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Machine Learning Solutions for Bridge Scour Forecast Based on Monitoring Data

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1 **ABSTRACT**

2 Bridge scour has been a challenge throughout the US and other countries. Despite the scale of the issue,
3 there is still a substantial lack of robust methods for scour prediction to support reliable, risk-based
4 management and decision-making. Throughout the past decade, the use of real-time scour monitoring
5 systems has gained an increasing interest by DOTs (department of transportation) across the US. This paper
6 introduces three distinct methodologies for scour prediction using advanced Artificial Intelligence
7 (AI)/Machine Learning (ML) technics based on real-time scour monitoring data. Scour monitoring data
8 included the riverbed and river stage elevation time-series at bridge piers gathered from various sources.
9 Deep learning algorithms showed promising in predicting bed elevation and water level variations as early
10 as a week in advance. Ensemble neural networks proved successful in predicting the maximum upcoming
11 scour depth, using the observed sensor data at the onset of a scour episode, and based on bridge pier, flow,
12 and riverbed characteristics. In addition, two of the common scour empirical models were calibrated based
13 on the observed sensor data using the Bayesian inference method, showing significant improvement in
14 prediction accuracy. Overall, this paper introduces a novel approach for scour risk management of bridges
15 by integrating emerging AI/ML algorithms with real-time monitoring systems for early scour forecast.

16
17 **Keywords:** Bridge Scour, Artificial Intelligence, Scour Prediction, Scour Monitoring, Deep Learning,
18 Neural Networks, Bayesian Inference, LSTM, Early Warning Systems

1 INTRODUCTION

2 Scour is the number one cause of bridge failure in the US, with approximately 260,000 scour critical
3 bridges across the country. Scour accounts for a significant number of bridge collapses not only in the US
4 (60%), but also in other countries such as New Zealand (62%) and South Africa (21%) [1]. It has been also
5 a major concern for transportation authorities in the UK and Australia.

6 Despite various research efforts, especially in the past two decades, there is still a significant need
7 for developing innovative solutions for more reliable scour predictions and scour risk management. Many
8 studies have applied ML methods for predicting the maximum scour depth, such as self-adaptive
9 evolutionary extreme learning machine [2], artificial neural networks (ANNs) [3,4], the adaptive neuro-
10 fuzzy inference system [5,6], genetic programming (GP) [7], support vector machines [8,9], and gene
11 expression programming (GEP) [10]. These studies have aimed at predicting the maximum scour depth by
12 learning from patterns in field data (and occasionally laboratory data) obtained from direct measurements
13 of scour at bridge piers in various years and locations. However, the common drawback is that the models
14 are trained using data from often geographically limited and scattered locations, therefore their reliability
15 cannot be validated for bridges outside the domain of training data. Given the uncertainty of scour as a
16 physical phenomenon involving complex flow-structure-soil interaction and the lack of reliability in
17 existing predictive models, there is an evident need for regular monitoring of scour at critical bridges with
18 higher risk of scour failure.

19 In the US, Federal Highway Administration (FHWA) requires state DOTs to monitor scour-
20 vulnerable bridges on a regular basis and implement countermeasures to protect them from scour failure.
21 Throughout the past decade, many states have implemented real-time bridge scour monitoring programs.
22 Similarly scour monitoring programs have been devised and implemented by transport authorities in other
23 countries. There are various scour monitoring devices that provide direct measurement of the bed level or
24 depth of scour. Examples of such devices are the followings [11-14]:

- 25 - *Single-use devices*: Installed vertically in the riverbed, and when scour depth reaches the installation
26 depth, the device simply floats out to the surface, triggering an electrical switch.
- 27 - *Pulse or radar devices*: use a radar signal or an electromagnetic pulse to determine changes in the
28 material properties, as a signal is propagated through a changing physical medium. Thus, a pulse is sent
29 along a buried measuring probe, determining the depth of the interface between water and soil, enabling
30 the estimation of scour depth. Such devices can be used to monitor the variation of scour over time.
- 31 - *Buried or driven rod systems*: are based on a gravity-based physical probe that rests on the riverbed
32 and moves downward as scour develops. As the device is based on a gravity sensor, it remains at the
33 lowest depth of scour after each flood, so it is not suitable for monitoring of scour development over
34 time.
- 35 - *Fiber-Bragg Grating devices*: piezo-electric devices, measuring strain along an embedded cantilever
36 rod to generate electrical signals, which indicate the progression of scour along the rod.
- 37 - *Electrical conductivity devices*: use the difference in electrical conductivity of different materials to
38 determine the depth of the water-sediment interface.
- 39 - *Sonar (Soundwave) devices*: are one of the most commonly used scour monitoring sensors and work
40 on the same principle as electromagnetic devices. Waves are reflected through materials of different
41 densities, thus establishing the depth of scour. Sonar sensors operate by releasing a sonic pulse from an
42 emitter, which travels until it is reflected to a receiver due to the change in medium, such as at the
43 sediment-water interface. The time taken for the signal to propagate from the emitter to the receiver
44 can be used to establish the distance to the water-sediment interface. Portable sonar can be a useful
45 bridge inspection tool but does not provide a continuous record of scour development. Fixed sonar has
46 several limitations; the most important one is that sonar measures scour depth within a narrow area
47 around a bridge pier and if the instrument is not mounted above the deepest scour location, it may give
48 a false sense of security.

49 Sonar instrumentation is often used in combination with a Water Stage Sensor (Stage), an ultrasonic
50 distance finder, aimed from a fixed reference point to the water surface. This can help establish the
51 water surface elevation.

1 There are also monitoring methods that identify scour with measurements of structural dynamic
2 properties of the bridge. Limited research has been conducted, trying to determine response of the
3 structure to varying depth of scour [13,15-17]. A disadvantage of this type of sensors is that they do not
4 provide information on the scour depth. They are often used in parallel with depth-measuring
5 instrumentation. Instruments used to measure the structural response to scour include tiltmeters and
6 accelerometers. Tiltmeters measure the relative rotation of a structural element and can be used to detect
7 differential settlement. Accelerometers can help determine changes in the stiffness of the bridge pier-
8 foundation system, caused by scour around the bridge foundation.

9 This study introduces a novel approach using AI/ML to forecast the trend of scour, based on sonar and
10 stage monitoring data around bridge piers. Three methodologies were developed providing algorithms that
11 can 1) make predictions on variation of bed level (therefore scour depth) on a real-time basis and serve as
12 an early warning system for detecting a major scour event in advance, 2) estimate the maximum upcoming
13 scour depth from the onset of a major scour event, 3) calibrate the scour empirical models based on real-
14 time data and then use them to predict the upcoming scour depth with systematic uncertainty assessment.
15 Integrating the proposed technics with the scour monitoring programs can significantly reduce the scour
16 failure risk, especially for large-scale bridges in flood-prone areas.

17 18 **DATA**

19 20 **Data Collection and Characteristics**

21 Despite difficulties in finding legitimate scour monitoring data, such as data quality, confidentiality,
22 and access, various reliable databases from different sources such as Alaska DOT, Minnesota DOT, and
23 USGS were gathered and used for training and validation of AI algorithms. Majority of the training database
24 contained sensor readings from Alaska DOT's scour monitoring program managed by USGS. This dataset
25 includes sonar and stage water readings for more than 20 bridges in Alaska from 2003 to 2017. In addition,
26 training data includes sonar and stage readings for two piers of Winona bridge in Minnesota between 2012
27 to 2017.

28 The received sensor data contains real time readings of bed elevation (sonar) and water level
29 (stage). The list of bridge monitoring data gathered in this study is provided in **Table 1**. **Figure 1** provides
30 plots of sonar and stage data received for bridge 742 in Alaska. It should be noted that sensor readings were
31 not available between November to April for Alaskan bridges due to frozen waters. **Figure 2** shows the
32 installed sensors for bridge 230 and the corresponding historic bed elevation obtained from survey and
33 sounding across the years. Also, **Figure 3** provides a schematic of the installed sensors.

34 In addition to sensor data, relevant information on bridge and river characteristics were collected
35 to inform the analyses using several sources, including National Bridge Inventory (NBI), National Bridge
36 Scour Database, and USGS online reports [18,19]. The key data extracted for the selected bridges is
37 summarised in **Table 2**.

38 39 **Data Quality and Pre-processing**

40 Prior to using the sensor data for model development, extensive pre-processing was performed to
41 generate smooth continuous time series with synchronised steps between sonar and stage readings. Data
42 series were up or down sampled to provide a uniform 1hr time step. In some cases, a portion of data was
43 missing due to issues with the sensors (damages due to debris, etc.) or the readings were noisy and
44 erroneous. Also, sensor reading intervals were not uniform across all the bridges and years of monitoring.
45 **Table 3** provides a summary of data quality issues and pre-processing technics applied to address them,
46 prior to using them for AI/ML. The following main steps were taken for pre-processing of data. The
47 workflow is provided in **Figure 4**.

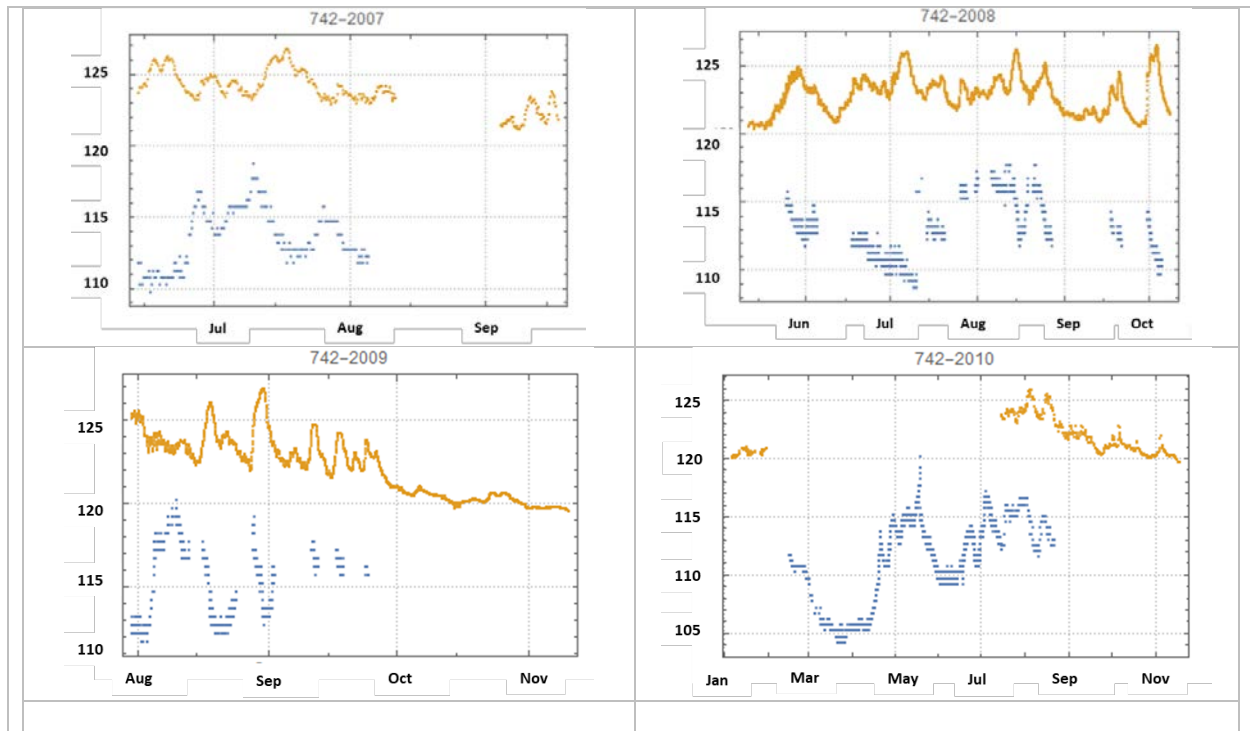
- 48 • Apparent bias shifts in the sensors were corrected based on manual inspection.
- 49 • Outliers were removed via median filtering
- 50 • Timestamps were made uniform (1hr) throughout the dataset and synchronized between sonar and
51 stage

- 1 • Denoising/filtering technics including Moving Average (MA) and Low Pass Filter (LPF) were
- 2 applied to remove high frequency noises and to capture the actual trend
- 3 • Missing data were imputed using polynomial interpolation and Gaussian Process.
- 4

5 **TABLE 1 List of Bridges with Stage and Sonar Data**

Bridge Number	Bridge Name	Years Included
202	Tanana River at Nenana	2003 – 2017
212	Kashwitna River	2004 – 2017
215	Montana Creek	2004 – 2017
230	Sheridan Glacier No. 3	2005 – 2017
524	Tanana River Big Delta	2007 – 2017
527	Salcha River	2003 – 2017
539	Knik River	2003 – 2017
573	Tazlina River	2011 – 2017
634	Twenty Mile River	2011 – 2017
670	Kasilof River	2003 - 2006
742	Chilkat River	2007 – 2017
983	Red Cloud River	2005 – 2017
999	Glacier Creek	2010 – 2017
1020	Quartz Creek	2015 – 2017
1187	Copper River (Flag Pt E)	2014 – 2017
1243	Nenana River at Windy	2003 – 2017
1383	Lowe River at Keystone	2006 – 2017
5900-19	Mississippi River - Winona Bridge/Pier 19	2012 – 2017
5900-20	Mississippi River - Winona Bridge/Pier 20	2012 - 2017

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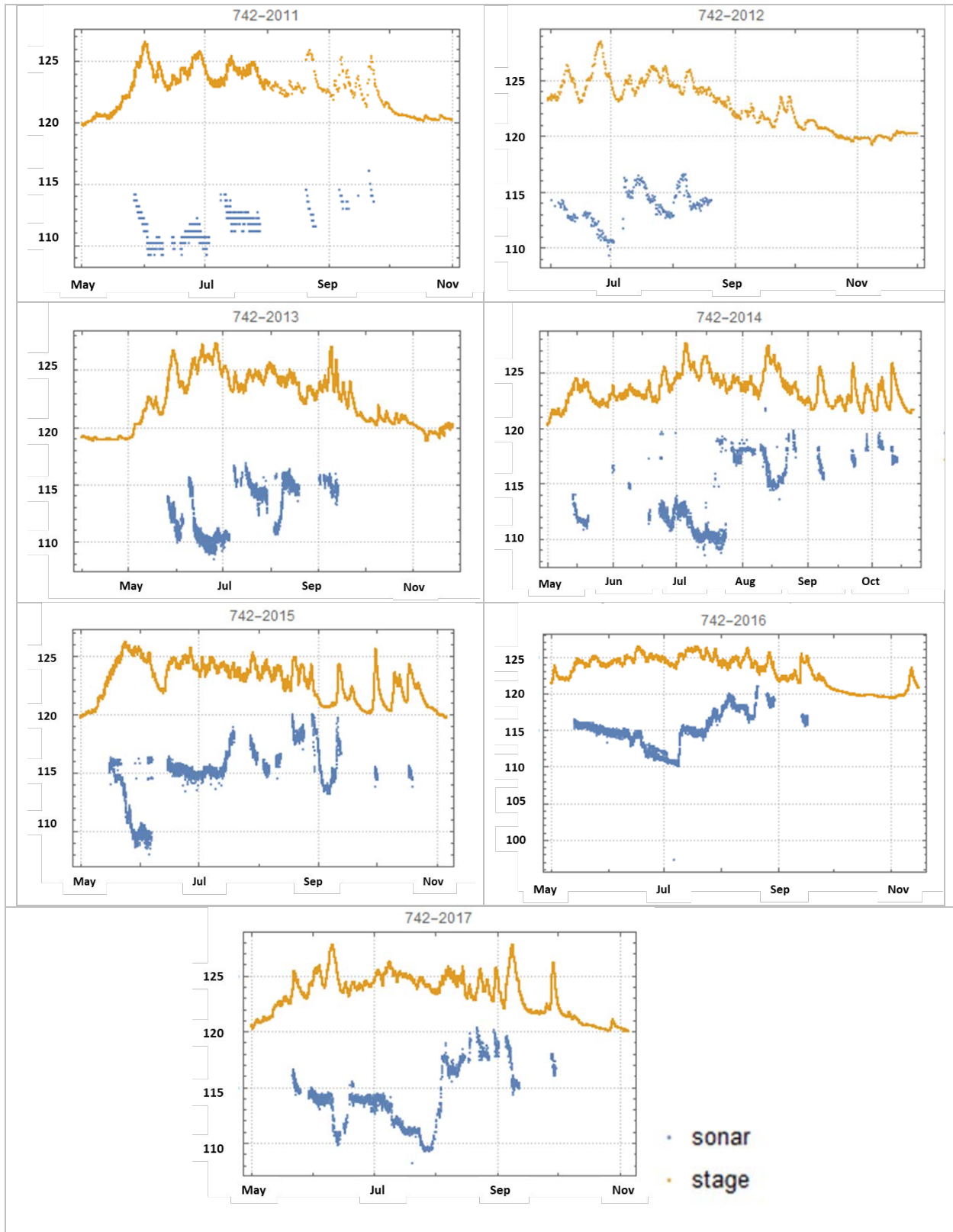
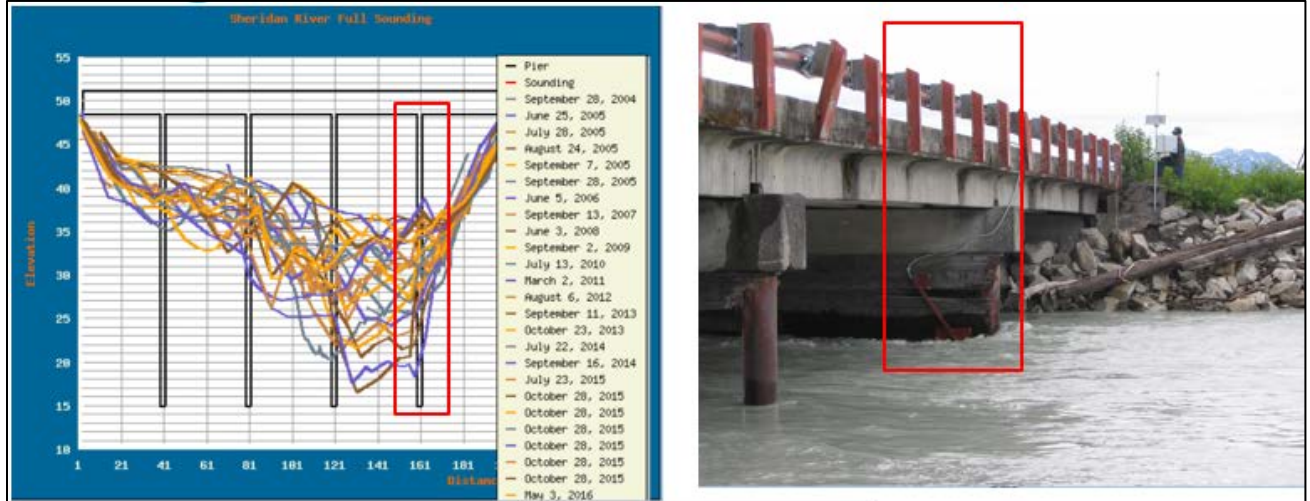
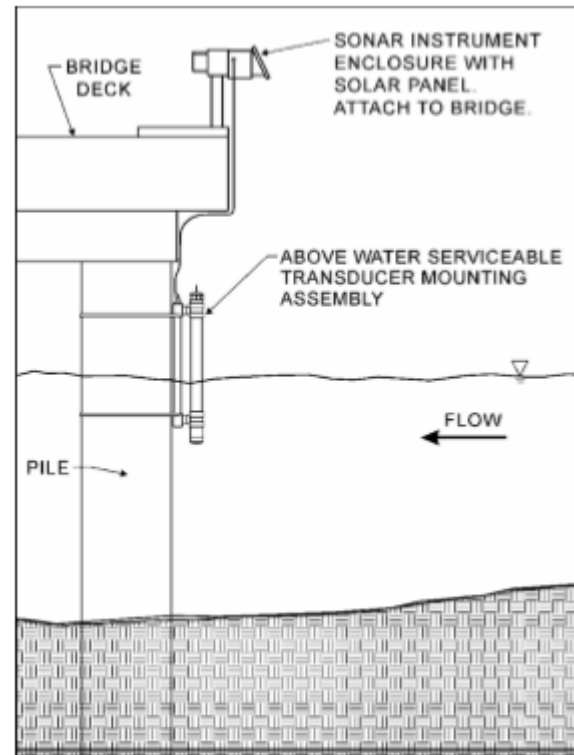
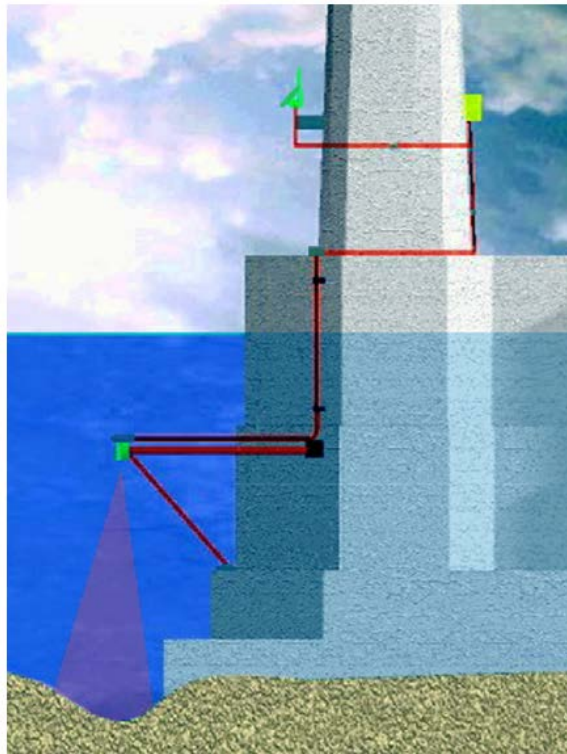


Figure 1 Synchronized stage water and sonar data from 2007 to 2017 – Bridge 742 (x axis is time, y axis is elevation in ft)



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Figure 2 Riverbed profile variations (from sounding) over years (left) and installed scour sensors (right) – bridge 230 [20]



1

2 **Figure 3 Schematic examples of installed sonar sensors at bridge piers [21,12]**

1 **TABLE 2 Summary of Key Scour-Related Characteristics for Selected Bridges**

Bridge NBI ID	River/Bridge Name	Pier Width ft (m)	Pier Spacing ft (m)	Pier Length ft (m)	Manning's Coef.	Valley Slope	D50 inch (mm)	Angle of Attack deg	Discharge 100 RP ft ³ /s (m ³ /s)	Discharge 500 RP ft ³ /s (m ³ /s)
202	Tanana River at Nenana	10 (3)	510 (155.5)	48 (14.6)	0.03	0.008	0.6 (15)	15	162,000 (4,590)	203,000 (5,750)
212	Kashwitna River	5 (1.5)	70 (21.3)	28 (98.5)	0.035	0.002	0.4 (10)	0	3,920 (110)	4,650 (130)
215	Montana Creek	5 (1.5)	62 (19.5)	28 (8.5)	0.035	0.004	0.4 (10)	0	8,270 (230)	11,700 (330)
230	Sheridan Glacier No. 3	5 (1.5)	40 (12.2)	30 (8.5)	0.03	0.0015	0.4 (10)	20	16,300 (460)	20,200 (570)
524	Tanana River Big Delta	5 (1.5)	95 (29.0)	35 (9.4)	0.03	0.0002	0.55 (14)	35	86,700 (2,450)	95,600 (2,700)
527	Salcha River	4 (1.22)	140 (42.7)	35 (10.7)	0.03	0.002	0.4 (10)	10	50,600 (1,430)	64,900 (1,830)
539	Knik River	4.2 (1.31)	180 (54.9)	26 (7.9)	0.046	0.0006	0.2 (5)	0	79,400 (2,250)	104,000 (2,940)
557	Lowe River Lower Cross	2.5 (0.76)	100 (30.5)	38 (11.6)	0.04	0.008	0.4 (10)	0	22,100 (620)	285,000 (8,070)
573	Tazlina River	15 (4.6)	175 (53.4)	35 (10.8)	0.036	0.002	3.54 (90)	35	79,400 (2,250)	10,900 (3,080)
634	Twenty Mile River	5 (1.5)	80 (24.4)	30 (9.1)	0.035	0.0005	0.4 (10)	0	32,500 (920)	35,600 (1,000)
670	Kasilof River	5 (1.5)	110 (33.5)	30 (9.1)	0.035	0.001	0.4 (10)	0	14,500 (410)	16,900 (470)
742	Chilkat River	5 (1.5)	50 (15.2)	24 (7.3)	0.035	0.006	0.4 (10)	0	32,600 (920)	42,900 (1,210)
983	Red Cloud River	5 (1.5)	30 (9.4)	38 (8.5)	0.045	0.02	0.4 (10)	0	1,580 (410)	1,960 (50)
999	Glacier Creek	5 (1.5)	55 (16.8)	30 (9.1)	0.04	0.015	0.4 (10)	20	7,020 (190)	10,200 (280)
1020	Quartz Creek	5 (1.5)	28 (8.5)	13.7 (4.2)	0.03	0.002	0.4 (10)	0	NaN	NaN
1187	Copper River	5 (1.5)	210 (64)	30 (9.1)	0.03	0.00015	0.4 (10)	35	54,400 (1,540)	69,000 (1,950)
1243	Nenana River at Windy	5 (1.5)	190 (58.2)	32 (9.8)	0.05	0.0042	0.4 (10)	0	13,000 (360)	15,400 (430)
1383	Lowe River at Keystone	5 (1.5)	100 (30.5)	36 (11)	0.04	0.005	0.4 (10)	50	21,300 (600)	27,600 (780)
5900-19	Mississippi River-Winona	8 (2.5)	345 (105.5)	30 (9.4)	0.03	0.00001	0.4 (10)	0	NaN	NaN
5900-20	Mississippi River-Winona	11.5 (3.5)	185 (57)	30 (9.4)	0.03	0.00001	0.4 (10)	0	NaN	NaN

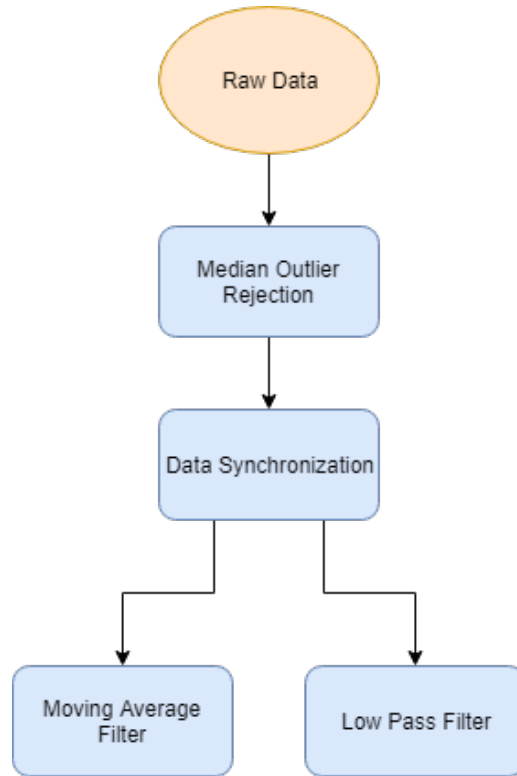


Figure 4 Basic data processing workflow

TABLE 3 Data quality issues and applied pre-processing technics

Data Quality Issue	Applied Processing Technic
Sample rate variability and misalignment between stage and sonar	Each point in the original data is a dual entry of [timestamp, value]. Sequential timestamped entries are not uniformly distributed, i.e., there isn't a standard length between the time steps (typically stage is at a higher sample rate than sonar).
Non-uniform sampling	There are some timestamps that differ from the majority sampling rate, these were detected and culled.
Outlier and spikes	Median filtering (non-linear filter that is effective in removing spikes in data), also applied some low pass filtering.
High frequency noise	Low pass filtering using a range of frequencies.
Bias shifts	A change in bias or a change in datum and units of the data. Manual inspection was performed for correction.
Interruptions to data recording/ Missing data	Missing data occurs throughout the data, particularly in the sonar readings. All data records are composed of shorter sub-sequences generally interspersed with small runs of missing data. Data imputation and interpolation technics were applied.

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1 **METHODOLOGY AND ALGORITHMS**

2 Three distinct methods/algorithms have been developed using advanced AI/ML technics to predict
3 scour depth at bridge piers based on stage and sonar data. The theoretical details of the methods are not
4 provided in this paper. Readers are encouraged to refer to provided references for more background. The
5 following sections discuss each method.
6

7 **Method 1: Bed Elevation and Stage Water Level Prediction using Long-Short Term Memory (LSTM)**
8 **Networks**

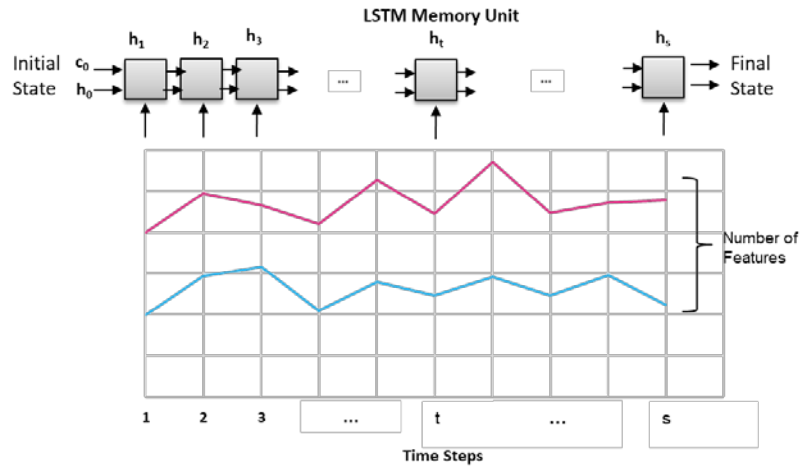
9 LSTM networks were developed in this study with the aim of forecasting trends of bed elevation variation
10 during critical scour episodes. The core idea was to develop an early warning system using algorithms
11 trained on the sensor data that can predict future based on the past.

12 LSTM networks are a type of Recurrent Neural Networks (RNNs) with special internal memory units that
13 can be updated, erased or read out [22,23]. These networks have proven successful for recognizing temporal
14 patterns in time-series data. In addition to feed-forward connections, computational units (neurons) in
15 RNNs have recurrent connections where the output of a unit is fed back to itself with a weight and a time
16 delay, which provides it with a memory of past activations. Stacking memory units in such networks enables
17 learning higher levels of temporal patterns in sequential data. LSTMs have been applied for forecast in
18 time-series data such as stock market trends, text, language and voice recognition [24]. **Figure 5** provides
19 a diagram of the LSTM architecture.

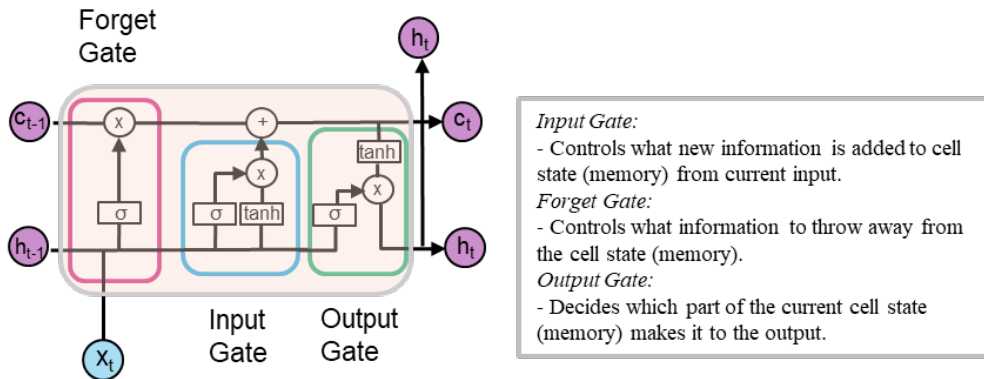
20 A grid search was performed to find the best configuration for LSTMs and to find the optimum values for
21 the hyperparameters. The hyperparameters include the number of LSTM units, number of hidden neurons,
22 optimization algorithm, initial gradient decay rate, maximum number of epochs, training and test data size,
23 and number of sequences (sequence length). **Table 4** provides the range of values tested for each
24 hyperparameter and the selected value for each.

25 LSTM models were trained with a bigger portion of the sequential data (training dataset) and their
26 performance was validated using the remaining of the data (test dataset). The target forecast window was
27 defined to cover both short (1hr in advance) and longer term (7-10 days in advance) predictions. For training
28 the LSTMs, different methods of data slicing and batching were experimented, including: 1) single
29 sequence using continuous data across all years, 2) single sequence using one-year data, 3) multiple
30 sequences from synchronized data across various years, and 4) dividing the data into smaller sequences
31 with a specified length (48 hrs). These sequences were then grouped into a number of mini-batches. The
32 LSTM model was then trained over all these mini-batches in each epoch. An example of training and test
33 sequences is shown in **Figure 6**.

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a)



b)

Figure 5 LSTM network architecture, a) Unfolded in time, b) LSTM Unit Memory

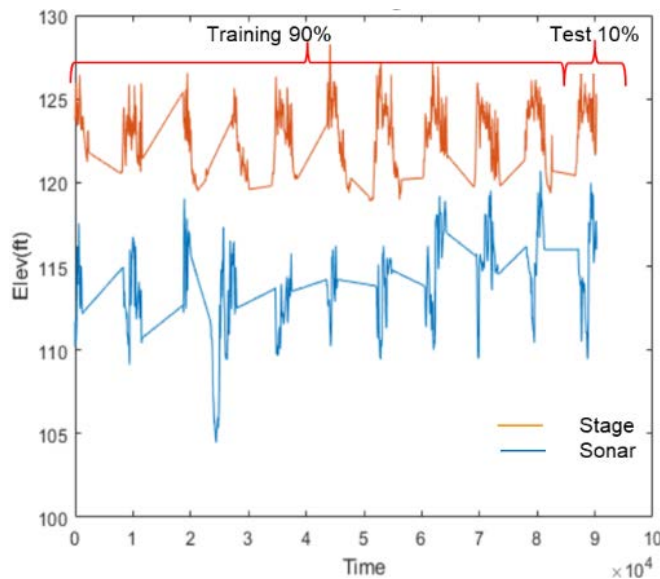


Figure 6 Example of training and test data sequences showing single continuous sequence across eleven years, from 2007 to 2017 (bridge 742), time step= 1hr

1

2 **TABLE 4 LSTM model hyperparameters**

Parameter	Tested Ranges	Selected Value
Number of LSTM Units	1, 2, 5, 10	1
Number of Hidden Neurons	20, 50, 100, 200	100
Optimization algorithm	SGDM, Adam and RMSProp	Adam
Initial Gradient Decay Rate	0.01, 0.005, 0.001	0.005
Max Number of Epochs	50 - 250	Variable depending on the dataset and batch size
Training/Test Data Size	98/2,95/5,90/10	95/5
Number of Sequences (Sequence Length)	One (all years of data in one sequence), No of Years (11), sequence length=48 hrs	-

3

4 **Method 2: Maximum Scour Prediction using Physically Driven Neural Networks**

5 This method aims at providing a holistic predictive model for the maximum depth of scour, not only based
6 on observed scour and stage data but also considering the actual physics of the scour process. The advantage
7 of this method over the first method is that, unlike LSTMs that are bridge-specific, the models can be trained
8 by data from various bridges and subsequently can make predictions for any bridge at any location.

9 Multilayer Perceptron networks (MLPs) are feed-forward neural networks proven successful for prediction
10 and approximation in high-dimensional problems [25-27]. Three-layer MLP networks were developed to
11 predict the maximum scour depth based on selected physical and engineering features (input parameters)
12 governing the scour process. The input parameters included flow, riverbed, and bridge characteristics which
13 are the key components of scour empirical models, such as HEC-18 [28,29] and CIRIA [30] (see **Equations**
14 **2 to 9**).

15 Stepwise parameter selection method was implemented for feature selection. This method includes a
16 forward selection and a backwards elimination of input parameters for the MLP networks [25]. Also, the
17 number of hidden neurons (NH) was a driving factor, as it depends on the number of input parameters. Two
18 sets of analyses were performed with both variable number of number of hidden neurons and a range of
19 fixed values.

20 The model performance was evaluated using adjusted R^2 . The adjusted R^2 penalize the model performance
21 based on the number of input parameters/feature as provided in following equation:
22

$$23 \quad R_{adj}^2 = \frac{(n-1)R^2 - p}{n-1-p} \quad (1)$$

24 where:

25 R_{adj}^2 = Adjusted R^2

26 n = No. of data points presented to the network in the training dataset

27 R^2 = R^2 for the reduced model

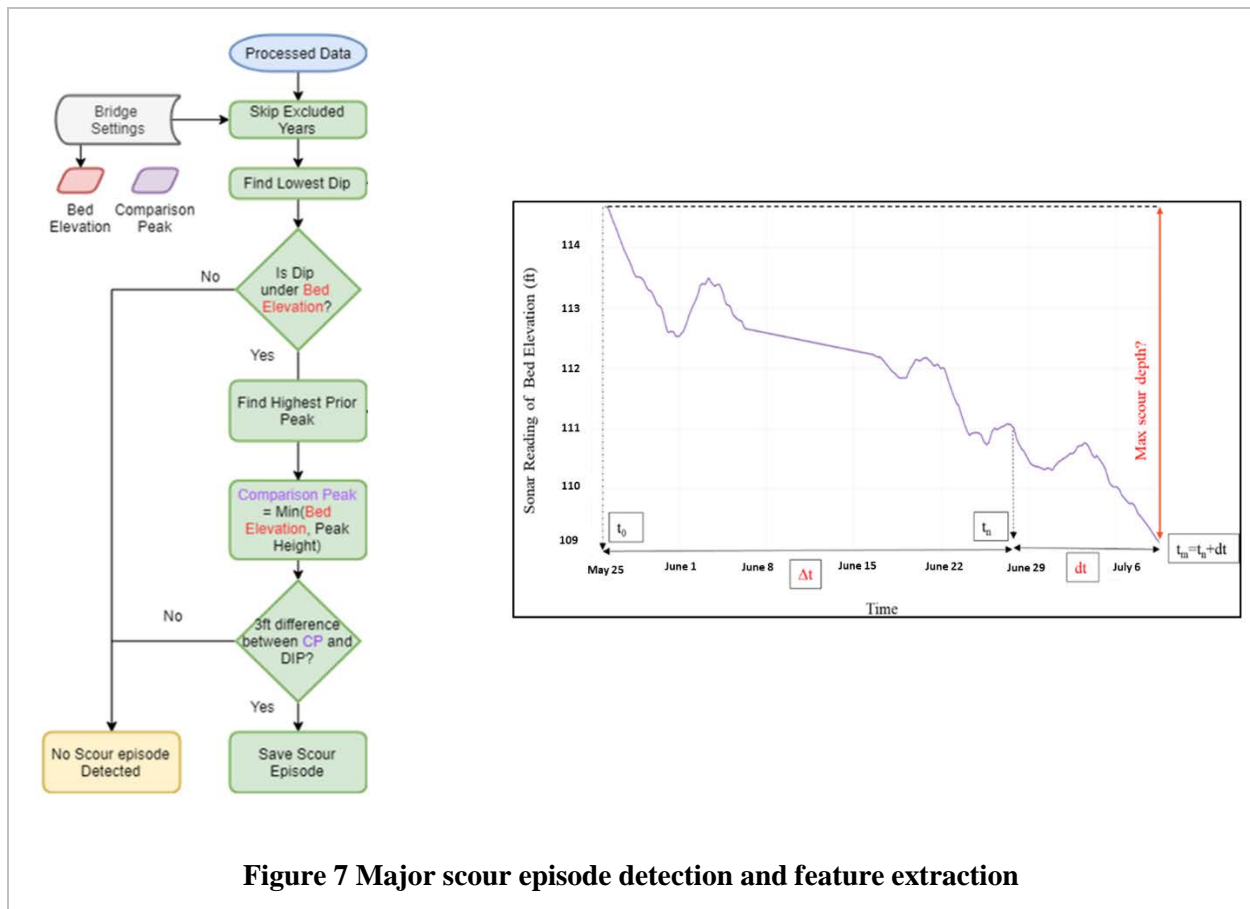
28 p = No. of network parameters (weights and biases) for the reduced model
29

30 The following parameters were gathered as provided in **Table 2**.

- 31 • Pier width (m)

- 1 • Pier spacing (m)
- 2 • Manning’s coefficient
- 3 • Valley slope
- 4 • Pier spacing (m)
- 5 • Pier length (m)
- 6 • Median riverbed particle size - D50 (mm)
- 7 • Flow angle of attack (deg)

8
 9 In addition, the flow depth and scour depth variations during a bridge major scour episode (usually one
 10 major scour episode within a year corresponding to a major flood event) were extracted from the collected
 11 sonar and stage data. Around 70 scour episodes were identified across all bridges in the database from 2007
 12 to 2017. **Figure 7** shows an example of a major scour episode. The criteria for identifying scour was if the
 13 lowest bed elevation is at least 3ft (1m) below the as-built bed elevation of a bridge (the elevation based on
 14 which the bridge foundation was originally designed). Also, in this diagram, t_0 is the starting point of the
 15 scour episode (peak point) and t_m is the time of maximum scour (or the target bed elevation). Based on a
 16 certain forecast window (dt), t_n is defined as the time of last available sonar reading, equal to t_m -dt.
 17



18 The following additional input parameters were extracted from each scour episode:

- 19 • Flow depth at $t_0 = \text{Stage}_{t_0} - \text{Sonar}_{t_0}$
- 20 • Flow depth at $t_n = \text{Stage}_{t_n} - \text{Sonar}_{t_n}$
- 21 • Scour depth at $t_0 = \text{Sonar}_{t_0} - \text{As built elev}$
- 22 • Scour depth at $t_n = \text{Sonar}_{t_n} - \text{As built elev}$
- 23 • Scour episode length, $\Delta t = t_n - t_0$ (hrs)

- Forecast window, $dt = 7\text{days}$ or 40% of Δt (hrs), whichever is smaller (when a scour event happens rapidly, 7 days can be too long relative to the total length of scour episode, therefore 40% of total time is suggested as an alternative)

Figure 8 provides a diagram of the developed MLP networks, showing the architecture, as well as input and target/output parameters. Previous studies on the optimum architecture for MLP networks have shown that one hidden layer is sufficient [25]. The optimum number of hidden units depends on the number of input and model parameters (neural network weights and biases). This was determined through series of experiments on the network performance.

MLPs were trained using random subsampling/Monte Carlo sampling method [25]. Thousands of networks were trained from scratch by randomly sampling data records for training (60%) and test (40%) datasets. Networks were trained using training dataset and their performance were evaluated over the test dataset.

Also, Bayesian Regularization was implemented in the optimization algorithm to enhance the accuracy of predictions [31]. This method automatically detects the most important model parameters (weights) and avoids overfitting to training data. Out of the large pool of generated networks, the ones with the best performance were selected to form an ensemble of predictive models. The accuracy was evaluated based on the average over the network predictions within the ensemble and the uncertainty of the predictions due to network initialization and data subdivision was captured.

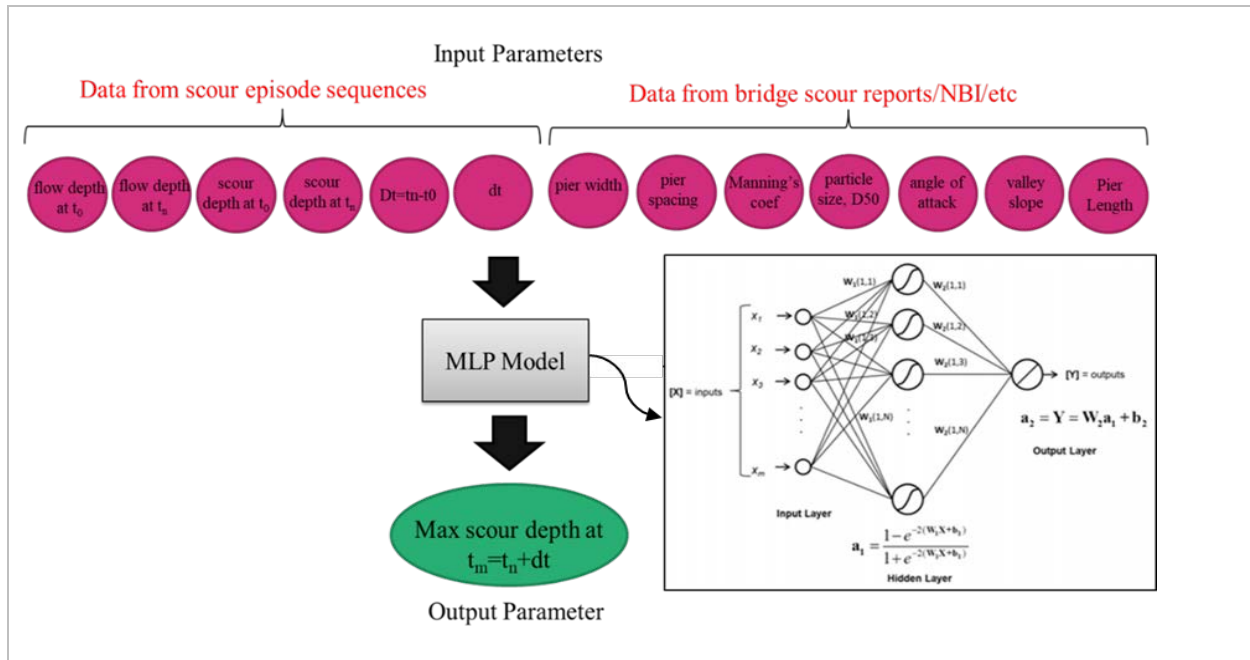


Figure 8 Physically driven neural network approach, showing MLP model architecture and the input and output parameters

Method 3: Scour Prediction and Uncertainty Quantification using Bayesian-Calibrated Empirical Models

Existing studies on empirical scour models show that the majority can result in significant error in scour depth prediction. Most of these models have been calibrated based on local, limited datasets and are not necessarily accurate when applied for an arbitrary bridge [32-34]. Despite the limitations of traditional scour empirical models, their role in management of scour risk is deeply-rooted.

In this study, two scour empirical models were calibrated using the Bayesian inference approach and based on the collected scour monitoring data. The uncertainty over the scour model parameters was modelled by

1 representing them via an initial, assumed probability distributions (prior distribution). Parameters treated
 2 in this manner are referred to as “latent” variables. Using the Bayesian framework, the prior distributions
 3 over the latent variables were updated based on the observed (training) data. The result was a joint
 4 probability distribution, conditional on the observed data, over all the latent variables. Markov-chain Monte
 5 Carlo (MCMC) method was implemented to generate this joint posterior distribution. For more details on
 6 the theory and implementation of Bayesian regression and the MCMC method, readers are referred to
 7 [26,35,36].

8 Probabilistic predictions of scour depth for a given river stage can be made by repeatedly sampling (Monte
 9 Carlo) from the joint posterior distribution over the latent parameters to generate a set of predicted scour
 10 depths. **Figure 9** provides a graphical representation of the Bayesian model structure and prediction of the
 11 bed elevation (sonar) using calibrated empirical models.

12 For implementing this method, the stage water data needs to be predicted in advance. This is possible using
 13 a combination of recorded rainfall in the river catchment and a hydrological model.

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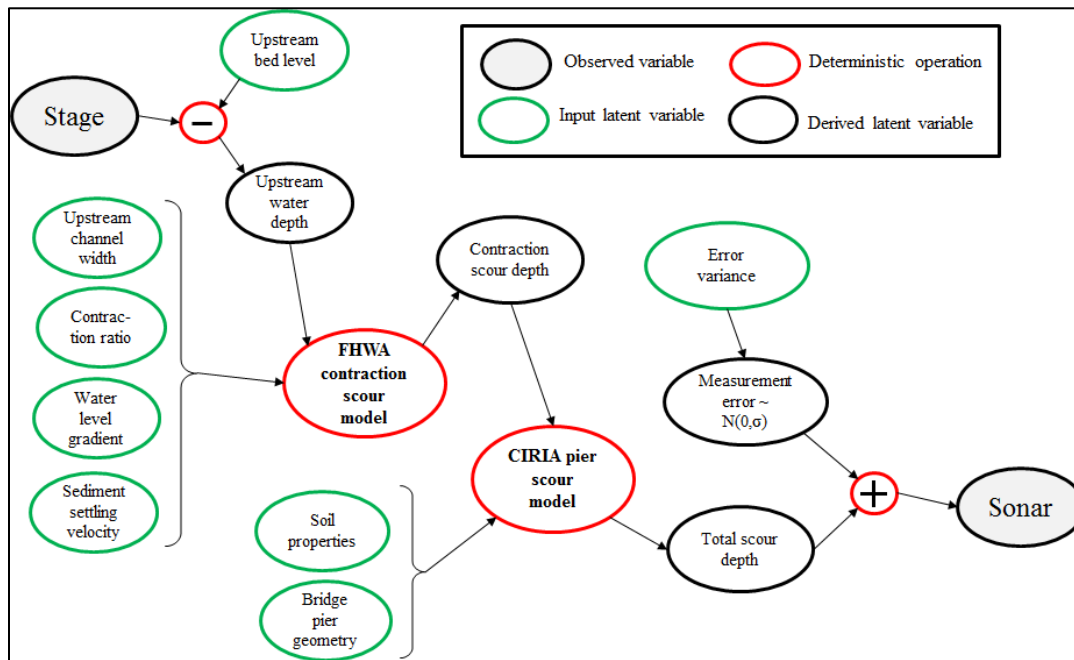


Figure 9 Graphical representation showing Bayesian model structure.

15

16 The empirical equations applied in this study for estimating local and contraction scour are described in the
 17 following sections.

18

19 *CIRIA Local Scour Model*

20 Local scour around a pier is assessed as the product of the pier width (D) and a number of factors depending
 21 on the flow depth (F_{depth}), angle of attack (F_{angle}), flow velocity ($F_{velocity}$), pier shape (F_{shape}), and debris
 22 condition (F_{debris}) as shown in **Equations 2 to 6**. F_{shape} varies between 1.15 and 2.0 and F_{debris} varies between
 23 1.0 and 1.48. S_F is a safety factor related to the assumed probability of exceedance [30].

24

$d_s = D \times (F_{angle} \times F_{shape} \times F_{depth} \times F_{velocity} \times F_{debris}) \times S_F$	(2)
$F_{angle} = \left(\cos \alpha + \left(\frac{L}{D} \right) \sin \alpha \right)^{0.62}$	(3)

$F_{depth} = 0.55 \left(\frac{Y_B}{D} \right)^{0.60}, \text{ for } \frac{Y_B}{D} \leq 2.7$ $F_{depth} = 1.0, \text{ for } \frac{Y_B}{D} > 2.7$	(4)
$F_{velocity} = 0, \text{ for } \frac{V}{V_c} \leq 0.375$ $F_{velocity} = 1.6 \left(\frac{V}{V_c} \right) - 0.6, \text{ for } 0.375 < \frac{V}{V_c} < 1$ $F_{velocity} = 1, \text{ for } \frac{V}{V_c} \geq 1$	(5)
$V_c = -\sqrt{32} \log_{10} \left(\frac{k_s}{12Y_B} + \frac{0.222\nu}{Y_B V_*} \right) V_*$	(6)

1 In the equations above L is pier length, α is the angle of attack, V is the mean channel velocity. V_c is the
2 critical velocity for sediment motion, Y_B is the flow depth, ν is the kinematic viscosity of water (equal to
3 $1.14e^{-6}$ at 15°C), k_s is the effective roughness, taken as D_{50} (median size of bed material) for uniform
4 sediment and $2*D_{50}$ for well-graded sediment, and V_* is the shear velocity at threshold of sediment
5 movement.

6
7 **FHWA (HEC-18) Contraction Model**
8 Depending on the flow velocity either **Equation 7** (live-bed contraction scour) or **Equation 8** (clear-water
9 conditions) is applied. The depth of contraction scour (d_g) is estimated using **Equation 9** [29].

$\frac{Y_B}{Y_u} = \left(\frac{Q_2}{Q_1} \right)^{\frac{6}{7}} \left(\frac{W_u}{W_B} \right)^{k_1}$	(7)
$Y_B = \left(\frac{K_u Q^2}{\frac{2}{D_m^3} W_B^2} \right)^{\frac{3}{7}}$	(8)
$d_g = Y_B - Y_e$	(9)

10 In the equations above Y_u is the average flow depth in the upstream main channel, Y_B is the average flow
11 depth in the contracted section, Y_e is the existing flow depth in the contracted section before scour, which
12 can be approximated by Y_u for sand and gravel beds. Q is the discharge through the bridge, Q_1 is the
13 discharge in the upstream channel, Q_2 is the discharge in the contracted channel, W_u is the width of the
14 upstream main channel, W_B is the width of the main channel in the contracted section, k_1 is an exponential
15 constant, D_m is the diameter of the smallest non-transportable particle taken as $1.25*(D_{50})$, K_u is a constant
16 equal to 0.025 (SI unit) or 0.0077 (English units).

17 **Table 5** provides a summary of latent and observed model parameters and adopted prior distributions (U
18 represents the uniform probability distribution).

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1

2 **TABLE 5 Latent and observed model parameters (variables) for Bayesian regression**

Variable name	Variable Type	Units	Prior Distribution	Observed value(s)
Upstream bed elevation	Latent	ft	U (31,36.5)	-
Upstream channel width	Latent	ft	U (150,500)	-
Contraction ratio	Latent	-	U (1.0,1.3)	-
Sediment settling velocity	Latent	ft/s	U (1.64,32.8)	-
Water surface friction slope	Latent	-	U (0,0.02)	-
Pier length	Latent	ft	U (5,10)	-
Pier shape factor (Fshape)	Latent	-	U (1.0,1.2)	-
Manning coefficient	Latent	-	U (0.02,0.06)	-
Friction velocity	Latent	ft/s	U (0.14,0.3)	-
Pier angle of attack	Latent	-	U (0, $\pi/3$)	-
(Nikuradse) Sand grain roughness	Latent	-	U (0.005,0.02)	-
Error standard deviation	Latent	ft	U (0.5,3.0)	-
Pier width	Observed	ft	-	4.3
Scoured bed elevation	Observed	ft	-	sonar sensor
Water level	Observed	ft	-	stage sensor

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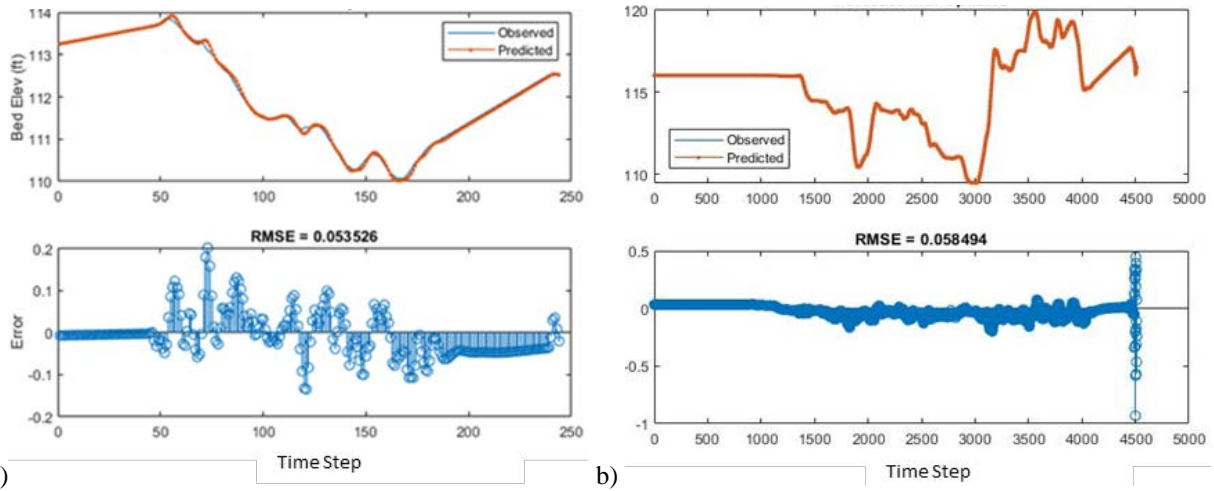
4 **RESULTS AND DISCUSSIONS**

5

6 **Method 1: LSTM Predictions**

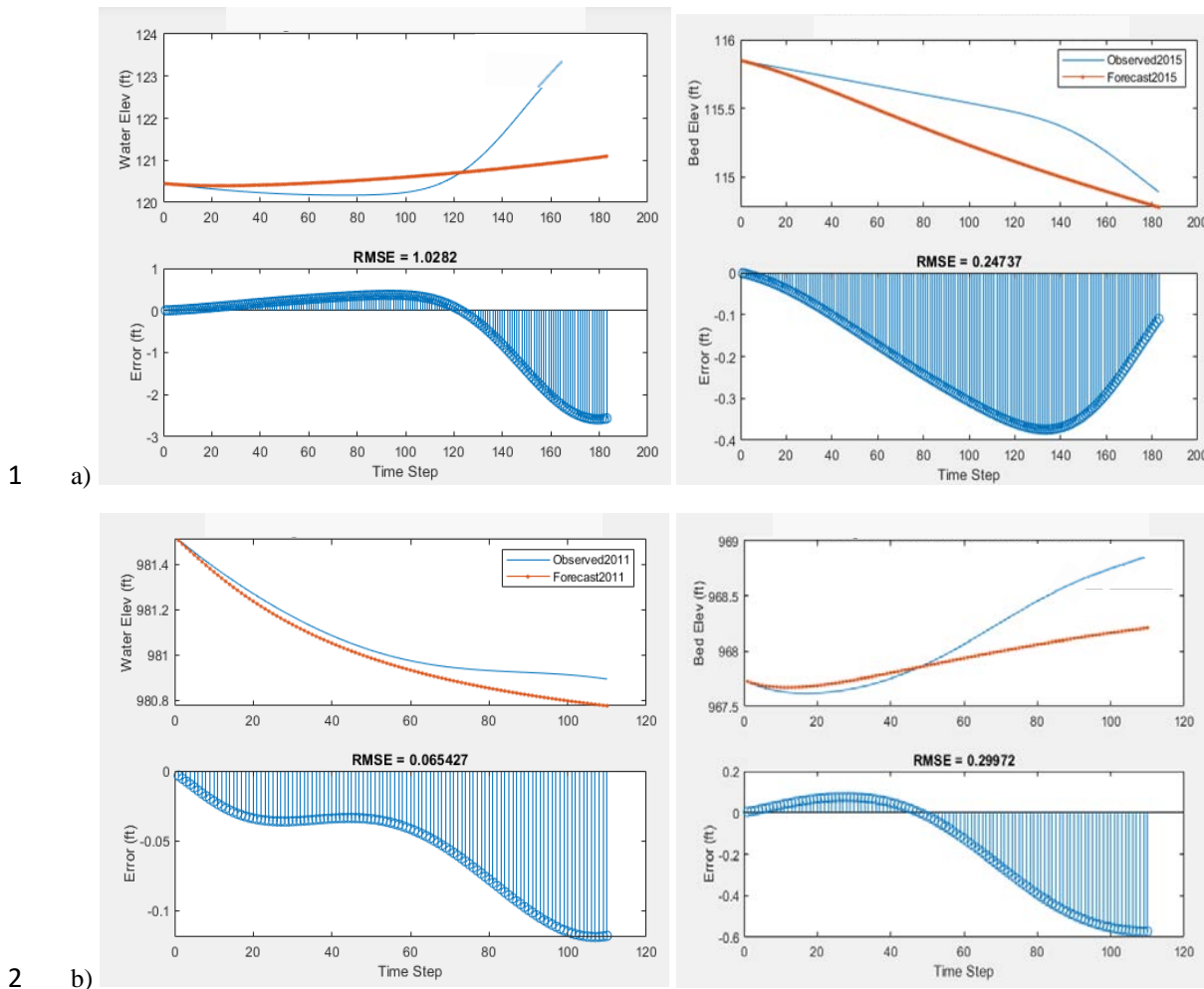
7 **Figure 10** shows examples of the LSTMs’ performance over test datasets for 1hr ahead predictions, using
 8 single sequence training method. At each time step, the LSTM model predicts the stage water and bed
 9 elevation, provided the actual sensor readings at the previous time steps. **Figure 11** shows the LSTM
 10 predictions of stage water and bed elevation for 7 days in advance, based on multiple sequence training
 11 methods. Seven to ten days was considered as a reasonable forecast window for early warnings of a bridge
 12 scour event. Across the forecast window, instead of the actual readings, the LSTM predicted values for a
 13 time-step are input to the next time step.

14 The 1hr ahead forecasts were highly accurate, showing Root Mean Squared Error (RMSE) close to zero,
 15 and as expected, the accuracy decayed as the forecast window was extended to 7-10 days. The LSTMs’
 16 performance showed to vary, depending on the bridge and quality of the data. The average RMSE on bed
 17 elevation predictions over 7-10 days forecast window was estimated between 1-5 ft.



1 a) b)
2 **Figure 10 LSTM performance over test datasets, trained using single sequences with, a) 1 year of**
3 **sensor data, b) 11 years of sensor data – 1hr forecast window, bridge 742 [time-step=1 hr]**

4



1 a)
 2 b)
 3 **Figure 11 LSTM performance over test datasets, trained using synchronized sequences, a) bridge**
 4 **742-2015, b) bridge 524-2011 – 7 to 10 days forecast window [time-step=1 hr]**

5 These results show a great potential in real-time assessment of scour around bridge piers using LSTMs. It
 6 should be noted that in general, LSTMs are extremely “data-hungry.” The size of the database available for
 7 training in this study was relatively small in deep learning terms. The performance of the developed LSTMs
 8 is expected to improve further, as more data is received and included in the training process in the future
 9 phases of this study.

10
 11 **Method 2: MLP Ensemble Predictions**

12 Stepwise parameter selection (forward selection and backward elimination) analyses were carried out to
 13 optimize the MLP performance by removing the redundant parameters and identifying the most relevant
 14 input parameters for maximum scour depth prediction. The following input parameters were selected for
 15 the final configuration of the MLP networks:

- 16 • Flow depth at t_0
- 17 • Flow depth at t_n
- 18 • Scour depth at t_0
- 19 • Scour depth at t_n
- 20 • Manning’s coefficient
- 21 • Valley slope

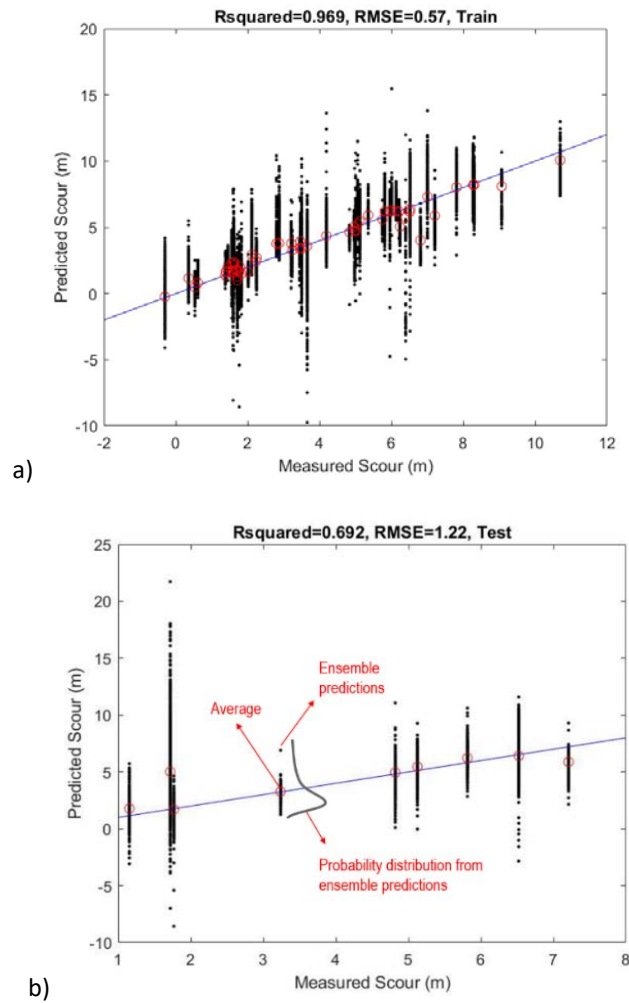
- Aggregate size, D_{50}

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Figure 12 shows the performance of the MLP ensembles for maximum scour depth prediction over training and test datasets. The black dots show individual predictions from each network in the ensemble, and the red circles show the average predictions. Summary statistics for the MLP ensemble performance, including the R^2 of predicted versus measured values, as well as $RMSE$ are provided in **Table 6**. This includes the performance over a control data set which was set aside during model development. R^2 of 0.7 for the test dataset and 0.91 for the control dataset (equivalent to 1.2m and 0.9m prediction error, respectively) show that this approach can be used to make reasonably accurate predictions on maximum scour depth.

The MLP ensembles method shows to outperform the commonly-used empirical models reported in [34]. SSE (sum of squared errors divided by sum of squared measured values $\times 100\%$), the performance metric used in [34] is estimated 6.67% over the test dataset and 3.79% over the control dataset. Comparing this with the performance of the best reported empirical model [37] with 6.8% SSE proves this claim.

Moreover, as shown in **Figure 12**, the range of predictions by ensemble networks for each scour episode allows for uncertainty quantification and probabilistic inferences, such as estimating confidence intervals and percentile values.



1 **Figure 12 MLP ensemble predictions over a) training dataset and b) test dataset, showing R^2 and**
 2 **RMSE of predictions. Blue line is the equity line.**

3 **TABLE 6 Performance of the MLP ensembles over data subsets**

Dataset	R^2	RMSE, ft (m)
Training Subsets (average)	0.97	2 (0.6)
Test Subsets (average)	0.70	3.9 (1.2)
Control Subset (average)	0.91	2.9 (0.9)

4
 5 **Method 3: Predictions by the Bayesian Empirical Models**

6 Unlike neural networks, which are capable of learning complex, non-linear patterns in data, linear models
 7 are less likely to benefit from large and diverse sets of training data. Thus, the empirical models should be
 8 calibrated on a case by case basis, with limited potential for learnings to transfer between bridges. The sonar
 9 readings from bridge 539 showed good quality, hence the initial models were developed and evaluated
 10 using this dataset.

11 After generating the joint posterior probability distribution of all latent parameters of the empirical models,
 12 the models were used to make posterior predictions on bed elevation. This was performed by drawing a
 13 large number of samples, using Monte Carlo method, from the joint posterior probability distribution of
 14 latent parameters, for each value of stage water and then using empirical scour model to estimate the scour
 15 depth. Using the generated predictions, the 5th, 50th and 95th percentile values from the posterior predictive
 16 distribution of bed level (i.e. sonar readings) were obtained. The range between the P5 and P95 values can
 17 be considered as the 90% credible interval for the predicted scour depth. This range was compared against
 18 the actual sonar readings (see **Figure 13** and **14**).

19
 20 *Global Fit*

21 A “global” model was trained using the whole dataset between 2008 to 2012. The model predictions on the
 22 training datasets and the test dataset taken from 2014 are shown in **Figure 13**.

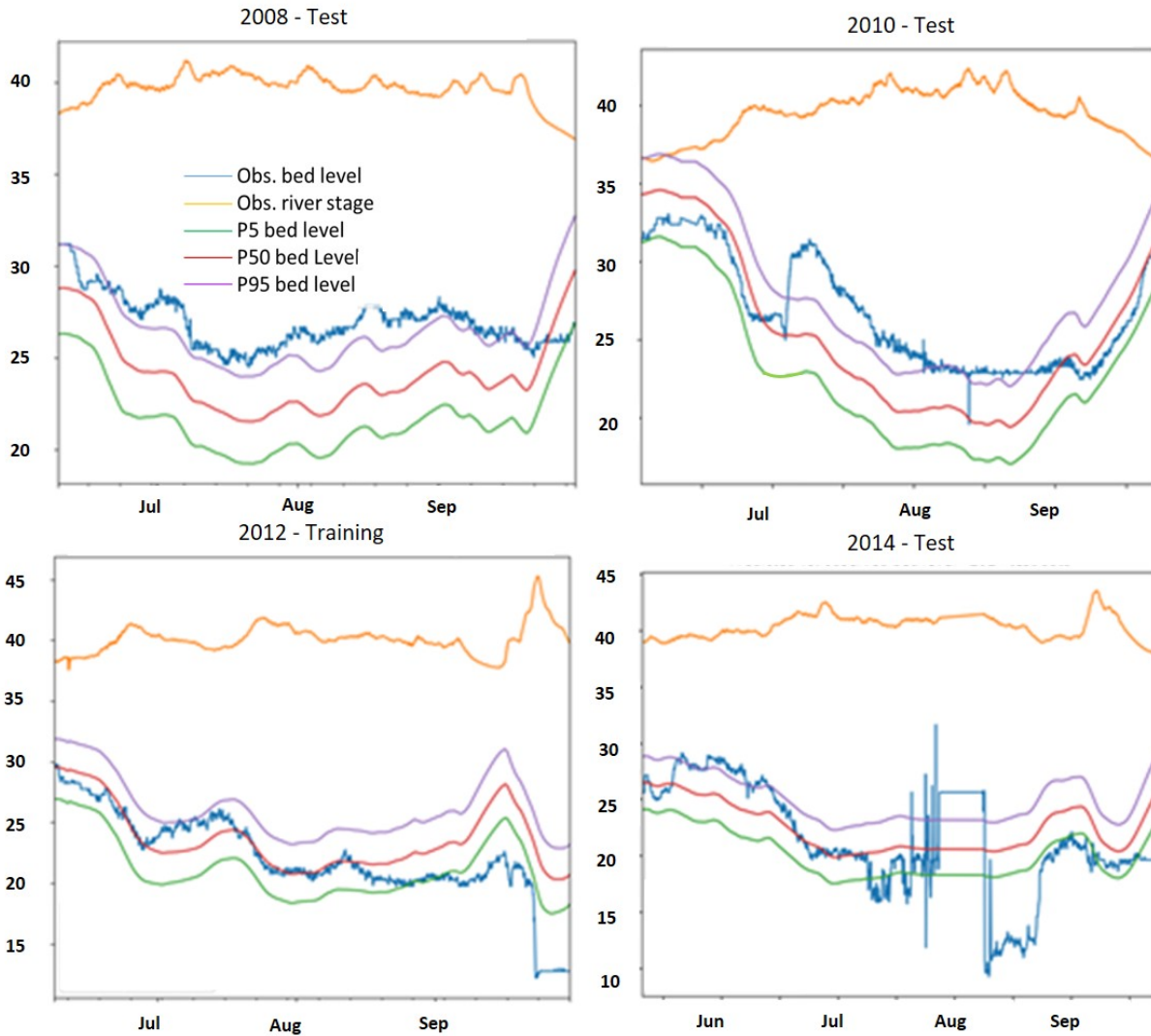


1 **Figure 13 Model predictions on 2008-2012 training dataset and test dataset from 2014 (x axis is time,**
 2 **y axis is elevation in ft).**

3
 4 *Seasonal/Local Fit*

5 In this analysis, it was of interest to know what quantity of observed data would be required to make useful
 6 predictions on unseen data. For example, is it possible to deploy temporary sensors during one season only
 7 to calibrate a model which can then be used reliably in future years? If this was the case, then the cost of
 8 monitoring could be significantly reduced.

9 **Figure 14** shows an example of prediction results using this method. Training data was extracted from the
 10 date range from 15th June to 31th August 2012. Model predictions on the training dataset are reasonably
 11 accurate, with the observed data mostly falling inside the 90% credible interval. Predictions on test data
 12 shows a general tendency to underestimate bed elevations in 2008 but shows better agreement in other
 13 years. The most noticeable discrepancies with the observed data coincides with sections where the actual
 14 readings are seemingly erroneous, for example the sudden bump in the sonar readings in early June 2010,
 15 or fluctuations in August 2014.



1 **Figure 14 Model predictions on 2012 training dataset and test dataset from years 2008, 2010 and**
 2 **2014 (x axis is time, y axis is elevation in ft).**

3
 4 The *RMSEs* for the “global” and “seasonal” models, based on the P50 (median) values from the posterior
 5 predictive distributions are shown in **Table 7**. Qualitatively, there is no strong evidence that training over
 6 multiple years could result in more accurate predictions. The predictions are generally accurate to within
 7 2-3 ft, with the largest errors generally explained by measurement errors rather than modelling errors.
 8

9 **TABLE 7 RMSE in predicted bed elevation, ft (m) for models trained against long term data (2008 -**
 10 **2012) and single season of data (2008 and 2012).**

Test Period	Training Period		
	Global: 2008-2012	Local: 2008	Local: 2012
2008	2.0 (0.6)	1.2 (0.4)	3.3 (1.0)
2010	2.0 (0.6)	2.3 (0.7)	2.9 (0.90)
2012	3.9 (1.2)	5.3 (1.5)	3.1 (0.90)
2014	4.9 (1.5)	6.0 (1.8)	3.8 (1.2)

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Implementation Remarks

Each of the three introduced methods is designed for a specific implementation/application purpose:

Method 1: *Real-time Scour Early Warning System*. The application of this method is straightforward, as the AI models will be trained using historical data for a bridge and then retrained as new monitoring data is fetched on a real-time basis. The training process can be reduced to several hours on a CPU or GPU cluster or other high-performance computing (HPC) systems, depending on the amount of data and the training process (e.g. number of epochs, number of mini-batches, and sequence length). This method provides real-time scour depth forecast (as well as stage water forecast).

Method 2: *Holistic Scour Prediction*. This method can be applied for any bridge at any location once the models are trained with a well-populated database from bridges in the area. The training on a HPC system is estimated to take up to several hours depending on the size of the database. The predicted maximum scour depth using this method can inform decision making and scour risk assessments.

Method 3: *Bayesian Empirical Scour Prediction*. This method can be implemented to predict upcoming scour depth at a bridge and provide systematic uncertainty assessments. The Bayesian calibration process can be time-intensive depending on the HPC system. Hydro-meteorological models will be required to forecast the stage water height (flow depth) as an input to the scour empirical equations.

SUMMARY AND CONCLUSIONS

New methodologies were developed using advanced AI/ML technics for early forecast of scour and maximum scour depth prediction based on real-time monitoring data. Sonar and stage sensor data were collected for a number of bridges in the US, along with other physical characteristics relevant to scour process, such as bridge geometry, river flow, and riverbed condition.

As the first approach, recurrent neural network models, LSTMs, were developed and trained to predict the trend of bed elevation and stage water variations over a predefined forecast window of 1hr to 10 days in advance, to provide a real-time early warning system. The main advantage of this approach is the ability to predict the stage water level in parallel to scour (flood forecast). Validation results revealed a good potential for this approach to be implemented for real-time scour forecast, with an average prediction error of 1-5 ft. It should be noted that accuracy of predictions using this approach may vary in a case by case basis, depending on the quality of the training data, scour process variations, and how well the network is trained over the collected dataset. Authors expect to further improve the algorithms introduced in this study in the upcoming phases.

As the second approach, ensembles of feedforward neural networks were developed and trained using both observed sensor data as well as bridge, flow and riverbed characteristics. This approach provides a holistic, physically-driven predictive model that can make reasonably accurate predictions on the maximum scour depth during a high-flood season. Unlike the first approach, the developed algorithms are robust in making predictions for bridges from different locations and do not require individual calibration and training for each bridge; once trained with spatially diverse database of bridges, they theoretically can make reasonable forecast for any selected bridge. In addition, using the random subsampling (ensemble) method, a probabilistic framework was introduced to capture the uncertainty and facilitate risk-based solutions for scour management.

Third approach implemented semi-empirical scour models and calibrated them using Bayesian regression based on the observed sensor data. This approach proved successful in predicting the scour depth with acceptable accuracy, while allowing for systematic uncertainty quantification. This method is specifically advantageous when attempting to extrapolate to extreme conditions (for example, floods with return periods larger than 100 years), which are highly unlikely to be represented in the available training data. Another advantage of this approach is the familiarity of bridge management authorities with the applied empirical models. Current state of practice requires bridge operators to perform regular surveys of

1 bed profiles and apply empirical models to estimate scour failure risk for a range of pre-defined flood
2 events. One disadvantage of this approach is that, unlike the first and second approach, it requires the river
3 stage data to be available throughout the forecast window, hence requires a flood forecast model in parallel.

4 The commonly used empirical scour models have been developed based on pre-defined regression
5 models and calibrated with local, limited data. These models have proven unreliable, too conservative in
6 some cases, yet underpredicting scour depth in other cases. The developed AI/ML models in this study
7 showed to outperform these traditional methods. These advanced algorithms in combination with real-time
8 monitoring systems can provide bridge owners with robust, cost-effective tools for scour risk management.
9 Considering the significant costs and causalities associated with bridge scour failure, implementing such
10 state-of-the-art technologies can be a revolution in the bridge management practice.

11
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19
20 **AUTHOR CONTRIBUTIONS**

21 The authors confirm contribution to the paper as follows: study conception and design:
22 N. Yousefpour, S. Downie, S. Walker; data collection: N. Yousefpour, H. Dikanski; analysis and
23 interpretation of results: N. Yousefpour, S. Walker, S. Downie, N. Perkins, H. Dikanski; draft manuscript
24 preparation: N. Yousefpour. All authors reviewed the results and approved the final version of the
25 manuscript.
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