
- Jaacks J., Thompson R., Finkelstein S. L., Bromm V., 2018, *MNRAS*, 475, 4396
- Jaura O., Glover S. C. O., Wollenberg K. M. J., Klessen R. S., Geen S., Haemmerlé L., 2022, *MNRAS*, 512, 116
- Kauffmann G., 1996, *MNRAS*, 281, 475
- Kennicutt R. C., Jr, 1998, *ApJ*, 498, 541
- Kennicutt R. C., Jr, De Los Reyes M. A. C., 2021, *ApJ*, 908, 61
- Klessen R. S., Glover S. C. O., 2023, *ARA&A*, 61, 65
- Kroupa P., 2001, *MNRAS*, 322, 231
- Kulkarni M., Visbal E., Bryan G. L., 2021, *ApJ*, 917, 40
- Magg M. et al., 2022, *MNRAS*, 514, 4433
- Maiolino R. et al., 2023, *A&A*, preprint (arXiv:2306.00953)
- Mebane R. H., Mirocha J., Furlanetto S. R., 2018, *MNRAS*, 479, 4544
- Mesinger A., Furlanetto S., Cen R., 2011, *MNRAS*, 411, 955
- Mutch S. J., Geil P. M., Poole G. B., Angel P. W., Duffy A. R., Mesinger A., Wyithe J. S. B., 2016, *MNRAS*, 462, 250(M16)
- Mutch S. J., Greig B., Qin Y., Poole G. B., Wyithe J. S. B., 2024, *MNRAS*, 527, 7924
- Nebrin O., Giri S. K., Mellema G., 2023, *MNRAS*, 524, 2290
- Padmanabhan H., Loeb A., 2023, *ApJ*, 953, L4
- Pallottini A., Ferrara A., Gallerani S., Salvadori S., D’Odorico V., 2014, *MNRAS*, 440, 2498
- Parashari P., Laha R., 2023, *MNRAS*, 526, L63
- Pérez-González P. G. et al., 2023, *ApJ*, 951, L1
- Prole L. R., Clark P. C., Klessen R. S., Glover S. C. O., 2022, *MNRAS*, 510, 4019
- Qin Y. et al., 2017, *MNRAS*, 472, 2009
- Qin Y., Mesinger A., Park J., Greig B., Muñoz J. B., 2020, *MNRAS*, 495, 123
- Qin Y., Mesinger A., Bosman S. E. I., Viel M., 2021, *MNRAS*, 506, 2390
- Qin Y., Balu S., Wyithe J. S. B., 2023, *MNRAS*, 526, 1324
- Qiu Y., Mutch S. J., da Cunha E., Poole G. B., Wyithe J. S. B., 2019, *MNRAS*, 489, 1357
- Raiter A., Schaerer D., Fosbury R. A. E., 2010, *A&A*, 523, A64
- Sarmiento R., Scannapieco E., 2022, *ApJ*, 935, 174
- Sarmiento R., Scannapieco E., Cohen S., 2018, *ApJ*, 854, 75
- Sassano F., Schneider R., Valiante R., Inayoshi K., Chon S., Omukai K., Mayer L., Capelo P. R., 2021, *MNRAS*, 506, 613
- Schaerer D., 2002, *A&A*, 382, 28
- Schaller M., Gonnet P., Draper P. W., Chalk A. B. G., Bower R. G., Willis J., Hausammann L., 2018, SWIFT: SPH With Inter-dependent Fine-grained Tasking. Astrophysics Source Code Library, record ascl:1805.020
- Schauer A. T. P., Glover S. C. O., Klessen R. S., Clark P., 2021, *MNRAS*, 507, 1775
- Schneider R., Omukai K., Inoue A. K., Ferrara A., 2006, *MNRAS*, 369, 1437
- Schneider R., Omukai K., Bianchi S., Valiante R., 2012, *MNRAS*, 419, 1566
- Shen X., Vogelsberger M., Boylan-Kolchin M., Tacchella S., Kannan R., 2023, *MNRAS*, 525, 3254
- Skinner D., Wise J. H., 2020, *MNRAS*, 492, 4386
- Smith B. D., Wise J. H., O’Shea B. W., Norman M. L., Khochfar S., 2015, *MNRAS*, 452, 2822
- Sobacchi E., Mesinger A., 2013, *MNRAS*, 432, 3340
- Sobacchi E., Mesinger A., 2014, *MNRAS*, 440, 1662
- Stacy A., Bromm V., Loeb A., 2011, *ApJ*, 730, L1
- Stacy A., Bromm V., Lee A. T., 2016, *MNRAS*, 462, 1307
- Sun G., Faucher-Giguère C.-A., Hayward C. C., Shen X., 2023, *MNRAS*, 526, 2665
- Sutherland R. S., Dopita M. A., 1993, *ApJS*, 88, 253
- Tegmark M., Silk J., Rees M. J., Blanchard A., Abel T., Palla F., 1997, *ApJ*, 474, 1
- Trenti M., Stiavelli M., Shull J. M., 2009, *ApJ*, 700, 1672
- Trinca A., Schneider R., Valiante R., Graziani L., Zappacosta L., Shankar F., 2022, *MNRAS*, 511, 616
- Trinca A., Schneider R., Valiante R., Graziani L., Ferrotti A., Omukai K., Chon S., 2023, *MNRAS*, preprint (arXiv:2305.04944)
- Trussler J. A. A. et al., 2023, *MNRAS*, 525, 5328
- Tselikhovich D., Hirata C., 2010, *Phys. Rev. D*, 82, 083520
- Tumlinson J., 2006, *ApJ*, 641, 1
- Venditti A., Graziani L., Schneider R., Pentericci L., Di Cesare C., Maio U., Omukai K., 2023, *MNRAS*, 522, 3809
- Ventura E. M., Trinca A., Schneider R., Graziani L., Valiante R., Wyithe J. S. B., 2023, *MNRAS*, 520, 3609
- Visbal E., Haiman Z., Bryan G. L., 2015, *MNRAS*, 453, 4456
- Visbal E., Haiman Z., Bryan G. L., 2018, *MNRAS*, 475, 5246
- Visbal E., Bryan G. L., Haiman Z., 2020, *ApJ*, 897, 95

⁷<https://github.com/meraxes-devs/dragons>

⁸<https://github.com/meraxes-devs/sector>

⁹<https://github.com/meraxes-devs/meraxes>

- Welch B. et al., 2022, *Nature*, 603, 815
 Wollenberg K. M. J., Glover S. C. O., Clark P. C., Klessen R. S., 2020, *MNRAS*, 494, 1871
 Xu H., Norman M. L., O’Shea B. W., Wise J. H., 2016, *ApJ*, 823, 140
 Yajima H., Abe M., Fukushima H., Ono Y., Harikane Y., Ouchi M., Hashimoto T., Khochfar S., 2023, *MNRAS*, 525, 4832
 Yamaguchi N., Furlanetto S. R., Trapp A. C., 2023, *MNRAS*, 520, 2922
 Yung L. Y. A., Somerville R. S., Finkelstein S. L., Wilkins S. M., Gardner J. P., 2024, *MNRAS*, 527, 5929

APPENDIX A: TESTING THE EXTERNAL METAL ENRICHMENT

In this appendix, we discuss the extent to which our approximation on the external metal enrichment based on the filling factor is appropriate and when it fails (see Section 2.5 for the detailed implementation).

Since we are avoiding computing all the pairs of distances, there might be some galaxies for which we are not getting a correct enrichment. For this reason, we computed in post-processing the distance between all the pairs of galaxies throughout the entire simulation, and we counted how many galaxies in MERAXES are marked as externally metal enriched (pristine), even if they are outside (inside) a metal bubble. We repeated this computation for several grid resolutions: $N = 16, 32, 64, 128$, and 256 . Hereafter, we will call ‘false pristine galaxies’ those galaxies that lie inside a metal bubble (and so should be enriched) but in MERAXES are labelled as pristine and ‘false enriched galaxies’ those galaxies that are not reached by any bubble but in MERAXES are labelled as enriched.

In the left-hand panel of Fig. A1, we computed the mass fraction of the false pristine (solid line) and false enriched galaxies (dashed line) using different metal grid resolutions. At lower resolution, the percentage of the false pristine galaxies increases from 4 per cent at $N = 128$ (black line) to 7 per cent at $N = 16$ (blue line). This

happens since, as the pixel becomes bigger, the assumption of the galaxies randomly distributed inside each pixel is no longer valid as the clustering becomes much more important. However, when we use a very fine grid ($N = 256$, grey line), the mass fraction of false enriched galaxies dramatically increases at $z \leq 10$. This happens because by $z = 10$, the typical bubble size becomes larger than the pixel volume ($r_{\text{bubble}} \simeq 40\text{--}80$ ckpc, see Fig. 2), and so we lose all the contributions that overflow outside the pixel. The mass percentage of false enriched galaxies instead is only mildly affected by different resolutions (always below 2 per cent). We then compute the absolute value of the difference between the mass percentage of the false pristine and the false enriched galaxies (middle panel). This quantity tells us if, statistically, we are reproducing the correct global enrichment of the Universe, and it tells us whether or not we can apply this model to study the global properties of the Universe. We can see that having a high-resolution grid significantly improves the quality of our results. For $N = 128$, this difference is always below 2 per cent, and at $z < 12$ is approximately 0 per cent. This tells us that for a high-resolution grid, globally, we are getting the correct enrichment of the Universe as the mass percentage of false pristine and false enriched galaxies cancels out. This agreement is almost perfect during the EoR, while during the Cosmic Dawn is still very good, but we are underestimating the metal enrichment of $\sim 1\text{--}2$ per cent. Finally, we are also showing the sum between the false enriched and pristine galaxies (right-hand panel). This quantity instead tells us what is the mass percentage of galaxies for which we are getting a wrong estimation of the enrichment and it is particularly important if we want to apply this model to study analogues. Increasing the resolution improves our result, which, for $N = 128$, peaks at ~ 4 per cent during the Cosmic Dawn. In conclusion, our model for $N = 128$, while reducing the computational cost, still gives an excellent agreement on global enrichment and a very good agreement on the enrichment of single galaxies.

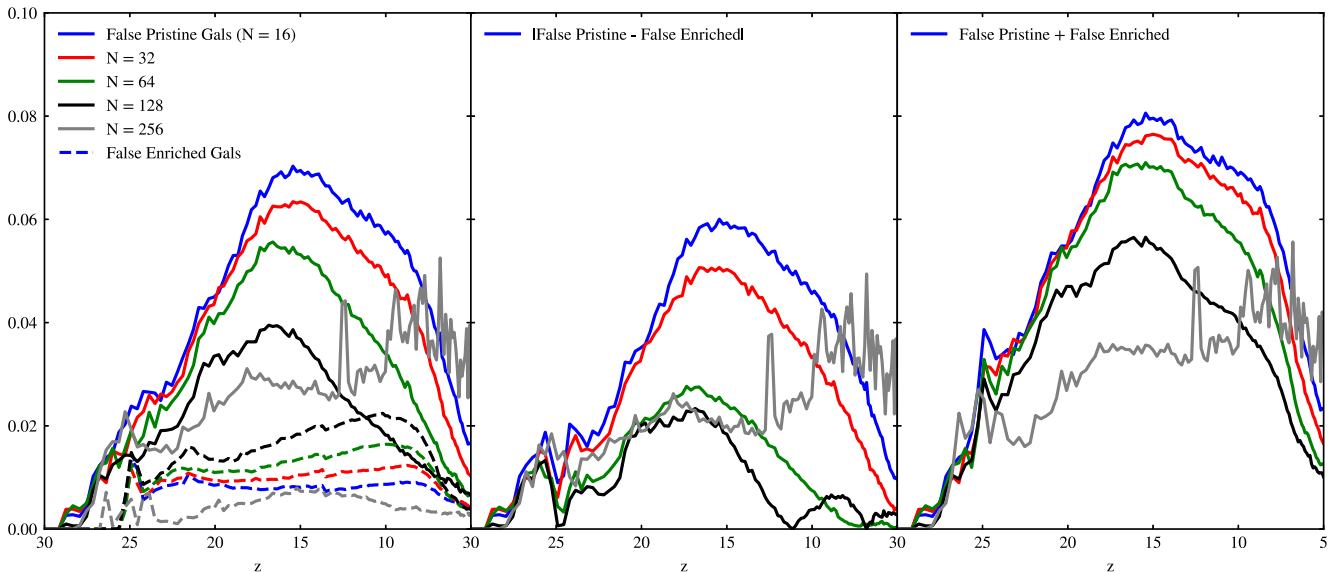


Figure A1. *Left:* mass fraction of false pristine (solid line) and false enriched (dashed line) galaxies (see text for details). Blue, red, green, black, and grey lines refer to different grid resolutions ($N = 16, 32, 64, 128, 256$, respectively). *Centre:* absolute value of the difference between the mass fraction of false pristine and false enriched galaxies. The same colour coding is adopted. *Right:* sum of the mass fraction of false pristine and false enriched galaxies. The same colour coding is adopted.

APPENDIX B: INSTANTANEOUS POP. III STAR FORMATION

In this appendix, we discuss how to evaluate the UV luminosity function of Pop. III galaxies assuming instantaneous star formation. Due to the stochasticity involved in the process of star formation, the burst might occur at any time within a snapshot (with a time duration of t_{snap}) for a galaxy, resulting in different luminosities when observed. We refer to Δt as the time delay of the star formation burst happening relative to the end of our snapshot and draw its value from a random uniform distribution between zero and t_{snap} . One can then evaluate the luminosity of this galaxy, repeat the exercise for all targets after assigning them different Δt , and calculate their probability distribution as a function of UV magnitude (i.e. the UV luminosity function, $\Phi(M_{\text{UV}}, z)$). To achieve a more efficient computation, we instead sample Δt in fine steps of $\Delta t_i = [0.01, 0.5, 1.0, 1.5, \dots, \Delta t_N]$ Myr, with the last sample bracketing the snapshot length as $\Delta t_N \leq t_{\text{snap}} < \Delta t_N + 0.5$ Myr.

Then we calculate the UV magnitudes of each galaxy for given Δt_i and evaluate the corresponding luminosity function at the condition of fixed Δt , $\Phi((M_{\text{UV}}, z)|\Delta t_i)$. Finally, the luminosity function is obtained by summing all conditional probability distributions as

$$\Phi(M_{\text{UV}}, z) = \sum_{\Delta t_i=0.01}^{\Delta t_N} \Phi((M_{\text{UV}}, z)|\Delta t_i) \times P(\Delta t_i). \quad (\text{B1})$$

Note that the probability of each conditional luminosity function is simply

$$P(\Delta t_i) = \begin{cases} \Delta t_i/t_{\text{snap}} & \text{when } i = 1, \\ (\Delta t_i - \Delta t_{i-1})/t_{\text{snap}} & \text{when } 1 < i < N, \\ (\Delta t_i - t_{\text{snap}})/t_{\text{snap}} & \text{when } i = N. \end{cases} \quad (\text{B2})$$

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